



# New Developments in Cosmology

## Internal seminar



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March 16, 2016, Torino

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## Cosmology

- Cosmic Microwave Background (CMB)
- The  $\Lambda$ CDM model
- Tensions between local and CMB measurements

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## Light Sterile Neutrino

- Neutrino Oscillation Anomalies
- Parameterization in Cosmology
- Cosmological Effects of Relativistic Neutrinos
- Cosmological Effects of non-Relativistic Neutrinos
- Cosmological Constraints on the Light Sterile Neutrino

3

## Inflationary Freedom

- The Inflationary Paradigm
- Beyond Power-Law Primordial Power Spectrum
- Constraints on Light Sterile Neutrino Properties
- Constraints on the Primordial Power Spectrum

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## Coupled Dark Energy Scenario

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# Cosmic Microwave Background (CMB)

Predicted in 1948 (Alpher, Herman): blackbody background radiation at  $T \simeq 5$  K.

Discovery (accidental): Penzias, Wilson 1964 → Nobel prize 1978

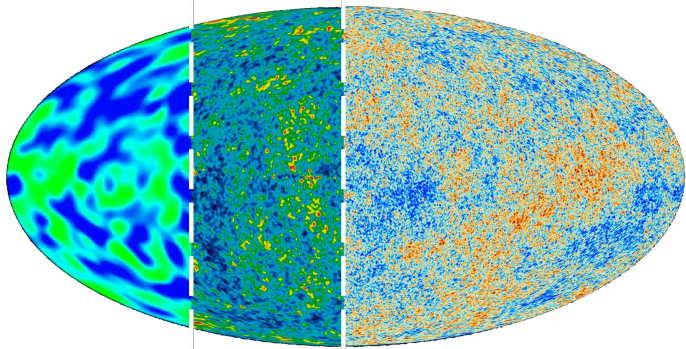
Observations: perfect black body spectrum at  $T_{\text{CMB}} = 2.72548 \pm 0.00057$  K

[Fixsen, 2009] → CMB is a remnant of the Big Bang.

Anisotropies at the level of  $10^{-5}$ : very high precision measurements are needed.

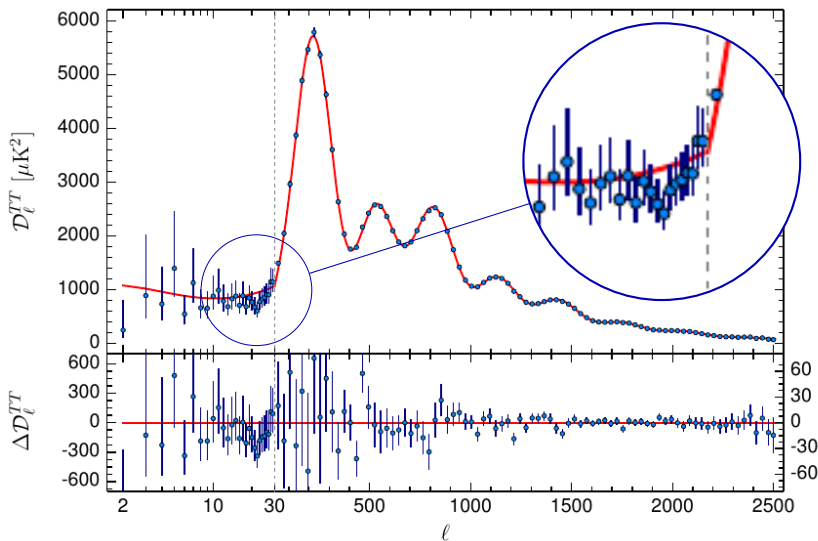
Improvement of the CMB experiments in 20 years:

COBE (1992)    WMAP (2003)    Planck (2013)



