Precision Higgs Physics the Next Step

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Outline: there are three vital steps or stages one must climb

- Theoretical precision: Missing Higher Orders (MHO)
- On Off Shell: the Dalitz sector



BSM: SM ⊕ *d* = 6 operators



Chiara Mariotti, Reisaburo Tanaka Ansgar Denner and André David

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Assertion

Precision Physics: restricting our attention to the relative merits of realism and instrumentalism. Do we have a way of knowing whether "unobservable" theoretical entities really exist, or that their meaning is defined solely through measurable quantities?

Leplin (1984), Sokal (2001)



Here we go



From my Logbook:

now we must move on to the next step

melting BSM-physics with high-precision SM-technology $The \ question \ has \ been \ repeated$

many times



• Answers converging around Not yet

 Meanwhile, it came dangerously close to realizing a nightmare, of Physics done by sub-sets of diagrams instead of cuts.

Well, several years ago we avoided that fate, may be The history will repeat itself?



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Missing Higher Orders



The traditional way for estimating THEORETICAL UNCERTAINTIES associated to collider physics is based on the notion of **QCD** scale variation

We introduce the concept of

MHO(MHOU), missing higher order (uncertainty), which has to do with the TRUNCATION ERROR IN THE PERTURBATIVE EXPANSION;

 \mathcal{I}_n the past 30 years the commonly accepted way for estimating MHOU has been based on scale variations.

Consider an observable $\sigma(Q,\mu)$ where

- **Q** is the typical scale of the process and
- μ ≡ {μ_R, μ_F} are the renormalization and factorization scales. The *conventional strategy* defines

$$\begin{split} &\sigma_{\xi}^{-} = \min \Big\{ \sigma \left(\mathcal{Q}, \frac{\mu}{\xi} \right), \sigma \left(\mathcal{Q}, \xi \mu \right) \Big\}, \\ &\sigma_{\xi}^{+} = \max \Big\{ \sigma \left(\mathcal{Q}, \frac{\mu}{\xi} \right), \sigma \left(\mathcal{Q}, \xi \mu \right) \Big\}, \end{split}$$

• selects a value for ξ (typically $\xi = 2$) and predicts $\sigma^{-} \leq \sigma \leq \sigma^{+}$

There is an open and *debatable* question on how to assign a probability distribution function (**pdf**) to the **MHOU**

- the *generally accepted* one is based on a Gaussian (or log-normal) distribution centered at $\sigma(Q, Q)$. What to use for the standard deviation, remains an *open problem*.
- Alternatively, it can be assumed that the pdf is a FLAT-BOX

Recently, there has been a proposal by Cacciari and Houdeau, based on a flat (**uninformative**) Bayesian prior for the MHOU. *More* generally, dependence on scales is only part of the problem: indeed, the MHO problem is based on the following fact: given an observable \mathcal{O} , related to a perturbative series

$$\mathscr{O} \asymp \sum_{n=0}^{\infty} c_n g^n$$

how should we interpret the relation?

- The perturbative expansion is unlikely to converge, simon, 1972
- the asymptotic behavior of the coefficients is expected to be

$$c_n ~\sim~ K \, n^lpha \, {n! \over S^n}, \quad n \,{ o} \, \infty \qquad$$
 Vainshtein 1994

The requirement of Eq.(1) (≍) is not a formal one, it has a physical content: it means that there is a smooth transition between the system with interaction and the system without it, **Fischer** 1995. Furthermore, Borel and Carleman proved that there are analytic functions corresponding to arbitrary asymptotic power series.

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We (A. David and I) did not answer general questions (e.g. to prove uniqueness) but concentrated (arXiv:1307.1843 [hep-ph]) on

predicting higher orders

using the well-known concept of "series acceleration", i.e. one of a collection of **sequence transformations (ST)** for improving the rate of convergence of a series.

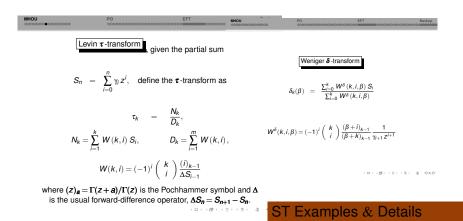
- If the original series is divergent, the ST acts as an extrapolation method
- in the case of infinite sums, STs have the effect that sums that formally diverge may return a result that can be interpreted as evaluation of the analytic extension of the series for the sum.
- the relation between Borel summation (usual method applied for summing divergent series) and these extrapolation methods is known
- Note that the definition of a sum of a factorially divergent series, including those with non-alternating coefficients, is always equivalent to Borel's definition, Suslov 2005

Example

$$S_{\infty} = \sum_{n=0}^{\infty} n! z^{n+1} = e^{-1/z} \operatorname{Ei}\left(\frac{1}{z}\right)$$

where the **exponential integral** is a single-valued function in the plane cut along the negative real axis. However, for z > 0 Ei(z) can be computed to great accuracy using several Chebyshev expansions. Note that the r.h.s. is the **Borel sum of the series**.

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The whole strategy is based on the fact that one can predict the coefficients by

- constructing an approximant with the known terms of the series (γ₀,..., γ_n) and
- expanding the approximant in a Taylor series. The first *n* terms of this series will exactly agree with those of the original series and

the subsequent terms may be treated as the predicted coefficients. i.e. if S_1, \ldots, S_k are known, one computes

$$\tau_k - S_k = \overline{\gamma}_{k+1} z^{k+1} + \mathscr{O}\left(z^{k+2}\right)$$

 $\rightarrow \overline{\gamma}_{k+1}$ is the prediction for γ_{k+1}

How to use it?

Consider a specific example, $gg \rightarrow H$. Define

$$\sigma_{\rm gg}\left(\tau\,,\,\textit{M}_{\rm H}^{2}\right) \ = \ \sigma_{\rm gg}^{0}\left(\tau\,,\,\textit{M}_{\rm H}^{2}\right)\,\textit{K}_{\rm gg}\left(\tau\,,\,\textit{M}_{\rm H}^{2}\,,\,\alpha_{\rm s}\right)$$

where $\tau = M_{\rm H}^2/s$ and $\sigma_{\rm gg}^0$ is the LO cross section. The *K*-factor admits a formal power expansion in $\alpha_{\rm s}(\mu_{\rm R})$

$$K_{gg}\left(au, M_{\mathrm{H}}^{2}, lpha_{\mathrm{s}}
ight) = 1 + \sum_{n=1}^{\infty} \, lpha_{\mathrm{s}}^{n}(\mu_{\mathrm{R}}) \, K_{\mathrm{gg}}^{n}$$

Known coefficients are 11.879 and 72.254

In their recent work, Ball et al, (Ball:2013bra) computed (at $\sqrt{s} = 8 \text{ TeV}$)

$$\begin{aligned} \alpha_{\rm s}^3 \left(\frac{M_{\rm H}}{2}\right) \, \mathcal{K}_{\rm gg}^3 \left(\mu = \frac{M_{\rm H}}{2}\right) &= 0.323 \pm 0.059 \\ \alpha_{\rm s}^3 \left(M_{\rm H}\right) \, \mathcal{K}_{\rm gg}^3 \left(\mu = M_{\rm H}\right) &= 0.527 \pm 0.043 \\ \alpha_{\rm s}^3 \left(2\,M_{\rm H}\right) \, \mathcal{K}_{\rm gg}^3 \left(\mu = 2\,M_{\rm H}\right) &= 0.729 \pm 0.032 \end{aligned}$$

Warming up with two coefficients

$$\tau_2 - S_2 = \frac{\gamma_2^2}{\gamma_1} z^3 + \mathscr{O}\left(z^4\right)$$

applied to the ggF series gives

346.42
$$\leq \gamma_3 (\mu = M_H) \leq$$
 407.48 (Ball:2013bra)
 $\bar{\gamma}_3 (\mu = M_H) =$ **439.48** \Leftarrow predicted

✤ which has the correct sign and the right order of magnitude.

Introducing

$$S_{\mathrm{N},n} = \sum_{k=0}^{n} \gamma_k z^k + \sum_{k=n+1}^{\mathrm{N}} \overline{\gamma}_k z^k,$$

and $\delta_{N,n}$ etc, constructed accordingly, our strategy for estimating MHO and MHOU can be summarized as follows:

- we select a scale, $\mu = M_{\rm H}$ for gg-fusion
- ESTIMATE THE UNCERTAINTY DUE TO HIGHER ORDERS AT THAT SCALE, I.E. THE (SCALE VARIATION) UNCERTAINTY AT THE CHOSEN SCALE IS PART OF THE UNCERTAINTY DUE TO HIGHER ORDERS AND SHOULD NOT BE COUNTED TWICE

.: we compare

$$\sigma_{gg}^{S,n} = \sigma_{gg}^{0} (\mu = M_{\rm H}) S_{n,3} (\mu = M_{\rm H}) \sigma_{gg}^{\delta,n} = \sigma_{gg}^{0} (\mu = M_{\rm H}) \delta_{n,3} (\mu = M_{\rm H})$$

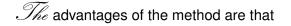
 \mathcal{O}_{ar} conclusion is that, to a very good accuracy,

$$\sigma_{
m gg} ~\in ~ \left[\sigma_{
m gg}^{
m S,3},\sigma_{
m gg}^{\delta,5}
ight]$$

with a flat interval of 16.37%.

