# Features of the particle acceleration in compact astrophysical objects 

V.S.Beskin

Lebedev Physical Institute, Moscow

# Features <br> of the $b$ particle acceleration in compact astrophysical objects 

V.S.Beskin

Lebedev Physical Institute, Moscow

# Features <br> of the bu particle acceleration in compact astrophysical objects 

V.S.Beskin

Lebedev Physical Institute, Moscow

# Features <br> of the bul particle acceleration in compact astrophysical objects 

V.S.Beskin

Lebedev Physical Institute, Moscow

# Features <br> of the bulk particle acceleration <br> in compact astrophysical objects 

V.S.Beskin

Lebedev Physical Institute, Moscow

## Fusion \& Astrophysics



## Fusion \& Astrophysics



## Fusion \& Astrophysics



What do we see

Active Galactic Nuclei (AGN)
$\mathrm{M} \sim\left(10^{6}-10^{9}\right) \mathrm{M}_{\odot}, \quad \mathrm{R} \sim\left(10^{10}-10^{13}\right) \mathrm{cm}$


Active Galactic Nuclei (AGN)

$$
\mathrm{M} \sim\left(10^{6}-10^{9}\right) \mathrm{M}_{\odot}, \quad \mathrm{R} \sim\left(10^{10}-10^{13}\right) \mathrm{cm}
$$



## Active Galactic Nuclei (model)



# Young Stellar Objects (YSO) $\mathrm{M} \sim 10 \mathrm{M}_{\odot}, \mathrm{R} \sim 10^{10} \mathrm{~cm}$ 



## Young Stellar Objects (YSO) $\mathrm{M} \sim 10 \mathrm{M}_{\odot}, \mathrm{R} \sim 10^{10} \mathrm{~cm}$



PRC95-24a - ST Scl OPO - June 6, 1995
C. Burrows (ST Scl), J. Hester (AZ State U.), J. Morse (ST Scl), NASA

## Young Stellar Objects (model)

## Diagram of HH 30 Circumstellar Disk \& Jet



## Microquasars ( $\mu \mathrm{QSO}$ ) $\mathrm{M} \sim(3-10) \mathrm{M}_{\odot}, \mathrm{R} \sim 10^{6} \mathrm{~cm}$



## Microquasars (model)



What do we think

## The same mechanism?



## The same mechanism?

## Thermal (gas pressure)?

Radiative (radiation pressure)?

Electromagnetic (Ampere force)?

## Main idea

Central engine is
an unipolar inductor

## Unipolar Inductor

- Electric circuit is to be touched to the sphere at different latitudes.
- Electric circuit is to rotate with the angular velocity $\Omega$ which differs from the angular velocity of a sphere.
- The energy source is the kinetic energy of the rotation.
- EMF does not result from the Faraday effect.


$$
W_{\mathrm{tot}}=I U
$$

## For the central engine to work

1.regular poloidal magnetic field, 2. rotation (inductive electric field $\boldsymbol{E}$, EMF $U$ ), 3. longitudinal current $I$ (toroidal magnetic field $B_{\varphi}$ ).

## An example - radio pulsars



## V.Beskin - N.Vlahakis, Email communication (2007)

>It's so nice your results are in agreement with our
> analytical calculations.

Yes, it is nice that the situation is pretty clear now.

## Two first steps only

- Force-free
- MHD
$\sigma$
- Two-fluid $\lambda$
- Radiation drag $l_{\mathrm{a}}$
- Reality


## Magnetization parameter $\sigma$

(maximum bulk Lorentz-factor)

$$
\begin{gathered}
\sigma=\frac{\Omega^{2} \Psi_{\mathrm{tot}}}{8 \pi^{2} c^{2} \mu \eta} \\
r_{\mathrm{F}}=R_{\mathrm{L}} \sigma^{1 / 3}
\end{gathered}
$$

Radio pulsars

$$
\begin{gathered}
10^{3}-10^{5} \\
? ? ? \\
10^{2}-10^{4} \\
10^{-3}-10^{-7}
\end{gathered}
$$