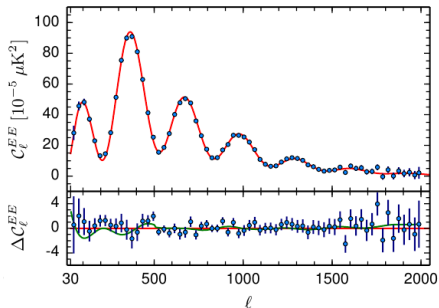
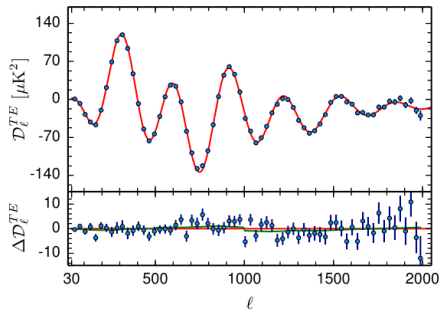
## Planck DR2 results - Temperature

Planck DR2 temperature auto-correlation power spectrum:



# Planck DR2 results - Polarization

- TE cross-correlation and EE auto-correlation measured with high precision;
- $\Lambda$ CDM explains very well the data;
- Note: in the plots, the red curve is the prediction based on the TT only best-fit for  $\Lambda$ CDM model  $\rightarrow$  very good consistency between temperature and polarization spectra.



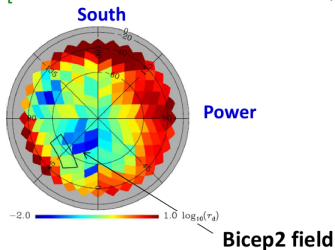
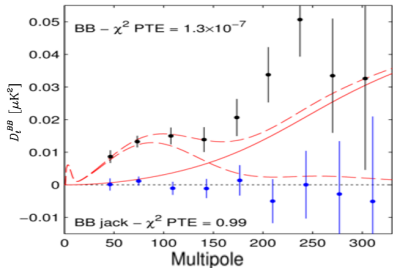
# Tensor modes: current status

[Planck Intermediate Results XXX, 2014]

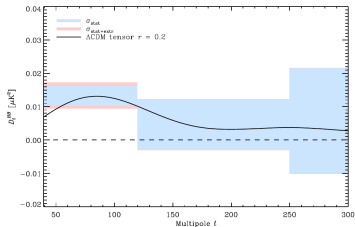
[BICEP2, 2014]: claim for detection of primordial tensor modes.

Non-zero value for tensor-to-scalar ratio  $r$ .

March 2014:  $r = A_t(k_*)/A_s(k_*) = 0.2^{+0.07}_{-0.05}$



Estimated dust emission:



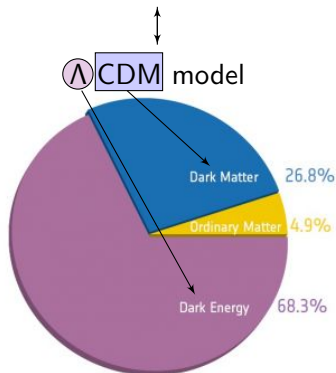
[BICEP2/Keck and Planck Collaborations, 2015]

Conclusions from the joint analysis:  $r_{0.05} < 0.12$  at 95% CL.

# Cosmological parameters

General Relativity + Homogeneity and isotropy

Cosmological evolution



[Planck collaboration, 2015]

$\Lambda$ CDM model described by 6 base parameters:

$\omega_b = \Omega_b h^2$  baryon density today;

$\omega_c = \Omega_c h^2$  CDM density today;

$\tau$  optical depth to reionization;

$\theta$  angular scale of acoustic peaks;

$n_s$  tilt and

$A_s$  amplitude of the power spectrum of initial curvature perturbations.

Other quantities can be derived:

$H_0$  Hubble parameter today;

$\sigma_8$  mean matter fluctuations at small scales;

...



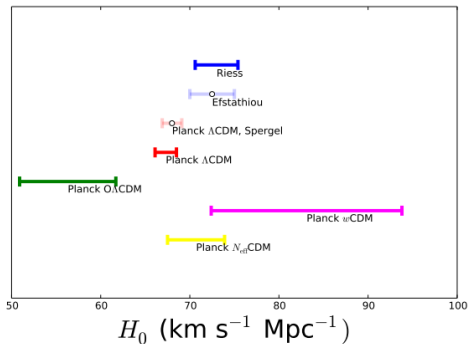
# Tension I: Hubble parameter

Hubble parameter today:  
 $v = H_0 d$ , with  $H_0 = H(z = 0)$

Local measurements:  $H(z = 0)$ ,  
local and independent on  
evolution (model independent,  
but systematics?)