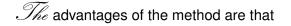
The uncertainty on the width, induced by the error on the coefficient $\gamma_3 (\mu = M_H)$ brings it to 26.01%

 $\label{eq:scales} \overset{\text{$\scales var.}}{\overset{\sigma_{gg} \in [18.90, 21.93]}{\sim} pb} \\ \text{$\scales var.} \\ \begin{array}{c} \text{$\scales var.} \\ \sigma_{gg} \in [20.13, 23.42] \ pb \\ \text{$\scales var.} \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \\ \sigma_{gg} \in [20.13, 23.42] \ pb \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \end{array} \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \end{array} \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \end{array} \\ \begin{array}{c} \text{$\scales var.} \end{array} \\ \end{array} \\ \end{array} \end{array} \\ \begin{array}{c} \text{$\scales var.} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \text{$\scales var.} \end{array} \\ \end{array} \\ \end{array} \\ \end{array}$ \\ \begin{array}{c} \text{\$\scales var.} \end{array} \\ \end{array} \\ \end{array} \end{array} \\ \begin{array}{c} \text



- the result does not depend on the choice of the parameter expansion (it is based on ^{ee} PARTIAL SUMS)^{ee} ✓
- it takes into account the nature of the coefficients, i.e. that the known terms of the perturbative expansion in gg-fusion are positive ✓

► BU1



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- it takes into account the nature of the coefficients, i.e. that the known terms of the perturbative expansion in gg-fusion are positive ✓

► BU1



The corresponding pdf could be derived by following the work of Cacciari and Houdeau giving

$$egin{aligned} \mathcal{P}_{ ext{CH}}(\sigma) &= \mathcal{N}_{\sigma}^{-1} egin{cases} &\left(egin{aligned} rac{\Delta\sigma}{\sigma_+ - \sigma}
ight)^5 & ext{if} & \sigma_- \leq \sigma \leq \sigma_+ \ &\left(rac{\Delta\sigma}{\sigma_- \sigma_-}
ight)^5 & ext{if} & \sigma > \sigma_+ \ &\left(rac{\Delta\sigma}{\sigma_- \sigma_-}
ight)^5 & ext{if} & \sigma > \sigma_+ \ &\sigma_- = \sigma_{ ext{gg}}^{ ext{S},3} & \sigma_+ = \sigma_{ ext{gg}}^{ ext{\delta},4} \ &\Delta\sigma = \sigma_+ - \sigma_- & \mathcal{N}_{\sigma} = rac{3}{2}\Delta\sigma \end{aligned}$$

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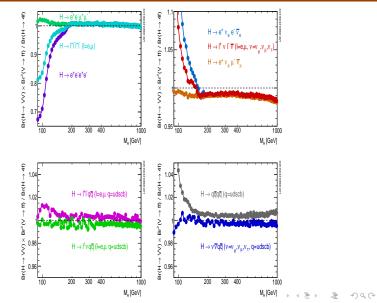
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Preudo Observables

What does the term "Higgs decay" mean? A mathematical expression? But what does it mean for such an expression to exist in the physical world? Trying to answer that question immediately raises other questions about the correspondence between mathematical objects and the physical world

EFT

from **PROPHECY4F**

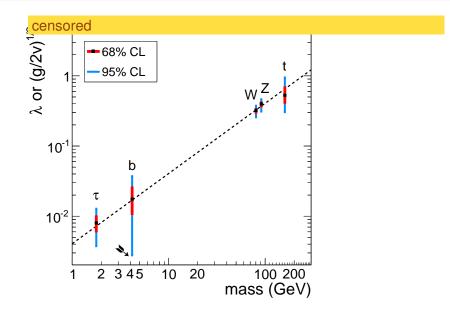


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These plots are one of the best examples that

$$\begin{array}{ccc} \mathsf{BR}(\mathrm{H} \mathop{\rightarrow} \mathrm{VV}) & \otimes & \mathsf{BR}^2\left(\textit{V} \mathop{\rightarrow} \bar{\mathrm{f}}\mathrm{f}\right) \\ \neq & \\ \mathsf{BR}\left(\mathrm{H} \mathop{\rightarrow} 4\mathrm{f}\right) \end{array}$$

Trivial but true, $\hookrightarrow H \to VV$ is not a physical OBSERVABLE, eventually it can be *defined* as "PSEUDO-OBSERVABLE"



\mathcal{T}_{he} previous plot (**couplings** \rightleftharpoons **masses**) is another example that

POs can be defined (couplings) **Iff** the rules of the game are respected

- MODEL-INDEPENDENT couplings are *extracted* in some *effective* way that includes QCD but not NLO EW
- If one wants to obtain the SM (the straight line) → use RUNNING MASSES m_f(M_H)

 EFT



Theorem \nexists $H \rightarrow Z + \gamma, H \rightarrow VV$ etc.do not exist/make sense since $\downarrow \downarrow$ $\gg V \notin$ \downarrow in/out > bases of the Hilbert space

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High Precision Road



$$\label{eq:MH} \textit{M}_{\rm H} = 125.5 ~\textit{GeV} ~ \textit{BR} \, ({\rm H} \rightarrow e^+ e^-) = 5.1 \, \times \, 10^{-9}$$

while a naive estimate gives

$$BR\left(H\rightarrow Z\gamma\right)BR\left(Z\rightarrow e^+e^-\right) \ = \ 5.31\times 10^{-5}$$

4 orders of MAGNITUDE larger

How much is the corresponding PO extracted from full Dalitz Decay? We could expect $\Gamma(H \rightarrow e^+e^-\gamma) = 5.7\% \Gamma(H \rightarrow \gamma\gamma)$ but photon

isolation must be discussed.





$\label{eq:transform} \begin{array}{l} \mbox{Terminology:} \\ \mbox{The name Dalitz Decay must be reserved for the full process} \\ \mbox{$H \to \bar{f}f\gamma$} \\ \mbox{Subcategories:} \end{array}$

$$\left\{ \begin{array}{ll} H \rightarrow Z^{*}\left(\rightarrow \bar{f}f\right) + \gamma & \And \textbf{unphysical}^{1} \\ H \rightarrow \gamma^{*}\left(\rightarrow \bar{f}f\right) + \gamma & \And \textbf{unphysical} \\ H \rightarrow Z_{c}\left(\rightarrow \bar{f}f\right) + \gamma & \textbf{PO}^{2} \end{array} \right.$$

 ${}^{1}Z^{*}$ is the off-shell Z ${}^{2}Z_{c}$ is the Z at its complex pole

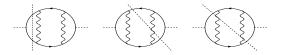
EFT

Understanding the problem

$$\mathbf{H} \rightarrow \mathbf{\bar{f}} \mathbf{f} \quad \text{or} \quad \mathbf{H} \rightarrow \mathbf{\bar{f}} \mathbf{f} + \boldsymbol{n\gamma}$$
?

Go to two-loop, the process is considerably more complex than, say, $H \rightarrow \gamma \gamma$ because of the role played by QED and QCD corrections.

The ingredients needed are better understood in terms of cuts of the three-loop H self-energy (



Moral: Unless you Isolate photons you don't know which process you are talking about $H \rightarrow \overline{f}f$ NNLO or $H \rightarrow \overline{f}f\gamma$ NLO

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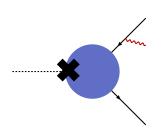
The complete **S**-matrix element will read as follows:

$$\begin{split} \mathcal{S} &= \left| \mathcal{A}^{(0)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \right) \right|^2 \\ &+ \left. 2 \operatorname{Re} \left[\mathrm{A}^{(0)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \right) \right]^{\dagger} \mathrm{A}^{(1)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \right) \\ &+ \left| \mathcal{A}^{(0)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \gamma \right) \right|^2 \mathcal{X} \\ &+ \left. 2 \operatorname{Re} \left[\mathrm{A}^{(0)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \right) \right]^{\dagger} \mathrm{A}^{(2)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \right) \\ &+ \left. 2 \operatorname{Re} \left[\mathrm{A}^{(0)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \gamma \right) \right]^{\dagger} \mathrm{A}^{(1)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \gamma \right) \mathcal{X} \\ &+ \left| \mathcal{A}^{(0)} \left(\mathrm{H} \to \bar{\mathrm{f}} \mathrm{f} \gamma \gamma \right) \right|^2 . \end{split}$$

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Don't get trapped by your intuition, the **IR**/collinear stuff will not survive in the limit $m_f \rightarrow 0$

There are **genuinely non-QED(QCD)** terms surviving the **zero-Yukawa** limit (a result known since the '80s)

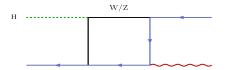


2f H-BRs below $10^{-3}-10^{-4}$ pose additional TH problems $\Delta BR \gg BR$

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DALITZ BOX



- Collinear/Virtual cancel in the total X
- Gram and Cayley do not generate real singularities X
- Plenty of hard stuff around 🖉

Only the total *Dulits*. *Decay* has a meaning and *can be differentiated through cuts*

- The most important is the definition of *visible photon* to distinguish between $\overline{f}f$ and $\overline{f}f\gamma$
- Next cuts are on **M**(ff) to *isolate* pseudo-observables
- One has to distinguish:
 - $H \rightarrow \bar{f}f+$ soft(collinear) photon(s) which is part of the real corrections to be added to the virtual ones in order to obtain $H \rightarrow \bar{f}f$ at (N)NLO
 - a visible photon and a soft ff-pair where you probe the Coulomb pole and get large (logarithmic) corrections that must be exponentiated.