AGNs
GRBs
YSOs

## Multiplicity parameter $\lambda$

$$
\lambda=\frac{n^{(\mathrm{lab})}}{n_{\mathrm{GJ}}}
$$

$$
\rho_{\mathrm{GJ}}=-\frac{\boldsymbol{\Omega} \cdot \mathbf{B}}{2 \pi c}
$$

Radio pulsars

$$
\begin{aligned}
& 10^{3}-10^{5} \\
& ? ? ? \\
& 10^{13}-10^{14}
\end{aligned}
$$

AGNs
GRBs

What a problem?

## Specific features

Divergence of a flow
Relativistic motion
Rotation
Poynting dominated flow near the origin

## Specific features

Divergence of a flow (4-5 order of magnitude)

## Magnetized Wind

- Magnetization parameter

$$
\sigma=e \Omega \Psi_{\mathrm{tot}} / \lambda m c^{3} \gg 1
$$

( $\gamma=\sigma$ corresponds to full conversion)

- Position of the fast magnetosonic surface

$$
r_{\mathrm{F}}=R_{\mathrm{L}} \sigma^{1 / 3} \sin ^{-1 / 3} \theta
$$

- Disturbance of the poloidal magnetic field at $r=r_{\mathrm{F}}$

$$
\delta \Psi / \Psi=\sigma^{-2 / 3}
$$



Nonrelativistic
Relativistic

$$
r_{\mathrm{F}}=R_{\mathrm{L}} \sigma^{1 / 3} \sin ^{-1 / 3} \theta
$$


T.Sakurai.

A\&A, 152, 121
(1985)
N.Bucciantini, T.Thompson, J.Arons, E.Quataert, L.Del Zanna.

MNRAS, 368, 1717 (2006)

## Magnetized Wind (Acceleration)

For $r<r_{\mathrm{F}}$

$$
\gamma \sim x=\Omega r \sin \theta / c
$$

Fast Magnetosonic Surface

$$
\gamma\left(r_{\mathrm{F}}\right)=\sigma^{1 / 3} \sin ^{2 / 3} \theta(\text { not } \sigma)
$$

- For $r \gg r_{\mathrm{F}}$

$$
\Psi / \Psi_{0}=1-\cos \theta+\sigma^{-2 / 3} \ln ^{1 / 3}\left(r / r_{\mathrm{F}}\right)
$$

$$
\gamma \sim \sigma^{1 / 3} \ln ^{1 / 3}\left(r / r_{\mathrm{F}}\right)
$$



## Specific features

Divergence of a flow (4-5 order of magnitude)

## Specific features

Divergence of a flow (4-5 order of magnitude)
The flow is to be transonic

## $\underline{\text { Specific features }}$

Divergence of a flow (4-5 order of magnitude)
The flow is to be transonic

- Current $I$ is determined by the critical conditions, not by the outer load

NOT the 'magnetic tower'

## Energy Losses

$$
W_{\text {tot }}=I U
$$

$\left(I=I_{\mathrm{GJ}}\right.$ for relativistic flow)

$$
W_{\mathrm{tot}} \approx\left(\frac{\Omega R_{0}}{c}\right)^{2} B_{0}^{2} R_{0}^{2} c
$$

## Magnetic tower



Wind + diff. rotation

D.Lynden-Bell. MNRAS,

279, 389, (1996)
Y.Kato, M.R.Hayashi, R.Matsumoto. ApJ, 600, 338 (2004)

## And in the laboratory

PHYSICS OF PLASMAS 16, 041005 (2009)
Astrophysical jets: Observations, numerical simulations, and laboratory experiments
P. M. Bellan, ${ }^{1}$ M. Livio, ${ }^{2}$ Y. Kato, ${ }^{3}$ S. V. Lebedev, ${ }^{4}$ T. P. Ray, ${ }^{5}$ A. Ferrari, ${ }^{6}$ P. Hartigan, ${ }^{7}$ A. Frank, ${ }^{8}$ J. M. Foster, ${ }^{9}$ and P. Nicolai ${ }^{10}$