CMB measurements  
(probe  $z \simeq 1100$ ):  
 $H_0$  from the cosmological  
evolution  
(model dependent, well  
controlled systematics)

[Cuesta et al., 2014] 68% CL error bars



(HST Cepheids)

[Riess et al., 2011] (SNe Ia calibrated distance):

$$H_0 = 73.8 \pm 2.4 \text{ Km s}^{-1} \text{ Mpc}^{-1}$$

[Efstathiou 2013] (NGC 4258 calibrated distance):

$$H_0 = 70.6 \pm 3.3 \text{ Km s}^{-1} \text{ Mpc}^{-1}$$

( $\Lambda$ CDM - CMB data only)

$$\text{[Planck 2013]: } H_0 = 67.3 \pm 1.2 \text{ Km s}^{-1} \text{ Mpc}^{-1}$$

$$\text{[Planck 2015]: } H_0 = 67.27 \pm 0.66 \text{ Km s}^{-1} \text{ Mpc}^{-1}$$

## Tension II: Cosmic Shear measurements

Cosmic shear: distortion of distant galaxy images by gravitational lensing of LSS  
⇒ sensitive to non-linear matter density along the line of sight/amplitude of matter power spectrum.

Assuming  $\Lambda$ CDM model:

$\sigma_8$ : rms fluctuation in total matter (baryons + CDM + neutrinos) in  $8h^{-1}$  Mpc spheres, today;  
 $\Omega_m$ : total matter density today divided by the critical density

CFHTLenS weak lensing data alone  
[Heymans et al., 2013] (68% CL):

$$\sigma_8(\Omega_m/0.27)^{0.46 \pm 0.02} = 0.774 \pm 0.04$$

CMB results

[Planck 2013] (68% CL):

$$\sigma_8(\Omega_m/0.27)^{0.46} = 0.89 \pm 0.03$$

2 $\sigma$  discrepancy!

Similar results from cluster counts:

Planck SZ Cluster Counts

[Planck 2013 Results XX] (68% CL):

$$\sigma_8(\Omega_m/0.27)^{0.3} = 0.764 \pm 0.025$$

Planck + WMAP pol + ACT/SPT

[Planck 2013] (68% CL):

$$\sigma_8(\Omega_m/0.27)^{0.3} = 0.87 \pm 0.02$$

3 $\sigma$  discrepancy!

Qualitatively similar results from *SPT* clusters, *Chandra Cluster Cosmology Project*.

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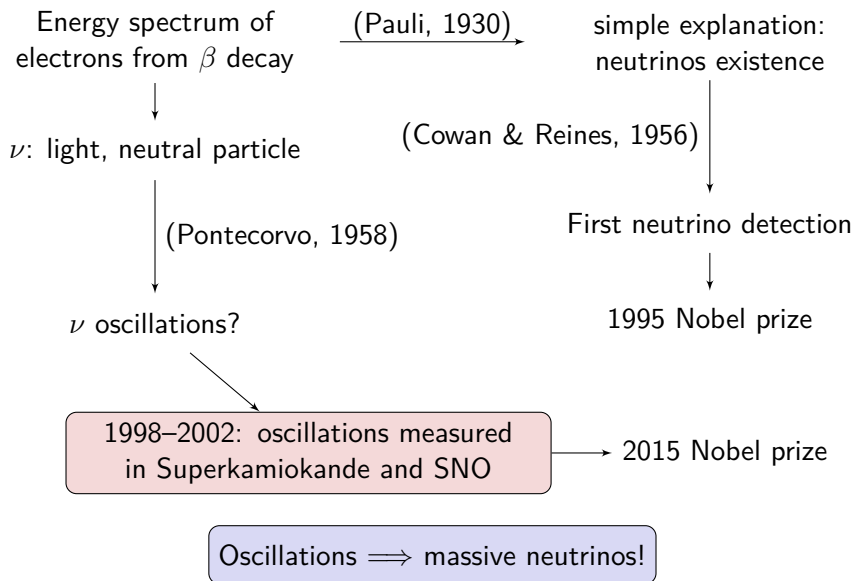
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# Brief Neutrino History