Unphysical $H \rightarrow Z\gamma \rightarrow \overline{f}f\gamma$ and $H \rightarrow \gamma\gamma \rightarrow \overline{f}f\gamma$



None of these contributions exists by itself, each of

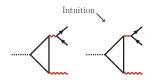
them is NOT even gauge invariant. One can put cuts and

- with a small window around the Z-peak the pseudo-observable H → Z_cγ can be enhanced, but there is a contamination due to many non-resonant backgrounds ✓
- Beware of generic statements box contamination in H → Zγ is known to be small and of ad-hec definition of gauge-invariant splittings √
- at small di-lepton invariant masses γ^* dominates \checkmark

Partial Summary BU2

- $H \rightarrow \overline{f}f$ is well defined and $H \rightarrow \overline{f}f + \gamma$ (γ soft+collinear) is part of the corresponding NLO corrections
- H→ Zγ is not well defined being a gauge-variant part of H→ ff+γ (γ visible) and can be *extracted* (
 in a PO sense) by *cutting the di-lepton invariant mass*.

the best that we can hope to achieve is simply misunderstand at a deeper level

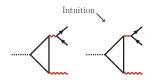


 $\not \in {\rm Facts \ of \ life \ with \ non-resonant}$

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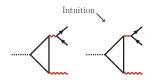


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 $\not \in {\rm Facts \ of \ life \ with \ non-resonant}$

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Results: leptons

$$m(\bar{\mathrm{f}}\mathrm{f}\mathrm{f}) > 0.1\,M_{\mathrm{H}}$$
 $m(\mathrm{f}\gamma) > 0.1\,M_{\mathrm{H}}$ $m(\bar{\mathrm{f}}\gamma) > 0.1\,M_{\mathrm{H}}$

$$\Gamma_{\rm NLO} = 0.233 \ keV \quad \oplus \quad \begin{cases} \Gamma_{\rm LO} = 0.29 \times 10^{-6} \ keV \quad e \\ \Gamma_{\rm LO} = 0.012 \ keV \qquad \mu \\ \Gamma_{\rm LO} = 3.504 \ keV \qquad \tau \end{cases}$$

LO and NLO do not interfere (as long as masses are neglected in NLO), they belong to different helicity sets. Cuts à la Dicus and Repko

Results: quarks

$$m(\bar{\rm f}{
m f}) > 0.1 \, M_{
m H} \qquad m({
m f}{
m \gamma}) > 0.1 \, M_{
m H} \qquad m(\bar{
m f}{
m \gamma}) > 0.1 \, M_{
m H}$$

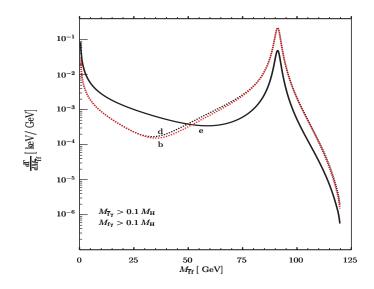
$$\Gamma_{\rm LO} = 0.013 \ keV$$
 $\Gamma_{\rm NLO} = 0.874 \ keV$ d
 $\Gamma_{\rm LO} = 8.139 \ keV$ $\Gamma_{\rm NLO} = 0.866 \ keV$ b

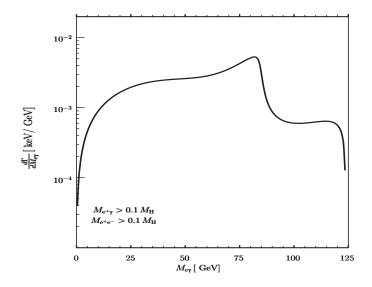
Note the effect of *m*_t



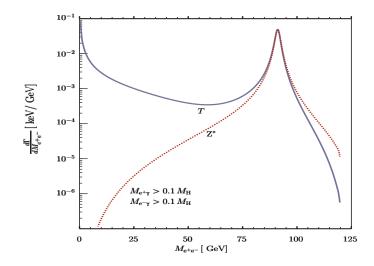
 $m(f\gamma) > 0.1 M_{\rm H}$ $m(\bar{f}\gamma) > 0.1 M_{\rm H}$ $\Gamma_{\rm NLO}[keV]$ $\begin{array}{cc} m(\bar{\rm f}{\rm f}) > 0.1\,M_{\rm H} & m(\bar{\rm f}{\rm f}) > 0.6\,M_{\rm H} \\ 1 & 0.233 & 0.188 \\ d & 0.874 & 0.835 \end{array}$ b 0.866 0.831 $\Gamma_{\rm LO}[keV]$ $m(\bar{\mathrm{f}}\mathrm{f}) > 0.1 \, M_\mathrm{H} \quad m(\bar{\mathrm{f}}\mathrm{f}) > 0.6 \, M_\mathrm{H}$ μ 0.012 d 0.013 0.010 0.011 8.139 6.745 b

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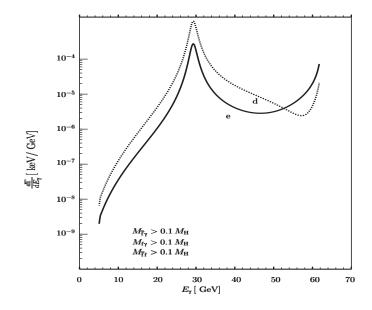




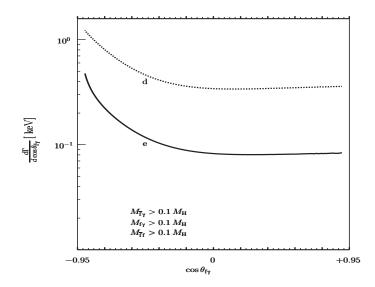
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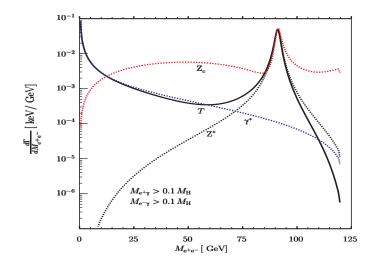


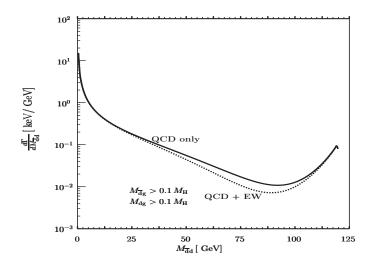
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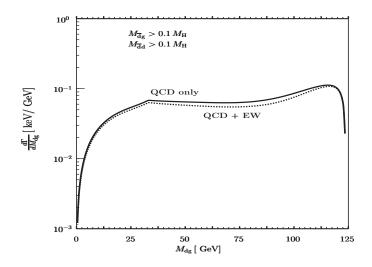


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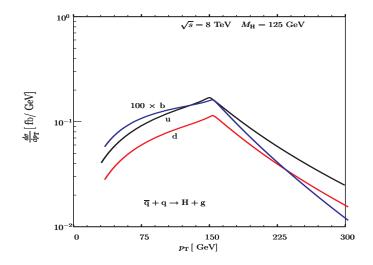




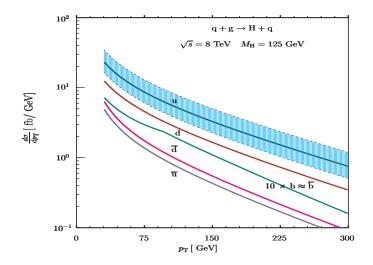




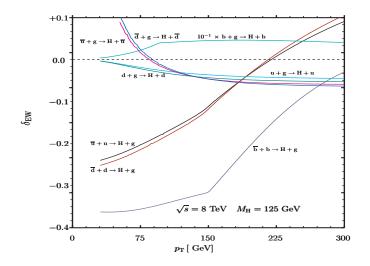
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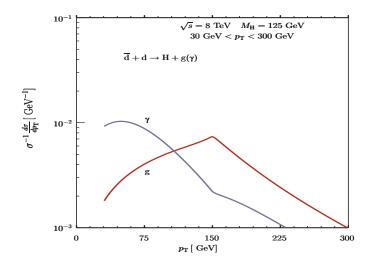


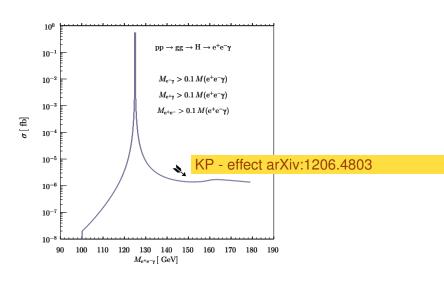
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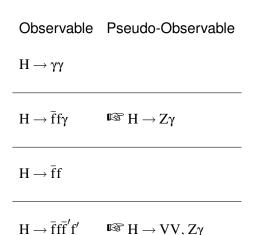
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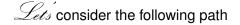


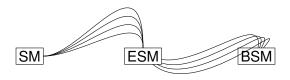
One needs to define when it is $\mathbf{4f}$ final state and when it is PAIR

CORRECTION to **2f** final state (as it was done at LEP2)

Effective Field Theory

Renormalization - group view of the world





The ontology of the SM on its scale should be understood as arising from the "emergent" effects of a more fundamental BSM at a finer scale

$$\begin{aligned} \mathscr{L}_{\text{ESM}} &= \mathscr{L}_{\text{SM}} + \sum_{n>4} \sum_{i=1}^{N_n} \frac{a_i^n}{\Lambda^{n-4}} \, \mathcal{O}_i^{(d=n)} \\ \exists (\exists !) \quad \mathscr{L}_{\text{UCSM}} \quad \rightarrowtail \quad \mathcal{O}_i \, ? \end{aligned}$$

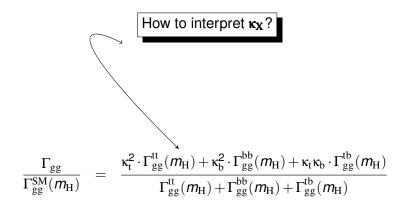
UV completion of the SM (UCSM) or ESM?

Bottom-up or top-down approach to ESM?

- How many facts the theory explains: it is a draw
- Having the fewer auxiliary hypothesis: SM --> UCSM superior
- Analogy: SM should be augmented by all possible terms consistent with symmetries --> ESM

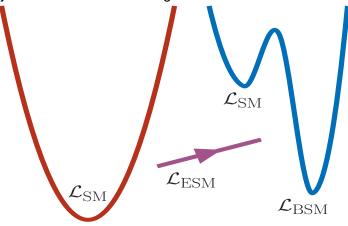
The regulative ideal

of an ultimate theory remains a powerful aesthetic ingredient



Space of Lagrangians (arXiv:1202.3144, arXiv:1202.3415, arXiv:1202.3697)

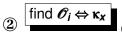
Wilson coefficients in \mathscr{L}_{ESM} are assumed to be small enough that they can be treated at leading order.



