

## Track Based Alignment

- Define a Global Track $\chi^{2}$ function:
$x^{2}=\sum_{j=1}^{N_{\text {tacks }}} \sum_{i=1}^{n_{\text {nits }}} r_{i j}^{T}\left(p, q_{j}\right) V_{i j}^{-1} r_{i j}\left(p, q_{j}\right)$

$$
r_{i j}\left(p, q_{j}\right)=m_{i j}-f_{i j}\left(p, q_{j}\right)
$$

where:

- $\mathrm{V}_{\mathrm{ij}}=$ covariance matrix from fit
- $p=$ alignment parameters
(module position/orientation) - $q_{j}=$ track parameters
- $r_{i j}\left(p, q_{j}\right)=$ residual: difference between measured position $m_{i j}$ and position extrapolated from fit $f_{i j}\left(p, q_{j}\right)$ (depending on $p$ and $q_{j}$ )
- Aligment algorithms attempt to minimize this $\chi^{2}$ function and therefore track residuals



## Alignment with cosmic rays



## First complete alignment of the CMS Traker

 performed at the Cosmic Run at Four Tesla (CRAFT) A "global run": all CMS subdetectors participating to the data takingData taking 24/7 for 3 weeks (Oct 2008)
Major milestone demonstrating CMS capability of running over long periods
300 Million cosmic muon triggers collected @ 3.8 T Chance of performing alignment and calibration as an input to collision data taking

Alignment Strategy
Run a multi-step approach for both algorithms:
large structure movements (coherent valignment of Single Sided modules)
Alignment of the two sides of 2 D strip modules. (units): $u, w, \gamma$
module-level alignment of strip and pixel modules

The challenge is to determine at $\mathrm{O}(10 \mu \mathrm{~m})$ corrections for the 6 d.o.f (3 rotations + 3 translations) for each of the $>16 \mathrm{k}$ modules in CMS Silicon Tracker!

- A complex system of equations to be solved: 16.5 k modules $\times 6$ d.o.f. $\simeq 100 \mathrm{k}$ unknowns Fast and robust algorithms are deployed in the CMS framework.




## Minimization leads to the matrix equation

 $C a=b$ which has to be solved to extract $a$| Pros model module less CPU with one or |
| :--- | :--- | :--- | correlations Cons simple helix trajectory model

few iterations arge matrix may limit total N of alignables

## Implications for first collisions

- The all-silicon design of the tracking system of the CMS experiment is expected to provide $1-2 \%$ resolution for 100 GeV tracks and an efficient tagging of b -jets.


Get the best from both algorithm, combining the two:

1) run the global method $\rightarrow$ solves global 2) run the
2) run the local method $\rightarrow$ solves locally to match track model in all degrees of freedom All the three results are compatible but th
Combined shows the best performance

## Validation Methods

- Alignment recovers the average position
of modules along the sensitive coordinate: check the Distribution of Median of Residuals (DMR)


Monte Carlo Studies
B-tagging relies completely on tracking performance:


- There are systematic distortions which affect slightly the $\chi^{2}$ but bias significantly physics results
-As an example: twist distortion cannot be recovered
only with cosmic rays $\Rightarrow$ collisions needed!