# Neutrino Oscillations

Analogous to CKM mixing for quarks: [Pontecorvo, 1958]  
[Maki, Nakagawa, Sakata, 1962]

$$\nu_\alpha = \sum_{k=1}^3 U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau)$$

$\nu_\alpha$  flavour eigenstates,  $U_{\alpha k}$  PMNS mixing matrix,  $\nu_k$  mass eigenstates.

Current knowledge of the 3 active  $\nu$  mixing: [PDG - Olive et al. (2015)]

$\Delta m_{ij}^2 = m_j^2 - m_i^2$ ,  $\theta_{ij}$  mixing angles

NO: Normal Ordering,  $m_1 < m_2 < m_3$

IO: Inverted Ordering,  $m_3 < m_1 < m_2$

$$\begin{aligned} \Delta m_{SOL}^2 &= (7.53 \pm 0.18) \cdot 10^{-5} \text{ eV}^2 &&= \Delta m_{21}^2 \\ \Delta m_{ATM}^2 &= (2.44 \pm 0.06) \cdot 10^{-3} \text{ eV}^2 \text{ (NO)} &&= |\Delta m_{32}^2| \simeq |\Delta m_{31}^2| \\ &= (2.49 \pm 0.06) \cdot 10^{-3} \text{ eV}^2 \text{ (IO)} \end{aligned}$$

$$\sin^2(2\theta_{12}) = 0.846 \pm 0.021$$

$$\sin^2(2\theta_{23}) = 0.999_{-0.018}^{+0.001} \text{ (NO)} - 1.000_{-0.017}^{+0.000} \text{ (IO)}$$

$$\sin^2(2\theta_{13}) = 0.085 \pm 0.005$$

CP violating phase  $\delta_{CP}$  still unknown. Hint:  $\delta_{CP} = -\pi/2$ ? [T2K Collaboration, 2015]

## Short Baseline (SBL) anomaly

Problem: **anomalies** in SBL experiments  $\Rightarrow$   $\left\{ \begin{array}{l} \text{errors in flux calculations?} \\ \text{deviations from } 3\nu \text{ description?} \end{array} \right.$

A short review:

**LSND** search for  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ , with  $L/E = 0.4 \div 1.5$  m/MeV. Observed a  $3.8\sigma$  excess of  $\bar{\nu}_e$  events [Aguilar et al., 2001]

**Reactor** re-evaluation of the expected anti-neutrino flux  $\Rightarrow$  excess of  $\bar{\nu}_e$  events compared to predictions ( $\sim 3\sigma$ ) with  $L < 100$  m [Azabajan et al, 2012]

**Gallium** calibration of GALLEX and SAGE Gallium solar neutrino experiments give a  $2.7\sigma$  anomaly (disappearance of  $\nu_e$ ) [Giunti, Laveder, 2011]

**MiniBooNE** (**inconclusive**) search for  $\nu_\mu \rightarrow \nu_e$  and  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ , with  $L/E = 0.2 \div 2.6$  m/MeV. No  $\nu_e$  excess detected, but  $\bar{\nu}_e$  excess observed at  $2.8\sigma$  [MiniBooNE Collaboration, 2013]

Possible explanation:

Additional squared mass difference

$$\Delta m_{\text{SBL}}^2 \simeq 1 \text{ eV}^2$$

## 3+1 Neutrino Model

$$\text{SBL anomalies} \Rightarrow \Delta m_{\text{SBL}}^2 \simeq 1 \text{ eV}^2$$



Existence of an additional neutrino degree of freedom,  
mass around 1 eV, no weak interaction  $\Rightarrow$  *light, sterile neutrino (LS $\nu$ )*