Strategy

(1) measure κ

$$\frac{\Gamma_{gg}}{\Gamma_{gg}^{SM}(\textit{m}_{H})} = \frac{\kappa_{t}^{2} \cdot \Gamma_{gg}^{tt}(\textit{m}_{H}) + \kappa_{b}^{2} \cdot \Gamma_{gg}^{bb}(\textit{m}_{H}) + \kappa_{t}\kappa_{b} \cdot \Gamma_{gg}^{tb}(\textit{m}_{H})}{\Gamma_{gg}^{tt}(\textit{m}_{H}) + \Gamma_{gg}^{bb}(\textit{m}_{H}) + \Gamma_{gg}^{tb}(\textit{m}_{H})}$$



(epistemological stop, true ESM believers stop here)

$$\mathscr{L}_{\text{ESM}} = \mathscr{L}_{\text{SM}} + \sum_{n>4} \sum_{i=1}^{N_n} \frac{a_i^n}{\Lambda^{n-4}} \mathscr{O}_i^{(d=n)}$$

(3) find $\{\mathscr{L}_{BSM}\}$ that produces \mathscr{O}_i

$\kappa_X \ cannot$ be arbitrary shifts of the SM diagrams

$$\frac{\Gamma_{gg}}{\Gamma_{gg}^{SM}(\textit{m}_{H})} = \frac{\kappa_{t}^{2} \cdot \Gamma_{gg}^{tt}(\textit{m}_{H}) + \kappa_{b}^{2} \cdot \Gamma_{gg}^{bb}(\textit{m}_{H}) + \kappa_{t}\kappa_{b} \cdot \Gamma_{gg}^{tb}(\textit{m}_{H})}{\Gamma_{gg}^{tt}(\textit{m}_{H}) + \Gamma_{gg}^{bb}(\textit{m}_{H}) + \Gamma_{gg}^{tb}(\textit{m}_{H})}$$

↔ they require an **underlying** (at least **effective**) theory

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 ${\mathscr W}_e$ define an effective Lagrangian based on

a **linear** representation of the EW gauge symmetry with a Higgs-doublet field, restricting ourselves to **dimension-6** operators relevant for Higgs physics Buchmuller:1985jz, Grzadkowski:2010es.



Disclaimer: it is impossible to quote all who have contributed. For what is relevant here:

- Yellow Report HXSWG vol. 3: A. David, A. Denner, M. Dührssen, M. Grazzini, C. Grojean, K. Prokofiev, G. Weiglein, M. Zanetti, S. Dittmaier, G. Passarino and M. Spira
- Contino:2013kra
- Corbett:2013hia
- Elias-Miro:2013gya
- Lopez-Val:2013yba

Lagrangian

$$\mathscr{L}_{\mathrm{eff}} = \mathscr{L}_{\mathrm{SM}}^{(4)} + \frac{1}{\Lambda^2} \sum_{k} \alpha_k \mathscr{O}_k,$$

$$\begin{split} \mathscr{L}^{(4)}_{SM} &= -\frac{1}{4} G^{A}_{\mu\nu} G^{A\mu\nu} - \frac{1}{4} W^{\prime}_{\mu\nu} W^{\prime\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} \\ &+ (D_{\mu} \Phi)^{\dagger} (D^{\mu} \Phi) + m^{2} \Phi^{\dagger} \Phi - \frac{1}{2} \lambda (\Phi^{\dagger} \Phi)^{2} \\ &+ i \bar{l} D l + i \bar{e} D e + i \bar{q} D q + i \bar{\bar{u}} D u + i \bar{\bar{d}} D d \\ &- (\bar{l} \Gamma_{e} e \Phi + \bar{q} \Gamma_{u} u \widetilde{\Phi} + \bar{d} \Gamma_{d} d \Phi + h.c.), \end{split}$$

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$X^2 \Phi^2$	$\psi^2 X \Phi$	$\psi^2 \Phi^2 D$
$\mathscr{O}_{\Phi G} = (\Phi^{\dagger} \Phi) G^{A}_{\mu \nu} G^{A \mu \nu}$	$\mathscr{O}_{\mathbf{u}\mathbf{G}} = (\bar{\mathbf{q}}\sigma^{\mu\nu}\frac{\lambda^{A}}{2}\Gamma_{\mathbf{u}}\mathbf{u}\widetilde{\Phi})\mathbf{G}^{A}_{\mu\nu}$	$\mathscr{O}_{\Phi \mathbf{l}}^{(1)} = (\Phi^{\dagger} \mathbf{i} \overset{\leftrightarrow}{D}_{\mu} \Phi)(\overline{\mathbf{l}} \gamma^{\mu} \mathbf{l})$
$\mathscr{O}_{\Phi\widetilde{G}} = (\Phi^{\dagger}\Phi)\widetilde{G}^{\mathcal{A}}_{\mu\nu}G^{\mathcal{A}\mu\nu}$	$\mathscr{O}_{\mathbf{d}\mathbf{G}} = (\bar{\mathbf{q}}\sigma^{\mu\nu}\frac{\lambda^{\mathcal{A}}}{2}\Gamma_{\mathbf{d}}\mathbf{d}\Phi)\mathbf{G}^{\mathcal{A}}_{\mu\nu}$	$\mathscr{O}_{\Phi l}^{(3)} = (\Phi^{\dagger} i \overset{\leftrightarrow}{D}{}^{I}_{\mu} \Phi) (\bar{\mathfrak{l}} \gamma^{\mu} \tau^{I} \mathfrak{l})$
$\mathscr{O}_{\Phi W} = (\Phi^{\dagger} \Phi) W^{I}_{\mu \nu} W^{I \mu \nu}$	$\mathscr{O}_{eW} = (\bar{l}\sigma^{\mu\nu}\Gamma_e e\tau^I \Phi) W_{\mu\nu}^I$	$\mathscr{O}_{\Phi e} = (\Phi^{\dagger} i \overset{\leftrightarrow}{D}_{\mu} \Phi) (\bar{e} \gamma^{\mu} e)$
$\mathscr{O}_{\Phi \widetilde{W}} = (\Phi^{\dagger} \Phi) \widetilde{W}^{I}_{\mu \nu} W^{I \mu \nu}$	$\mathscr{O}_{uW} = (\bar{\mathfrak{q}} \sigma^{\mu\nu} \Gamma_u \mathfrak{u} \tau^I \widetilde{\Phi}) W_{\mu\nu}^I$	$\mathscr{O}_{\Phi q}^{(1)} = (\Phi^{\dagger} i \overset{\leftrightarrow}{D}_{\mu} \Phi) (\bar{q} \gamma^{\mu} q)$
$\mathscr{O}_{\Phi B} = (\Phi^\dagger \Phi) B_{\mu\nu} B^{\mu\nu}$	$\mathscr{O}_{dW} = (\bar{q}\sigma^{\mu\nu}\Gamma_{d}d\tau^{I}\Phi)W^{I}_{\mu\nu}$	$\mathscr{O}^{(3)}_{\Phi q} = (\Phi^\dagger \mathrm{i} \overset{\leftrightarrow}{D}{}^I_\mu \Phi) (\bar{q} \gamma^\mu \tau^I q)$
$\mathscr{O}_{\Phi \widetilde{B}} = (\Phi^\dagger \Phi) \widetilde{B}_{\mu \nu} B^{\mu \nu}$	$\mathscr{O}_{eB}=(\bar{\mathfrak{l}}\sigma^{\mu\nu}\Gamma_{e}e\Phi)B_{\mu\nu}$	$\mathscr{O}_{\Phi u} = (\Phi^{\dagger} i \overset{\leftrightarrow}{D}_{\mu} \Phi) (\bar{u} \gamma^{\mu} u)$
$\mathscr{O}_{\Phi WB} = (\Phi^{\dagger} \tau^{I} \Phi) W^{I}_{\mu \nu} B^{\mu \nu}$	$\mathscr{O}_{uB}=(\bar{\mathfrak{q}}\sigma^{\mu\nu}\Gamma_{u}u\widetilde{\Phi})B_{\mu\nu}$	$\mathscr{O}_{\Phi d} = (\Phi^{\dagger} i \overleftrightarrow{D}_{\mu} \Phi) (\bar{d} \gamma^{\mu} d)$
$\mathscr{O}_{\Phi \widetilde{\mathrm{W}}\mathrm{B}} = (\Phi^{\dagger} \tau^{I} \Phi) \widetilde{\mathrm{W}}_{\mu \nu}^{I} \mathrm{B}^{\mu \nu}$	$\mathscr{O}_{dB}=(\bar{q}\sigma^{\mu\nu}\Gamma_{d}d\Phi)B_{\mu\nu}$	$\mathscr{O}_{\Phi ud} = \mathrm{i}(\widetilde{\Phi}^{\dagger} \textit{D}_{\mu} \Phi) (\mathrm{\bar{u}} \gamma^{\mu} \Gamma_{ud} \mathrm{d})$

 $\psi^2 \Phi^3$

 $\mathscr{O}_{e\Phi} = (\Phi^{\dagger}\Phi)(\overline{1}\Gamma_{e}e\Phi)$

 $\mathscr{O}_{\mathbf{u}\Phi} = (\Phi^{\dagger}\Phi)(\bar{q}\,\Gamma_{\mathbf{u}}\mathbf{u}\widetilde{\Phi})$

 $\mathcal{O}_{d\Phi} = (\Phi^{\dagger}\Phi)(\bar{q}\Gamma_{d}d\Phi)$

Operators

 Φ^6

and $\Phi^4 D^2$

 $\mathscr{O}_{\Phi\square} = (\Phi^\dagger \Phi) \square (\Phi^\dagger \Phi)$

 $\mathscr{O}_{\Phi D} = (\Phi^\dagger D^\mu \Phi)^* (\Phi^\dagger D_\mu \Phi)$

 $\mathscr{O}_\Phi = (\Phi^\dagger \Phi)^3$

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 $\mathscr{O}_{G} = f^{ABC} G^{Av}_{\mu} G^{B\rho}_{\nu} G^{C\mu}_{\rho}$

$$\begin{split} \mathcal{O}_{\widetilde{G}} &= f^{ABC} \widetilde{G}_{\mu}^{\mu} \nabla_{V}^{B\rho} G_{\rho}^{C\mu} \\ \mathcal{O}_{W} &= \varepsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{F\mu} \\ \mathcal{O}_{\widetilde{W}} &= \varepsilon^{IJK} \widetilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu} \end{split}$$

EFT

IN A COMPLETE ANALYSIS ALL **59** INDEPENDENT OPERATORS OF grzadkowski:2010es), INCLUDING **25** FOUR-FERMION OPERATORS, HAVE TO BE CONSIDERED IN ADDITION TO THE SELECTED **34** OPERATORS

In **weakly interacting** theories the dimension-6 operators involving field strengths can only result from loops, while the others also result from tree diagrams (Arzt:1994gp). The operators involving dual field strengths tensors or complex Wilson coefficients violate CP.