## The role of the divergence

M. M.Romanova,
G. V.Ustyugova,
A. V. Koldoba,
R. V. E. Lovelace. MNRAS, 399, 1802 (2009)


## Specific features

Relativistic motion

$$
\begin{gathered}
\sigma \sim \frac{1}{\lambda}\left(\frac{W_{\text {tot }}}{W_{\mathrm{A}}}\right)^{1 / 2} \\
W_{\mathrm{A}}=m_{\mathrm{e}}^{2} c^{5} / e^{2} \approx 10^{17} \mathrm{erg} \mathrm{~s}^{-1}
\end{gathered}
$$

## $\underline{\text { Specific features }}$

## Poynting dominated flow near the origin

## Far from the origin $E \sim B$

## Disturbance of the monopole magnetic field

V.S.Beskin \& R.R.Rafikov.

MNRAS, 313, 344, 2000

For electric current
$I=I_{\mathrm{GJ}}(1-h)$
an exact solution is
$\Psi=\Psi_{0}\left[1-\cos \theta+h(\Omega r / c)^{2} \sin ^{2} \theta \cos \theta\right]$
Light surface for $h<0$ at
$r \sin \theta=(2 h)^{-1 / 4} R_{\mathrm{L}}$



$$
\begin{array}{r}
-\frac{1}{\sin \theta} \frac{\partial}{\partial \theta}(\zeta \sin \theta)=2\left(\eta^{+}-\eta^{-}\right)-2\left[\left(\lambda-\frac{1}{2} \cos \theta\right) \xi_{r}^{+}-\left(\lambda+\frac{1}{2} \cos \theta\right) \xi_{r}^{-}\right] \\
2\left(\eta^{+}-\eta^{-}\right)+\frac{\partial}{\partial r}\left(r^{2} \frac{\partial \delta}{\partial r}\right)+\frac{1}{\sin \theta} \frac{\partial}{\partial \theta}\left(\sin \theta \frac{\partial \delta}{\partial \theta}\right)=0, \\
\frac{\partial \zeta}{\partial r}=\frac{2}{r}\left[\left(\lambda-\frac{1}{2} \cos \theta\right) \xi_{\theta}^{+}-\left(\lambda+\frac{1}{2} \cos \theta\right) \xi_{\theta}^{-}\right], \\
\frac{\varepsilon}{\sin \theta} \frac{\partial^{2} f}{\partial r^{2}}-\frac{\varepsilon}{r^{2}} \frac{\partial}{\partial \theta}\left(\frac{1}{\sin \theta} \frac{\partial f}{\partial \theta}\right)=2 \frac{\Omega}{r c}\left[\left(\lambda-\frac{1}{2} \cos \theta\right) \xi_{\varphi}^{+}-\left(\lambda+\frac{1}{2} \cos \theta\right) \xi_{\varphi}^{-}\right], \\
\frac{\partial}{\partial r}\left(\xi_{\theta}^{+} \gamma^{+}\right)+\frac{\xi_{\theta}^{+} \gamma^{+}}{r}=4 \lambda \sigma\left(-\frac{1}{r} \frac{\partial \delta}{\partial \theta}+\frac{\zeta}{r}-\frac{\sin \theta}{r} \xi_{r}^{+}+\frac{c}{\Omega r^{2}} \xi_{\varphi}^{+}\right), \\
\frac{\partial}{\partial r}\left(\xi_{\theta}^{-} \gamma^{-}\right)+\frac{\xi_{\theta}^{-} \gamma^{-}}{r}=-4 \lambda \sigma\left(-\frac{1}{r} \frac{\partial \delta}{\partial \theta}+\frac{\zeta}{r}-\frac{\sin \theta}{r} \xi_{r}^{-}+\frac{c}{\Omega r^{2}} \xi_{\varphi}^{-}\right), \\
\frac{\partial}{\partial r}\left(\gamma^{+}\right)=4 \lambda \sigma\left(-\frac{\partial \delta}{\partial r}-\frac{\sin \theta}{r} \xi_{\theta}^{+}\right), \\
\frac{\partial}{\partial r}\left(\gamma^{-}\right)=-4 \lambda \sigma\left(-\frac{\partial \delta}{\partial r}-\frac{\sin \theta}{r} \xi_{\theta}^{-}\right), \\
\frac{\partial}{\partial r}\left(\xi_{\varphi}^{+} \gamma^{+}\right)+\frac{\xi_{\varphi}^{+} \gamma^{+}}{r}=4 \lambda \sigma\left(-\varepsilon \frac{c}{\Omega r \sin \theta} \frac{\partial f}{\partial r}-\frac{c}{\Omega r^{2}} \xi_{\theta}^{+}\right), \\
\frac{\partial}{\partial r}\left(\xi_{\varphi}^{-} \gamma^{-}\right)+\frac{\xi_{\varphi}^{-} \gamma^{-}}{r}=-4 \lambda \sigma\left(-\varepsilon \frac{c}{\Omega r \sin \theta} \frac{\partial f}{\partial r}-\frac{c}{\Omega r^{2}} \xi_{\theta}^{-}\right)
\end{array}
$$