3 active ( $m_i \ll 1 \text{ eV}$ ) + 1 sterile ( $m_s \simeq 1 \text{ eV}$ )  $\nu$  scenario

We must update our mixing paradigm:

$$\nu_\alpha = \sum_{k=1}^{3+1} U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau, s)$$

$\nu_s$  is mainly  $\nu_4$ :

$$m_s \simeq m_4 \simeq \sqrt{\Delta m_{41}^2} \simeq \sqrt{\Delta m_{\text{SBL}}^2}$$

Active  $\nu$ :

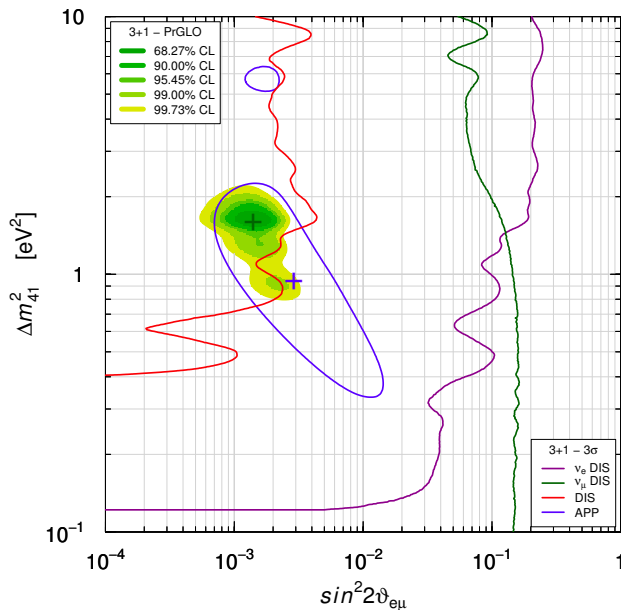
$$\sum m_{\nu, \text{active}} \simeq 0$$

Sterile  $\nu$ :

$$0.82 \leq m_s^2/\text{eV}^2 \leq 2.19 \quad (3\sigma)$$

[Giunti et al, 2013]

# Appearance–Disappearance Tension



SBL anomalies from

APPearance  
measurements

+

DISappearance  
measurements



APP–DIS tension?

DIS bound  
excludes part  
of the APP  
allowed region



# Relativistic Sterile Neutrino: Effective Number $N_{\text{eff}}$

Radiation energy density  $\rho_r$  in the early Universe:

$$\rho_r = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma = [1 + 0.2271 N_{\text{eff}}] \rho_\gamma$$

$\rho_\gamma$  photon energy density,  $7/8$  is for fermions,  $(4/11)^{4/3}$  due to photon reheating after neutrino decoupling

- $N_{\text{eff}} \rightarrow$  all the radiation contribution not given by photons
- $N_{\text{eff}} \simeq 1$  correspond to a single family of active neutrino, in equilibrium in the early Universe
- Active neutrinos:  $N_{\text{eff}} = 3.046$  [Mangano et al., 2005] due to not instantaneous decoupling for the neutrinos
- additional  $LS\nu$  contributes with  $\Delta N_{\text{eff}} = N_{\text{eff}} - 3.046$ :

$$\Delta N_{\text{eff}} = \frac{\rho_s^{\text{rel}}}{\rho_\nu} = \left[ \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 \right]^{-1} \frac{1}{\pi^2} \int dp p^3 f_s(p) \quad [\text{Acero et al., 2009}]$$

$\rho_\nu$  energy density for one active neutrino species,  $\rho_s^{\text{rel}}$  energy density of  $LS\nu$  when relativistic,

$p$  neutrino momentum,  $f_s(p)$  momentum distribution,  $T_\nu = (4/11)^{1/3} T_\gamma$

# Non-Relativistic Sterile Neutrino: Effective Mass $m_s^{\text{eff}}$

$m_s \simeq 1 \text{ eV} \rightarrow \nu_s$  is non-relativistic today ( $T_\nu \propto 10^{-4} \text{ eV}$ )