PO EFT The parameters of the SM Lagrangian ແລະ ກ່ວວຍ ກະການ and ກົວ between their availing in the presence of itemsion-6 operators.

3285 10.4.2 Higgs vertices

3226 Here we list the most important Feynman rules for vertices involving exactly one physical Higgs bosor

3227 These are given in terms of the above-defined physical fields and parameters. In the coefficients of

dimension-6 couplings we replaced v^2 by the Fermi constant via $v^2 = 1/(\sqrt{2}G_F)$.

The triple vertices involving one Higgs boson read:

Hgg coupling:

$$H = \frac{G_{\mu}^{A}, p_{1}}{G_{\nu}^{B}, p_{2}} = i \frac{2g}{M_{W}} \frac{1}{\sqrt{2}G_{F}\Lambda^{2}} \left[\alpha_{GG}(p_{2\mu}p_{1\nu} - p_{1}p_{2}g_{\mu\nu}) + \alpha_{G\bar{G}}\varepsilon_{\mu\nu\rho\sigma}p_{1}^{\rho}p_{2}^{\sigma} \right] \delta^{AB},$$
(155)

HAA coupling:

$$\mathbf{H} = \mathbf{i} \frac{2g}{M_{\mathrm{W}}} \frac{1}{\sqrt{2}G_F \Lambda^2} \left[\alpha_{\mathrm{AA}} (p_{2\mu}p_{1\nu} - p_1 p_2 g_{\mu\nu}) + \alpha_{\mathrm{A}\tilde{\mathrm{A}}} \varepsilon_{\mu\nu\rho\sigma} p_1^{\rho} p_2^{\sigma} \right], \quad (156)$$



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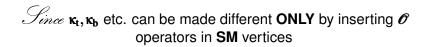
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Vademecum (NLO + EFT) trainee

- the EFT part has to be *implemented* into existing (EW + QCD) codes: formulation in arbitrary gauge (not U-gauge restricted) is needed
- Renormalization for the full SM + EFT Lagrangian is needed

Shone restricts the analysis to the calculation of **on-shell matrix** elements then additional operators are eliminated by the **Equations-Of-Motion** (EOM).

given a theory with a Lagrangian $\mathscr{L}[\phi]$ consider an effective Lagrangian $\mathscr{L}_{\text{eff}} = \mathscr{L} + g \mathscr{O} + g' \mathscr{O}''$ where

$$\mathscr{O} - \mathscr{O}'' \;\; = \;\; {\mathcal F}[\phi] \, \delta \mathscr{L} / \delta \phi$$

and **F** is some local functional of ϕ . The effect of \mathcal{O}' on $\mathscr{L}_{\text{eff}} = \mathscr{L} + g \mathcal{O}$ is

to shift g
ightarrow g + g' and to replace $\phi
ightarrow \phi + g' F$



Only **S**-matrix elements will be the same for equivalent operators but not the Green's functions ...

- since we are working with unstable particles,
- since we are inserting operators inside loops,
- since we want to use (off-shell) S, T and U parameters to constrain the Wilson coefficients,

↔ the use of EOM should be taken with extreme caution

T, L operators

The d = 6 operators are supposed to arise from a local Lagrangian, containing heavy degrees of freedom, ONCE THE LATTER ARE INTEGRATED OUT (the correspondence Lagrangians \rightarrow effective operators is not bijective) These operators are of two different origins:

- *T*-**operators** are those that arise from the tree-level exchange of some heavy degree of freedom
- *L***-operators** are those that arise from loops of heavy degrees of freedom

The *L*-operators are usually not included in the analysis.

See recent results in Einhorn:2013kja, Einhorn:2013tja

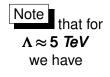
UV

Insertion of *d* = 6 operators in loops

We have to deal with

- renormalization of composite operators
- absorbing UV divergences to all orders and of maintaining the independence of arbitrary UV scale cutoff, problems that require the introduction of all possible terms allowed by the symmetries Georgi:1994qn,Kaplan:1995uv (EFT renormalization à la BPHZ?)
- Special care should be devoted in avoiding double-counting when we consider insertion of *T*-operators in loops and *L*-operators as well.





$$1/(\sqrt{2}G_{\rm F}\Lambda^2)\approx g^2/(4\pi)$$

i.e. [™] the contributions of *d* = 6 operators are [∞] loop effects.
 [™] [™] For higher scales, loop contributions tend to be more important (≽)

UV

UV Characteristic

- Operators normally alter the UV power-counting of a SM diagram
- but THERE ARE OPERATORS THAT DO NOT CHANGE THE UV POWER-COUNTING: we say that a set of SM diagrams is UV-scalable w.r.t. a combination of d = 6 operators if
 - their sum is UV finite
 - all diagrams in the set are scaled by the same combination of *d* = 6 operators.
- these diagrams are UV admissible

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Example: SM loops dressed only with UV-admissible operators

$$H \rightarrow \gamma \gamma$$

For $H \rightarrow \gamma \gamma$ the SM amplitude reads

$$\mathcal{M}_{\rm SM} = \mathcal{F}_{\rm SM} \left(\delta^{\mu\nu} + 2 \frac{\boldsymbol{\rho}_1^{\nu} \boldsymbol{\rho}_2^{\mu}}{\overline{\rm M}_{\rm H}^2} \right) \boldsymbol{e}_{\mu} \left(\boldsymbol{\rho}_1 \right) \boldsymbol{e}_{\nu} \left(\boldsymbol{\rho}_2 \right)$$

$$F_{_{\mathrm{SM}}} = -g \overline{\mathrm{M}} F_{_{\mathrm{SM}}}^{\mathrm{W}} - rac{1}{2} g rac{M_{\mathrm{t}}^2}{\overline{\mathrm{M}}} F_{_{\mathrm{SM}}}^{\mathrm{t}} - rac{1}{2} g rac{M_{\mathrm{b}}^2}{\overline{\mathrm{M}}} F_{_{\mathrm{SM}}}^{\mathrm{b}}.$$

$$\begin{split} F_{\rm SM}^{\rm W} &= 6 + \frac{\overline{\rm M}_{\rm H}^2}{\overline{\rm M}^2} + 6\left(\overline{\rm M}_{\rm H}^2 - 2\,\overline{\rm M}^2\right)\,C_0\left(-\overline{\rm M}_{\rm H}^2,0,0;\overline{\rm M},\overline{\rm M},\overline{\rm M}\right),\\ F_{\rm SM}^t &= -8 - 4\left(\overline{\rm M}_{\rm H}^2 - 4\,\textit{M}_t^2\right)\,C_0\left(-\overline{\rm M}_{\rm H}^2,0,0;\textit{M}_t,\textit{M}_t,\textit{M}_t\right), \end{split}$$

We only need a subset of operators \curvearrowright

$$\begin{split} \widetilde{\mathscr{S}} &= A_{\mathrm{V}}^{1} \left(\Phi^{\dagger} \Phi - v^{2} \right) F_{\mu\nu}^{a} F_{\mu\nu}^{a} + A_{\mathrm{V}}^{2} \left(\Phi^{\dagger} \Phi - v^{2} \right) F_{\mu\nu}^{0} F_{\mu\nu}^{0} \\ &+ A_{\mathrm{V}}^{3} \Phi^{\dagger} \tau_{a} \Phi F_{\mu\nu}^{a} F_{\mu\nu}^{0} + \frac{1}{2} A_{\partial\Phi} \partial_{\mu} \left(\Phi^{\dagger} \Phi \right) \partial_{\mu} \left(\Phi^{\dagger} \Phi \right) \\ &+ A_{\Phi}^{1} \left(\Phi^{\dagger} \Phi \right) \left(D_{\mu} \Phi \right)^{\dagger} D_{\mu} \Phi + A_{\Phi}^{3} \left(\Phi^{\dagger} D_{\mu} \Phi \right) \left[\left(D_{\mu} \Phi \right)^{\dagger} \Phi \right] \\ &+ \frac{1}{4\sqrt{2}} \frac{M_{\mathrm{t}}}{\overline{\mathrm{M}}} A_{\mathrm{f}}^{1} \left(\Phi^{\dagger} \Phi - v^{2} \right) \psi_{\mathrm{L}} \Phi t_{\mathrm{R}} \\ &+ \frac{1}{4\sqrt{2}} \frac{M_{\mathrm{b}}}{\overline{\mathrm{M}}} A_{\mathrm{f}}^{2} \left(\Phi^{\dagger} \Phi - v^{2} \right) \psi_{\mathrm{L}} \Phi^{c} b_{\mathrm{R}} + \mathrm{h. \ c.} \end{split}$$