## Properties

- Current sheet $\delta \mathrm{r} \sim \mathrm{R}_{\mathrm{L}} / \lambda$
- Acceleration results from the motion perpendicular to magnetic field lines, $v_{\theta} \sim v_{r}$
- Particle energy $\gamma \sim \sigma$


## Comment for TeV Binaries



What was done

## Bulk particle acceleration

## Grad - Shafranov Approach

In general case 2D axisymmetric stationary structure of the flow is determined by the second order partial differential equation containing invariants as free functions.

# Full Version of the Grad - Shafranov Equation in the Kerr Metric 

$$
\begin{aligned}
& A\left[\frac{1}{\alpha} \nabla_{k}\left(\frac{1}{\alpha \varpi^{2}} \nabla^{k} \Psi\right)+\frac{1}{\alpha^{2} \varpi^{2}(\nabla \Psi)^{2}} \frac{\nabla^{i} \Psi \cdot \nabla^{k} \Psi \cdot \nabla_{i} \nabla_{k} \Psi}{D}\right] \\
& +\frac{1}{\alpha^{2} \varpi^{2}} \nabla_{k}^{\prime} A \cdot \nabla^{k} \Psi-\frac{A}{\alpha^{2} \varpi^{2}(\nabla \Psi)^{2}} \frac{1}{2 D} \nabla_{k}^{\prime} F \cdot \nabla^{k} \Psi \\
& \quad+\frac{\Omega_{\mathrm{F}}-\omega}{\alpha^{2}}(\nabla \Psi)^{2} \frac{\mathrm{~d} \Omega_{\mathrm{F}}}{\mathrm{~d} \Psi}+\frac{64 \pi^{4}}{\alpha^{2} \varpi^{2}} \frac{1}{2 \mathcal{M}^{2}} \frac{\partial}{\partial \Psi}\left(\frac{G}{A}\right) \\
& \quad-16 \pi^{3} \mu n \frac{1}{\eta} \frac{\mathrm{~d} \eta}{\mathrm{~d} \Psi}-16 \pi^{3} n T \frac{\mathrm{~d} s}{\mathrm{~d} \Psi}=0,
\end{aligned}
$$