LS $\nu$  density parameter today:

$$\omega_s = \Omega_s h^2 = \frac{\rho_s}{\rho_c} h^2 = \frac{h^2 m_s}{\rho_c \pi^2} \int dp p^2 f_s(p) \quad [\text{Acero et al., 2009}]$$

$\rho_s$  energy density of non-relativistic LS $\nu$ ,  $\rho_c$  critical density and  $h$  reduced Hubble parameter

Alternatively:

$$m_s^{\text{eff}} = 94.1 \text{ eV } \omega_s \quad [\text{Planck 2013 Results, XVI}]$$

The factor (94.1 eV) is the same for the active neutrinos:

$$\omega_{\nu, \text{active}} = \sum_{\text{active}} m_\nu / (94.1 \text{ eV})$$

$$\text{If } f_s(p) = f_{\text{active}}(p), \quad m_s^{\text{eff}} \equiv m_s$$

## The momentum distribution function $f_s(p)$

$\Delta N_{\text{eff}}$ ,  $m_s^{\text{eff}}$  depend on the momentum distribution function  $f_s(p)$ .

LS $\nu$  relativistic at decoupling  $\Rightarrow f_s(p)$  independent of  $m_s$ .

Active neutrinos decoupled at  $T_\nu \simeq 1$  MeV. Is the same for LS $\nu$ ?

Oscillations + sterile  $\Rightarrow$  LS $\nu$  decouples not later than active neutrinos.

### Production mechanism?

Thermal production (TH):

temperature  $T_s = \alpha T_\nu$

$$f_s(p) = \frac{1}{e^{p/T_s} + 1}$$

$\Downarrow$

$$\Delta N_{\text{eff}} = \alpha^4$$

$$\omega_s = \alpha^3 m_s / (94.1 \text{ eV})$$

$\Downarrow$

$$m_s^{\text{eff}} = \alpha^3 m_s = \Delta N_{\text{eff}}^{3/4} m_s$$

Non-thermal production:

[Dodelson, Widrow 1993] (DW) model

$$f_s(p) = \frac{\beta}{e^{p/T_\nu} + 1}$$

$\Downarrow$

$$\Delta N_{\text{eff}} = \beta$$

$$\omega_s = \beta m_s / (94.1 \text{ eV})$$

$\Downarrow$

$$m_s^{\text{eff}} = \beta m_s = \Delta N_{\text{eff}} m_s$$

# Additional Radiation in the Early Universe

$$\rho_r = [1 + 0.2271 N_{\text{eff}}] \rho_\gamma$$

$$H^2 = 8\pi G \rho_T / 3$$

$N_{\text{eff}}$  controls the expansion rate  $H$  in the early Universe, during radiation dominated phase

influence on

Big Bang Nucleosynthesis:  
production of light nuclei

matter-radiation equality

expansion rate at  
CMB decoupling

CMB+BBN+ $^4\text{He}$ ,  $D$  abundances:

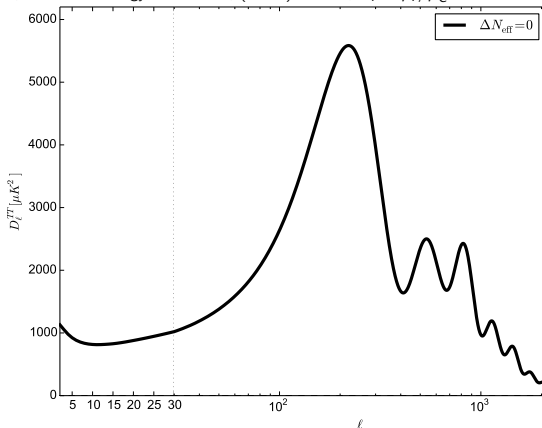
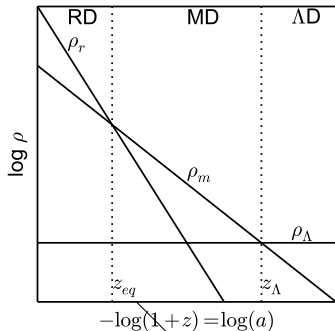
$\Delta N_{\text{eff}} \lesssim 0.2$  at 95% CL