$$A^0_\Phi=A^1_\Phi+2rac{A^3_\Phi}{\hat{s}^2_ heta}+4\,A_{\partial\Phi}.$$

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$$\begin{aligned} \mathcal{M}_{\mathrm{H}\to\gamma\gamma} &= \left(4\sqrt{2}\,G_{\mathrm{F}}\right)^{1/2} \left\{-\frac{\alpha}{\pi} \left[C_{\mathrm{W}}^{\gamma\gamma}\,F_{\mathrm{SM}}^{\mathrm{W}} + 3\sum_{\mathrm{q}}\,Q_{\mathrm{q}}^{2}\,C_{\mathrm{q}}^{\gamma\gamma}\,F_{\mathrm{SM}}^{\mathrm{q}}\right] + F_{\mathrm{AC}}\right\} \\ F_{\mathrm{AC}} &= \frac{g_{6}}{\sqrt{2}}\,\overline{\mathrm{M}}_{\mathrm{H}}^{2} \left(\hat{s}_{\theta}^{2}\,\mathcal{A}_{\mathrm{V}}^{1} + \hat{c}_{\theta}^{2}\,\mathcal{A}_{\mathrm{V}}^{2} + \hat{c}_{\theta}\,\hat{s}_{\theta}\,\mathcal{A}_{\mathrm{V}}^{3}\right). \end{aligned}$$

$$g_6 = \frac{1}{G_F \Lambda^2} = 0.085736 \left(\frac{TeV}{\Lambda}\right)^2$$

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${\ensuremath{\mathfrak{B}}}$ the scaling factors are given by

$$C_{\mathrm{W}}^{\gamma\gamma} = rac{1}{4} \overline{\mathrm{M}}^2 \Big\{ 1 + rac{g_6}{4\sqrt{2}} \Big[8 A_{\mathrm{V}}^3 \, \hat{c}_{ heta} \left(\hat{s}_{ heta} + rac{1}{\hat{s}_{ heta}}
ight) + A_{\Phi}^0 \Big] \Big\}$$

$$egin{array}{rcl} \mathcal{C}_{ ext{t}}^{\gamma\gamma} &=& rac{1}{8}\,\mathcal{M}_{ ext{t}}^2\left\{1+rac{g_6}{4\,\sqrt{2}}\left[8\,\mathcal{A}_{ ext{V}}^3\,\hat{c}_ heta\,\left(\hat{s}_ heta+rac{1}{\hat{s}_ heta}
ight)+\mathcal{A}_{\Phi}^0-\mathcal{A}_{ ext{f}}^1
ight]
ight\} \end{array}$$

$$egin{array}{rcl} \mathcal{C}_{\mathrm{b}}^{\gamma\gamma} &=& rac{1}{8}\,\mathcal{M}_{\mathrm{b}}^2\left\{1+rac{g_6}{4\,\sqrt{2}}\left[8\,\mathcal{A}_{\mathrm{V}}^3\,\hat{c}_{ heta}\,\left(\hat{s}_{ heta}+rac{1}{\hat{s}_{ heta}}
ight)+\mathcal{A}_{\Phi}^0-\mathcal{A}_{\mathrm{f}}^2
ight]
ight\}$$

The amplitude is the sum of

- the W,t and b SM components, each scaled by some combination of Wilson coefficients, and of
- a contact term

The latter is $\mathscr{O}(g_6)$ while the rest of the corrections is $\mathscr{O}(\frac{\alpha}{\pi}g_6)$. However, one should remember that

*O*ⁱ_V are operators of *L*-type, i.e. they arise from loop correction in the complete theory

 \therefore , the corresponding coefficients are expected to be very small although this is only an argument about naturalness without a specific quantitative counterpart (apart from a 1/(16 π^2) factor from loop integration)

Glimpsing at the headlines of the complete calculation for $H \rightarrow \gamma \gamma$

- SM loops, dressed with admissible operators
- New 33 loop-diagrams
- Counter-terms