## Algebraic Relations

$$
\begin{gathered}
\frac{I}{2 \pi}=\frac{\alpha^{2} L-\left(\Omega_{\mathrm{F}}-\omega\right) \varpi^{2}(E-\omega L)}{\alpha^{2}-\left(\Omega_{\mathrm{F}}-\omega\right)^{2} \varpi^{2}-\mathcal{M}^{2}} \\
\gamma=\frac{1}{\alpha \mu \eta} \frac{\alpha^{2}\left(E-\Omega_{\mathrm{F}} L\right)-\mathcal{M}^{2}(E-\omega L)}{\alpha^{2}-\left(\Omega_{\mathrm{F}}-\omega\right)^{2} \varpi^{2}-\mathcal{M}^{2}} \\
u_{\hat{\varphi}}=\frac{1}{\varpi \mu \eta} \frac{\left(E-\Omega_{\mathrm{F}} L\right)\left(\Omega_{\mathrm{F}}-\omega\right) \varpi^{2}-L \mathcal{M}^{2}}{\alpha^{2}-\left(\Omega_{\mathrm{F}}-\omega\right)^{2} \varpi^{2}-\mathcal{M}^{2}}
\end{gathered}
$$

## Algebraic Relations

$$
\begin{aligned}
\frac{I}{2 \pi} & =c \eta_{\mathrm{n}} \frac{L_{\mathrm{n}}-\Omega_{\mathrm{F}} \varpi^{2}}{1-\mathcal{M}^{2}} \\
v_{\varphi} & =\frac{1}{\varpi} \frac{\Omega_{\mathrm{F}} \varpi^{2}-L_{\mathrm{n}} \mathcal{M}^{2}}{1-\mathcal{M}^{2}}
\end{aligned}
$$

- Subsonic flow

$$
\mathrm{v}_{\varphi}=\Omega_{\mathrm{F}} r \sin \theta
$$

- Supersonic flow $\mathrm{v}_{\varphi}=L / r \sin \theta, \mathrm{v}_{\mathrm{p}} \sim \Omega_{\mathrm{F}} r_{\mathrm{F}}$


## The origin of an acceleration is a centrifugal force

Inside the critical surfaces the magnetic field plays a role of a sling, $\Omega=\Omega_{\mathrm{F}}$, so that

$$
\begin{aligned}
& \mathrm{v}_{\mathrm{p}}\left(r_{\mathrm{F}}\right)=\Omega_{\mathrm{F}} r_{\mathrm{F}} \sim\left(2 E_{\mathrm{n}}\right)^{1 / 2}=\mathrm{v}_{\mathrm{inf}} \\
& \mathrm{v}_{\mathrm{p}}\left(r_{\mathrm{F}}\right) \sim \mathrm{v}_{\mathrm{inf}}
\end{aligned}
$$

## Simple asymptotic solutions

## The role of the curvature

Grad-Shafranov equation is the force-balance one. For magnetically dominated case

$$
\rho_{\mathrm{e}} \boldsymbol{E}+\boldsymbol{j} \times \boldsymbol{B} / c \sim 0 .
$$

After some algebra

$$
\frac{S / c}{R_{c}}=\frac{1}{4 \pi} \nabla\left(B_{\varphi}^{2}-E^{2}\right)+\frac{1}{4 \pi} \nabla\left(B_{p}^{2}\right)
$$

If one can neglect the curvature $R_{\mathrm{c},}$, then $B^{2}-E^{2} \sim B^{2} / \gamma^{2}$ and $B^{2}{ }_{\varphi}=x^{2} B^{2}{ }_{\mathrm{p}}$, so we return to

$$
\gamma=x
$$

## The role of the curvature

$$
\frac{S / c}{R_{\mathrm{c}}}=\frac{1}{4 \pi} \nabla\left(B_{\varphi}^{2}-E^{2}\right)+\frac{1}{4 \pi} \nabla\left(B_{\mathrm{p}}^{2}\right)
$$

If one cannot neglect the curvature $R_{\mathrm{c}}$, then $S \sim(c / 4 \pi) B_{\varphi}{ }^{2}$, and one can neglect the last term (Beskin, Zakamska, Sol, MNRAS, 347, 587, 2004).