[Cyburt et al., 2015]

# Additional Radiation: Effects on the CMB

## Starting configuration:

RD: Radiation Dominated, MD: Matter Dominated,  $\Lambda$ D: Dark Energy Dominated;  $(1+z) = a^{-1}$ ;  $\omega_i = \rho_i / \rho_C$

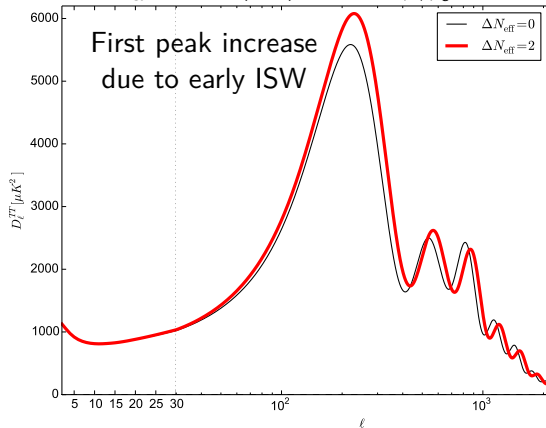
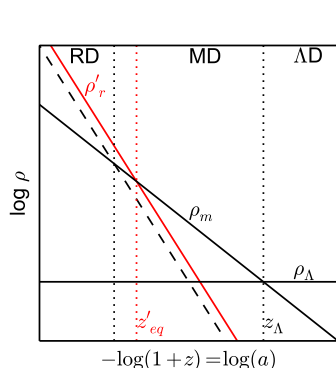


$$1 + z_{eq} = \frac{\omega_m}{\omega_r} = \frac{\omega_m}{\omega_\gamma} \frac{1}{1 + 0.2271 N_{eff}}$$

# Additional Radiation: Effects on the CMB

If we increase  $N_{\text{eff}}$ , all the other parameters fixed:

RD: Radiation Dominated, MD: Matter Dominated,  $\Lambda$ D: Dark Energy Dominated;  $(1+z) = a^{-1}$ ;  $\omega_i = \rho_i / \rho_C$

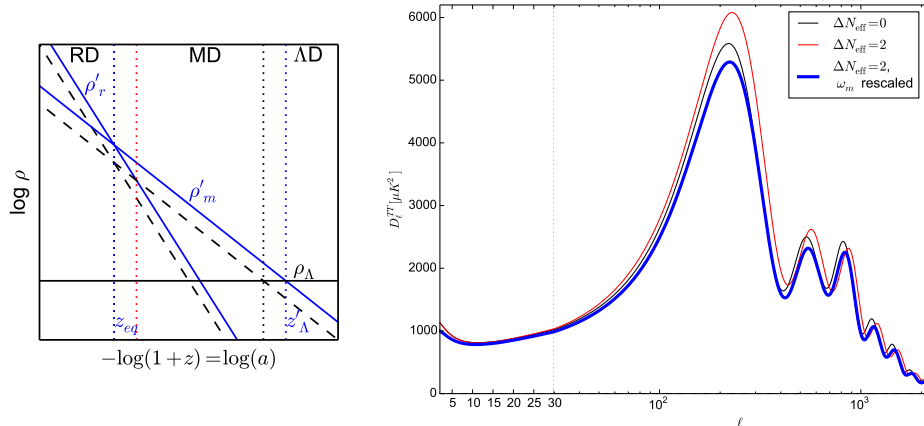


At  $z_{\text{CMB}}$ : higher  $H \propto \rho_r \Rightarrow$  smaller comoving sound horizon  $r_s \propto H^{-1}$   
 $\Rightarrow$  decrease of the angular scale of the acoustic peaks  $\theta_s = r_s / D_A$   
 $\Rightarrow$  shift of the peaks at higher  $\ell$