Amplitude in *internal* notations

g HAA= -int(g)*Qs(-1,[g]^2+mt^2)*Qs(-1,[g+p1]^2+mt^2)*Qs(-1,[g+p1+p2]^2+mt^2)*3*trace*((-1/2*g*mt/M + L^-2 *(4*r2^-1*M^2*af1 - 2*M*aV1*mt - 1/2*a3K*M*g*mt + 2*adK*M*g*mt))* (-i *(ad(s,a)+ad(s,p1)+ad(s,p2))+mt)*VAtt(nu, p2)*(-i *(gd(s,q)+gd(s,p1))+mt)*VAtt(mu,p1)*(-i *qd(s,q)+mt)+ $(-1/2*q*mt/M + L^{2} * (4*r^{2}-1*M^{2}*af_{1} - 2*M*aV_{1}*mt - 1/2*a3K*M*q*mt + 2*adK*M*q*mt))*$ (i *ad(s.a)+mt)* VAtt(mu,p1)*(i *(qd(s,q)+qd(s,p1))+mt)* VAtt(nu, p2)*(i *(gd(s,q)+gd(s,p1)+gd(s,p2))+mt)) int(q)*Qs(-1,[q]^2+mb^2)*Qs(-1,[q+p1]^2+mb^2)*Qs(-1,[q+p1+p2]^2+mb^2)*trace*($(-1/2*q*mb/M + L^{-2} * (-4*r2^{-1}*M^{2}*af2 - 2*M*aV1*mb - 1/2*a3K*M*q*mb + 2*adK*M*q*mb))*$ $(-i \star (qd(s,q)+qd(s,p1)+qd(s,p2))+mb) \star$ VAbb(nu, p2)*(-i *(gd(s,q)+gd(s,p1))+mb)*VAbb(mu, p1) * (-i * qd(s, q) + mb) + $(-1/2*q*mb/M + L^{2} + (-4*r^{2} - 1*M^{2}*af^{2} - 2*M*aV1*mb - 1/2*a3K*M*q*mb + 2*adK*M*q*mb))*$ (i *ad(s.a)+mb)* VAbb(mu,p1)*(i *(gd(s,q)+gd(s,p1))+mb)* VAbb(nu,p2)*(i *(qd(s,q)+qd(s,p1)+qd(s,p2))+mb))+ + i *L^-2 *($+ 8*M*(sth^2*aV1 + cth^2*aV2 + sth*cth*aV3)*(p1(nu)*p2(mu) - d (mu,nu)*p1,p2))+$ $int(q) * Qs(-1,[q]^2+M^2) * Qs(-1,[q+p1]^2+M^2) * Qs(-1,[q+p1+p2]^2+M^2) * (Qs(-1,[q+p1+p2]^2+M^2)) * (Qs(-1,[q+p1+p2]^2)) * (Qs(-1,[q+p1+p2)) * (Qs(-1,[q+p1+p2))) * (Qs(-1,[q+p1+p2)))$

```
 \begin{array}{l} \mbox{dia30 +VAAWP(mu,nu,al,p1,p2) +VHPpWm(al,-p1-p2,-q)) + \\ \mbox{int}(q) + Qs(-1,[q]^2 + M0^2) + Qs(-1,[q+p1+p2]^2 + M0^2) + (\\ \mbox{dia31 +VHPOP0(-p1-p2,-q,q+p1+p2) + VAAPOP0(mu,nu,p1,p2)) + \\ \mbox{int}(q) + Qs(-1,[q]^2 + mh^2) + Qs(-1,[q+p1+p2]^2 + mh^2) + (\\ \mbox{dia32 +VHHH}(-p1-p2,q+p1,-q) + VAAHH(mu,nu,p1,p2)) + \\ \mbox{int}(q) + Qs(-1,[q]^2 + Mh^2) + (\mbox{dia33 +VHAAWW(mu,nu,si,si))); \\ \end{array}
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id VHPmPp(p1?,p2?,p3?)= - 1/2*M^-1*mh^2*g $+ L^{-2} * ($ $-2*M*mh^{2}*aV1 - 2*p2.p3*a1K*M*q + 1/2*(mh^{2} + 2*p1.p1)*a3K*M*q - 2*(mh^{2} + 2*p1.p1)*adK*M*q$ id VHPmWp(be?,p1?,p2?)= - 1/2*(p1(be) - p2(be))*i *a + L^-2 * (- 2*p2(be)*i *a1K*M^2*g - 2*(p1(be) - p2(be))*i *M^2*aV1 $- \frac{1}{2} (p1(be) - p2(be)) + i + a3K + M^{2} + 2 + (p1(be) - p2(be)) + i + adK + M^{2} + q);$ × id VHPpWm(be?,p1?,p2?)= $- 1/2 \cdot (p1(be) - p2(be)) \cdot i \cdot q$ + L^-2 * (- 2*p2(be)*i *a1K*M^2*g - 2*(p1(be) - p2(be))*i *M^2*aV1 $- \frac{1}{2}(p1(be) - p2(be)) * i * a3K * M^2 * q + 2 * (p1(be) - p2(be)) * i * adK * M^2 * q);$ × id VHWW(al?,be?,p2?,p3?)= - d (al,be)*M*g $+ L^{-2} * ($ $- 4 \star d (al, be) \star M^3 \star aV1 - d (al, be) \star a3K \star M^3 \star g + 2 \star d (al, be) \star a1K \star M^3 \star g$ + $4 \times d$ (al, be) $* adK \times M^3 \times q$ + $8 \times (p2(be) \times p3(al)) - d$ (al, be) $* p2.p3) \times M \times aV1$; + id VHZZ(al?.be?.p2?.p3?)= - d (al,be)*M*cth^-2*g $+ L^{-2} * ($ $-4 \star d$ (al, be) $\star M^3 \star aV1 \star cth^2 + d$ (al, be) $\star a3K \star M^3 \star cth^2 + 2 \star d$ + 2*d (al, be)*a1K*M^3*cth^-2*g + 4*d (al, be)*adK*M^3*cth^-2*g - 8*(p2(be)*p3(al) - d (al,be)*p2.p3)*M*aV3*cth*sth + 8*(p2(be)*p3(al) - d (al.be)*p2.p3)*M*aV2*sth^2 + $8 \cdot (p2(be) \cdot p3(al) - d(al, be) \cdot p2.p3) \cdot M \cdot aV1 \cdot cth^2);$

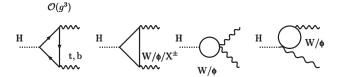
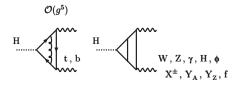


Figure 1: The three families of diagrams contributing to the amplitude for $H \rightarrow \gamma\gamma$; W/ ϕ denotes a W-line or a ϕ -line. X[±] denotes a FP-ghost line



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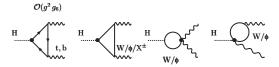


Figure 3: Example of one-loop SM diagrams with ${\cal O}\xspace$ -insertions, contributing to the amplitude for $H\to\gamma\gamma$

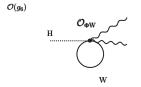
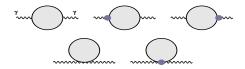


Figure 4: Example of one-loop O-diagrams, contributing to the amplitude for $H \rightarrow \gamma \gamma$

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 $_{Figure 5:}$ The photon self-energy with inclusion of $\mathcal{O}\text{-operators into SM}$ one-loop diagrams. The last diagram contains vertices, like AAHH, AA $\phi^0\phi^0$, that do not belong to the SM part.

Renormalization

$$g = g_{\text{ren}} \left[1 + \frac{g_{\text{ren}}^2}{16 \pi^2} \left(dZ_g + g_6 \, dZ_g^{(6)} \right) \frac{1}{\overline{\epsilon}} \right]$$

$$M_{\text{W}} = M_{\text{W}}^{\text{ren}} \left[1 + \frac{1}{2} \frac{g_{\text{ren}}^2}{16 \pi^2} \left(dZ_{M_{\text{W}}} + g_6 \, dZ_{M_{\text{W}}}^{(6)} \right) \frac{1}{\overline{\epsilon}} \right]$$

etc.

Wilson coefficients $\rightarrow W_i$

$$W_{i} = \sum_{j} Z_{ij}^{\text{wc}} W_{j}^{\text{ren}}$$

$$Z_{ij}^{\text{wc}} = \delta_{ij} + \left(g_{\text{ren}}^{2} dZ_{ij}^{\text{wc}} + dZ_{ij}^{\text{wc},6}\right) \frac{1}{\overline{\epsilon}}$$

EFT

Conclusions?



If you're looking for your lost keys, failing to find them in the kitchen is not evidence against their being somewhere else in the house

Conclusions?

 Higgs-landscape: asking the right questions takes as much skill as giving the right answers

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Thanks for your attention

Backup

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assumptions/inferences

- Given the (few) known coefficients in the perturbative expansion we estimate the next (few) coefficients and the corresponding partial sums by means of sequence transformations. This is the first step towards " reconstructing " the physical observable.
- The sequence transformations have been tested on a number of test sequences.
- A function can be uniquely determined by its asymptotic expansion if certain conditions are satisfied (Sokal).
- Borel procedure is a summation method which, under the above conditions, determines uniquely the sum of the series. It should be taken into account that there is a large class of series that have Borel sums (analytic in the cut-plane) and there is evidence that Levin-Weniger transforms produce approximations to these Borel sums. This is one of the arguments of plausibility supporting our results.
- The QCD scale variation uncertainty decreases when we include new (estimated) partial sums.
- All known and predicted coefficients are positive and all transforms predict convergence within a narrow interval.
- Missing a formal proof of uniqueness, we assume uninformative prior between the last known partial sum and the (largest) predicted partial sum.

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F. Wilczek hep-ph/9311302

typical strong interaction scale we'll be getting higher and higher powers of the strong interactions scale over Q^2 . Keeping the first few terms should be a good approximation even at 1.8 GeV. It is very helpful that the mass dimensions of the gauge invariant operators start at 4.

The Wilson coefficients, the operator product coefficients C above, obey renormalization group equations. They can be calculated in perturbation theory in the effective coupling at large Q^2 , of course. However, at Q^2 of approximately m_τ^2 we cannot simply ignore plausible non-perturbative corrections and still guarantee worthwhile accuracy. A term of the form $\Lambda_{QCD}^2(Q)^2$ would show up, through the mechanism of dimensional transmutation, as a contribution proportional to exp($-cr/\alpha_A$) in this coefficient, where c is a calculable numerical constant. It is an important question whether there is such a contribution, because if there were, and they were not under tight control, it is formally of such a magnitude as to ruin the useful precision of the predictions. Such a correction would be bigger than the ones coming from higher operators because these operators have dimension 4, so their coefficients have Q^2 over Λ^2 squared, which is a *priori* smaller.

Mucler [7] has given an important, although not entirely rigorous, argument that no Λ^2/Q^2 term can appear. The argument is a little technical, so I won't be able to do it full justice here but I will attempt to convey the main idea. The argument is based on the idea that at each successive power of 1 over Q^2 one can make the perturbation series in QCD, which is a badly divergent series in general, at least almost convergent, that is Borel summable, by removing a finite number of obstructions. Furthermore the obstructions are captured and parameterized by the low dimension operators mentioned before. Once these obstructions are removed, the remaining (processed) perturbation expression converges on the correct result for the full theory. Neither in the obstructions nor in the residual perturbative expression do the potentially dangerous terms occur – which means that they don't occur at all.

Maybe I should draw a picture of this [Figure 4]. One has the current product, and one is doing an analysis of its behavior when large virtual momentum is flowing through the current lines. The principle of the operator product expansion is to exhibit the powers of Q^2 by breaking the propagators in the graph into hard and soft parts. Any soft part costs you a power of one over Q^2 so you want the minimal number. If you just take out a couple of lines you have one of those low dimension operators, so those are interpreted as the operators, with the

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causality and unitarity. The usual demonstrations that these properties hold order by order in perturbation theory can be adapted to the re-processed version, which is more complicated but has the virtue of actually defining an answer. In fact we can agree that it gives the answer, since after all the whole point of quantum field theory is to give non-trivial realizations of the axioms, and that is what we have found.

QCD is not quite so favorable as this ideal, which occurs only for massive super-renormalizable theories in low dimensions. There are several known obstructions to Borel summability in QCD, which go by frightening names: ultraviolet and infrared renormalons, instantons, and threshold-induced oscillations. What Mueller did was to analyze these known sources of possible dangerous terms. He argued that the infrared renormalons are essentially just the higher-order terms in the operator product expansion, the ultraviolet renormalons generate singularities in $g(\alpha)$ away from the real axis whose influence on the truncated form of $g(\alpha)$ one actually computes can be minimized by judicious mappings in the α plane, that the threshold-induced oscillations are negligible quantitatively, and that the instanton contribution is both small and in principle calculable.