It gives

$$
\gamma=\left(R_{c} / \varpi\right)^{1 / 2}
$$

## Magnetized Wind

$$
\left(\sigma / \gamma_{\mathrm{in}}\right)^{1 / 2}
$$

- Magnetization parameter

$$
\sigma=e \Omega \Psi_{\text {tot }} / \lambda m c^{3} \gg 1
$$

( $\gamma=\sigma$ corresponds to full conversion)

- Position of the fast magnetosonic surface

$$
r_{\mathrm{F}}=R_{\mathrm{L}} \sigma^{1 / 3} \sin ^{-1 / 3} \theta
$$

- Disturbance of the poloidal magnetic field at $r=r_{\mathrm{F}}$

$$
\delta \Psi / \Psi=\sigma^{-2 / 3}
$$



## Magnetized Wind (Acceleration)

For $r<r_{\mathrm{F}}$

$$
\gamma \sim x=\Omega r \sin \theta / c
$$

- Fast Magnetosonic Surface

$$
\gamma\left(r_{\mathrm{F}}\right)=\sigma^{1 / 3} \sin ^{2 / 3} \theta(\text { not } \sigma)
$$

- For $r \gg r_{\mathrm{F}}$

$$
\Psi / \Psi_{0}=1-\cos \theta+\sigma^{-2 / 3} \ln ^{1 / 3}\left(r / r_{\mathrm{F}}\right)
$$

$$
\gamma \sim \sigma^{1 / 3} \ln ^{1 / 3}\left(r / r_{\mathrm{F}}\right)
$$



No collimation, no particle acceleration outside $r_{\mathrm{F}}$

# Numerical calculations (S.V.Bogovalov, A\&A, 371, 1155, 2001) 




## S.Komissarov, MNRAS, 350, 1431 (2004)



## Parabolic magnetic field

(V.S.Beskin \& E.E.Nokhrina, MNRAS. 367. 375. 2006)

- FMS position

$$
r_{\mathrm{F}}=R_{\mathrm{L}}(\sigma / \theta)^{1 / 2}
$$

- Lorentz-factor varies from $\gamma_{\mathrm{F}}=\gamma_{\mathrm{in}}$ at radial distance $x=\gamma_{\text {in }}$ to $\gamma_{\mathrm{F}}=\sigma^{1 / 3}$ at $x=\sigma^{1 / 3}$
- For $z>\sigma^{2 / 3} R_{\mathrm{L}}$ the flow becomes 1D (cylindrical)



## J.McKinney, MNRAS, 368,1561 (2006)




$$
\gamma(z)=\left(z / R_{L}\right)^{1 / 2}, u_{\varphi}=1
$$

# R. Narayan, J.McKinney, A.F.Farmer, MNRAS, 375, 548 (2006) 

Self-similar solution $z \sim \omega^{\alpha}$
For $\alpha>2$

$$
\gamma=x
$$

For $\alpha<2$
$\gamma=\left(R_{c} / \varpi\right)^{1 / 2}$


Central core

Central core $r_{\text {core }}=\gamma_{\text {in }} R_{\mathrm{L}}$

$$
B_{\min }=B\left(R_{\mathrm{L}}\right) / \sigma \gamma_{\text {in }}, \Psi_{\text {core }}=\left(\gamma_{\mathrm{in}} / \sigma\right) \Psi_{0}
$$




Yu.Lyubarsky,
ApJ. 698, 1570, 2009

V.S.Beskin, E.E.Nokhrina, MNRAS, 397, 1486, 2009

## Central core


S.Komissarov, M.Barkov,
N.Vlahakis, A.Königl,

MNRAS, 380, 51, 2007

O.Porth, Ch.Fendt, Z.Meliani,B.Vaidya. ApJ (in press) (2011)

## Conclusion

- Effective ( $\gamma=x$ ) acceleration takes place for strong collimation only (parabolic or stronger)
- Ineffective acceleration for weak collimation (parabolic or weaker)
- Effective particle acceleration takes place only if

$$
\varpi \sim \sigma R_{L}
$$

- Effective particle acceleration is possible only if the curvature plays no role
- External media is necessary