So now I have fleshed out my earlier description of Mueller's argument a bit. The key underlying assumption is that the known obstacles to Borel summability are the only ones. In principle, one can test this circle of ideas by calculating the operator product coefficients directly in the full theory (*i.e.* numerically, using lattice gauge theory techniques). If they were to fail, it would signify that there is an important gap in our understanding of quantum field theory.

On the experimental side, the Aleph group has tested the framework leading to this operator product expansion by comparing the resulting specific predictions for decay into semi-inclusive final states with specific quantum numbers, including the Q^2 dependence (which you can look at by looking at final states of different mass) [9]. They got a good fit with no one over Q^2 term and with matrix elements of the lowest dimension relevant operators $m\bar{\psi}\psi$, $trG_{\mu\nu}G_{\mu\nu}$ fitted to other experiments. These quantities also appear in other similar applications, where observed hadron parameters are correlated using the so-called QCD or ITEP sum rules, which arise by saturated various operator products. By taking suitable moments one can define quantities that are insensitive to the higher dimension operators, and for these the predictions of perturbative QCD are especially stringent.

I went into some detail into the analysis of tau decay because I think it's not

Structure of the calculation

- Process: $H \rightarrow \bar{f} f \gamma$, f = l, q, including b with non-zero m_t
- Setup: $m_{\rm f} = 0$ at NLO. Calculation based on helicity amplitudes

LO and NLO do not interfere (with $m_{\rm f} = 0$)

Cuts available in the H rest-frame Please complain but it took years to interface POWHEG and Prophecy4f $gg \rightarrow \bar{f}f\gamma$? Can be done, But

HTO-DALITZ Features

- Internal cross-check, loops are evaluated both analytically and numerically (using BST-algorithm)
- The code makes extensive use of *In-House* abbreviation algorithms (if *a* + *b* appears twice or more it receives an abbreviation and it is pre-computed only once).
- All functions are collinear-free
- High performances thanks to gcc-4.8.0
- Open MPI version under construction, GPU version in a preliminar phase
- Returns the full result and also the unphysical components

Man at work



 Extensions: as it was done during Lep times, there are diagrams where both the Z and the γ propagators should be Dyson-improved, i.e.

 $\alpha_{QED}(\textbf{0}) \rightarrow \alpha_{QED}(virtuality) \qquad \qquad \rho_{f} - \text{parameter included}$

However, the interested sub-sets are not gauge invariant,
 ∴ appropriate subtractions must be performed (at virtuality = 0, s_Z, the latter being the Z complex-pole).

Misunderstandings

- use *M*(ffγ) and require | *M* − *M*_Z |≤ *n*Γ_Z. *This is not the photon we are discussing* Photons are collinear to leptons only if emitted by leptons but those are Yukawa-suppressed.
 In any case *M*(ffγ) = *M*_H or it is *Not* Dalitz decay
- Requiring a cut on the opening angle between leptons and the photon to define *isolated photons* is highly recommended, *But* at the moment we are still in the Higgs rest-frame (*Miraeles take a bit lenger*)

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with the physical mass parameters

$$M_W^2 = \frac{1}{4}g^2v^2\left[1 + 2\frac{v^2}{\lambda^2}\alpha_{\Phi W}\right],$$

 $M_Z^2 = \frac{1}{4}(g^2 + g^2)v^2\left[1 + \frac{v^2}{2\lambda^2}(4\alpha_{ZZ} + \alpha_{\Phi D})\right],$
 $M_{11}^2 = \lambda v^2\left[1 + \frac{v^2}{2\lambda^2}\left(4\alpha_{\Phi \Box} - \frac{6}{\lambda}\alpha_{\Phi} - \alpha_{\Phi D}\right)\right],$
 $m_t = \frac{1}{\sqrt{2}}U^{\dagger}\Gamma_t U^{\tau_1}v\left[1 - \frac{1}{2}\frac{k^2}{\lambda^2}\alpha_{\tau_{\Phi}}\right].$ (151)

In (150) we have used the usual 't Hooft-Feynman gauge-fixing term

$$\mathcal{L}_{fix} = -C_{+}C_{-} - \frac{1}{2}(C_{Z})^{2} - \frac{1}{2}(C_{A})^{2} - \frac{1}{2}C_{G}^{A}C_{G}^{A}$$
(152)

with

$$C_G^A = \partial_\mu G^{A\mu}, \qquad C_A = \partial_\mu A^\mu, \qquad C_Z = \partial_\mu Z^\mu + M_Z \phi^0, \qquad C_{\pm} = \partial_\mu W^{\pm\mu} \pm i M_W \phi^{\pm}$$
 (153)

in terms of the physical fields and parameters, which gives rise to the same propagators as in the SM.

In the following, the abbreviations c_w and s_w are defined via the physical masses

$$c_w = \frac{M_W}{M_Z}, \quad s_w = \sqrt{1 - c_w^2}.$$
 (154)

The parameters of the SM Lagrangian g, g', λ , m^2 , and Γ_r keep their meaning in the presence of dimension-6 operators.

1288 10.4.2 Higgs vertices

²²⁸⁰ Here we list the most important Feynman rules for vertices involving exactly one physical Higgs boson. ²²⁸⁷ These are given in terms of the above-defined physical fields and parameters. In the coefficients of ²³⁸⁶ dimension-6 couplings we replaced u^2 by the Fermi constant via $u^2 = 1/(\sqrt{2}G_P)$.

The triple vertices involving one Higgs boson read:

Hgg coupling:

$$\mathbf{H} = \dots = \underbrace{\begin{array}{c} G_{\rho}^{A}, p_{1} \\ G_{\nu}^{B}, p_{2} \end{array}}_{G_{\nu}^{B}, p_{2}} = i \frac{2g}{M_{W}} \frac{1}{\sqrt{2G_{F}A^{2}}} \left[\alpha_{GG}(p_{2\mu}p_{1\nu} - p_{1}p_{2}g_{\mu\nu}) + \alpha_{GG}\varepsilon_{\mu\nu\rho\sigma}p_{1}^{\mu}p_{2}^{\sigma} \right] \delta^{AB},$$
(155)

HAA coupling:

$$\mathbf{H} = - \mathbf{I} \left\{ \begin{array}{c} \mathbf{A}_{\mu}, p_1 \\ \mathbf{A}_{\nu}, p_2 \\ \mathbf{A}_{\nu}, p_2 \end{array} \right\} = \mathbf{I} \frac{2g}{M_W} \frac{1}{\sqrt{2}G_F A^2} \left[\alpha_{AA} (p_{2\mu}p_{1\nu} - p_1p_2g_{\mu\nu}) + \alpha_{A\overline{A}}\varepsilon_{\mu\nu\rho\sigma} p_1^{\rho} p_2^{\sigma} \right], \quad (156)$$

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Hgg coupling:

$$\mathbf{H} = \dots = \underbrace{\begin{array}{c} G_{\rho}^{A}, p_{1} \\ G_{\nu}^{B}, p_{2} \end{array}}_{G_{\nu}^{B}, p_{2}} = i \frac{2g}{M_{W}} \frac{1}{\sqrt{2G_{F}A^{2}}} \left[\alpha_{GG}(p_{2\mu}p_{1\nu} - p_{1}p_{2}g_{\mu\nu}) + \alpha_{GG}\varepsilon_{\mu\nu\rho\sigma}p_{1}^{\mu}p_{2}^{\sigma} \right] \delta^{AB},$$
(155)

HAA coupling:

$$\mathbf{H} = - \mathbf{I} \left\{ \begin{array}{c} \mathbf{A}_{\mu}, p_1 \\ \mathbf{A}_{\nu}, p_2 \\ \mathbf{A}_{\nu}, p_2 \end{array} \right\} = \mathbf{I} \frac{2g}{M_W} \frac{1}{\sqrt{2}G_F A^2} \left[\alpha_{AA} (p_{2\mu}p_{1\nu} - p_1p_2g_{\mu\nu}) + \alpha_{A\overline{A}}\varepsilon_{\mu\nu\rho\sigma} p_1^{\rho} p_2^{\sigma} \right], \quad (156)$$

DRAFT

159

with the physical mass parameters

$$M_W^2 = \frac{1}{4}g^2v^2\left[1 + 2\frac{v^2}{\lambda^2}\alpha_{\Phi W}\right],$$

 $M_Z^2 = \frac{1}{4}(g^2 + g^2)v^2\left[1 + \frac{v^2}{2\lambda^2}(4\alpha_{ZZ} + \alpha_{\Phi D})\right],$
 $M_{11}^2 = \lambda v^2\left[1 + \frac{v^2}{2\lambda^2}\left(4\alpha_{\Phi \Box} - \frac{6}{\lambda}\alpha_{\Phi} - \alpha_{\Phi D}\right)\right],$
 $m_t = \frac{1}{\sqrt{2}}U^{\dagger}\Gamma_t U^{\tau_1}v\left[1 - \frac{1}{2}\frac{k^2}{\lambda^2}\alpha_{\tau_{\Phi}}\right].$ (151)

In (150) we have used the usual 't Hooft-Feynman gauge-fixing term

$$\mathcal{L}_{fix} = -C_{+}C_{-} - \frac{1}{2}(C_{Z})^{2} - \frac{1}{2}(C_{A})^{2} - \frac{1}{2}C_{G}^{A}C_{G}^{A}$$
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with

$$C_G^A = \partial_\mu G^{A\mu}, \qquad C_A = \partial_\mu A^\mu, \qquad C_Z = \partial_\mu Z^\mu + M_Z \phi^0, \qquad C_{\pm} = \partial_\mu W^{\pm\mu} \pm i M_W \phi^{\pm}$$
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160

HAZ coupling:

$$H = - i \frac{g}{M_W} \frac{1}{\sqrt{2}G_F \Lambda^2} \left[\alpha_{AZ}(p_{2\mu}p_{1\nu} - p_1p_2g_{\mu\nu}) + \alpha_{A\overline{Z}} \epsilon_{\mu\nu\rho\sigma} p_1^{\mu} p_2^{\sigma} \right], \quad (157)$$

HZZ coupling:

$$H = \left(\begin{array}{c} Z_{\mu}, p_1 \\ - ig \frac{M_2}{c_w} g_{\mu\nu} \left[1 + \frac{1}{\sqrt{2}G_F \Lambda^2} \left(\alpha_{\Phi \Psi} + \alpha_{\Phi \Box} + \frac{1}{4} \alpha_{\Phi D} \right) \right] \\ + \frac{2g}{M_W} \frac{2g}{\sqrt{2}G_F \Lambda^2} \left[\alpha_{ZZ} (p_{2\mu}p_{1\nu} - p_1p_{2\mu}) + \alpha_{ZZ} \varepsilon_{\mu\nu\rho\sigma} p_1^{\rho} p_2^{\sigma} \right], \quad (158)$$

HWW coupling:

$$H = - - \left[\frac{W_{\mu}^{2}, p_{1}}{\sqrt{2}G_{F}\Lambda^{2}} \left(\alpha_{\Phi W} + \alpha_{\Phi \Box} - \frac{1}{4}\alpha_{\Phi D} \right) \right] \\ + \left[\frac{2g}{M_{W}} \frac{1}{\sqrt{2}G_{F}\Lambda^{2}} \left(\alpha_{\Phi W} (p_{2\mu}p_{1\nu} - p_{1}p_{2\mu}) + \alpha_{\Phi \widetilde{W}} \varepsilon_{\mu\nu\rho\sigma} p_{1}^{\rho} p_{2}^{\sigma} \right) \right],$$
(189)

Hff coupling:

$$^{\text{H}} \cdots \cdots \left(\begin{array}{c} 1 \\ r_{c}, p_{1} \\ r_{c}, p_{2} \end{array} \right) = -i \frac{g}{2} \frac{m_{f}}{M_{W}} \left[1 + \frac{1}{\sqrt{2G_{F}A^{2}}} \left(\alpha_{\Phi W} + \alpha_{\Phi \Box} - \frac{1}{4} \alpha_{\Phi D} - \alpha_{f\phi} \right) \right], \quad (160)$$

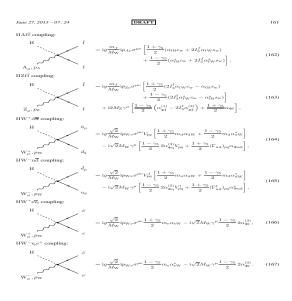
3289 where f = e, u, d.

The quadruple vertices involving one Higgs field, one gauge boson and a fermion–antifermion pair are given by $(q-u,d,f-u,d,v_l,e,$ and $\hat{f}-q$ for f-u,d and $\hat{f}-l$ for f-e):

Hgqq coupling:

$$\begin{array}{c} \mathbf{H} \\ & \overline{\mathbf{q}} \\ & \mathbf{q} \\ & \mathbf$$

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EFT

Decoupling and $SU(2)_C$

Heavy degrees of freedom → H → γγ: to be fully general one has to consider effects due to heavy fermions ∈ R_f and heavy scalars ∈ R_s of SU(3). Colored scalars disappear from the low energy physics as their mass increases. However, the same is not true for fermions.

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 Alternatively one could examine models containing
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