# Additional Radiation: Effects on the CMB

If we increase  $N_{\text{eff}}$ , plus  $\omega_m$  to fix  $z_{\text{eq}}$ :

RD: Radiation Dominated, MD: Matter Dominated,  $\Lambda$ D: Dark Energy Dominated;  $(1+z) = a^{-1}$ ;  $\omega_i = \rho_i / \rho_C$

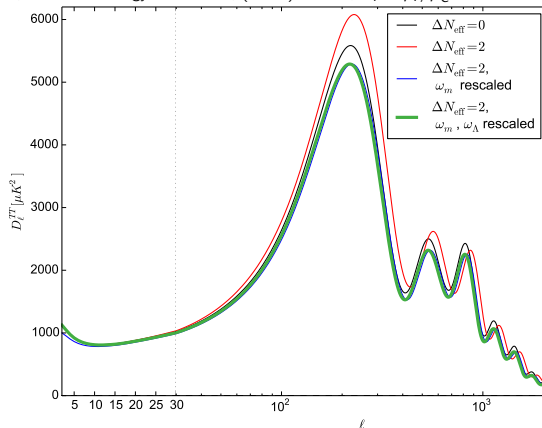
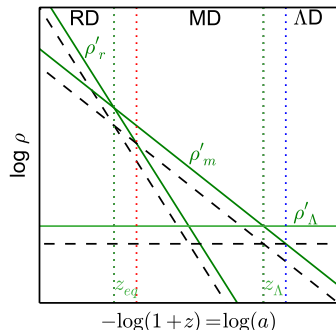


- Contribution from early ISW effect restored (first peak)
- different slope of the Sachs-Wolfe plateau, peak positions, envelope of high- $\ell$  peaks  $\Rightarrow$  due to later  $z_\Lambda$

# Additional Radiation: Effects on the CMB

If we increase  $N_{\text{eff}}$ , plus  $\omega_m, \omega_\Lambda$  to fix  $z_{\text{eq}}, z_\Lambda$ :

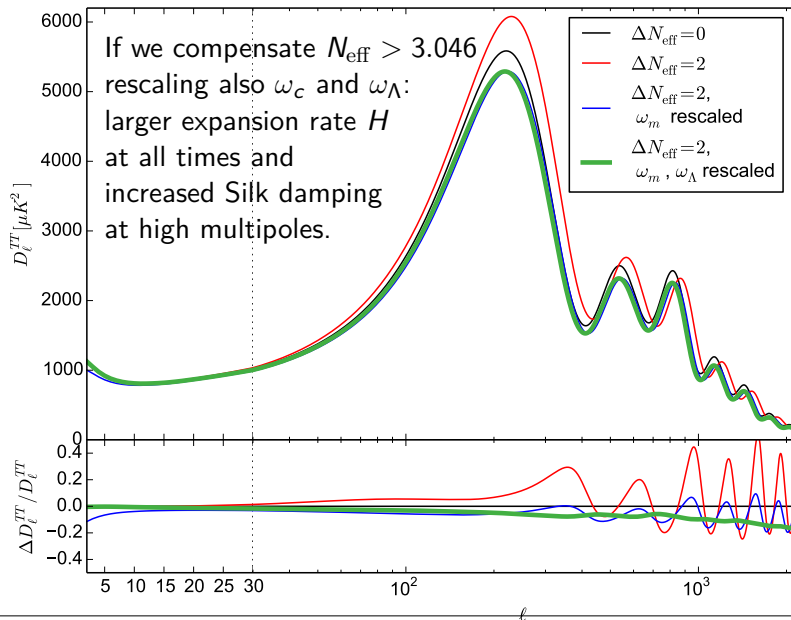
RD: Radiation Dominated, MD: Matter Dominated,  $\Lambda$ D: Dark Energy Dominated;  $(1+z) = a^{-1}$ ;  $\omega_i = \rho_i / \rho_C$



- peak positions recovered;
- slope of the Sachs-Wolfe plateau recovered;
- peak amplitude not recovered!



# Additional Radiation: Effects on the CMB



# Impact of additional non-relativistic neutrinos on the CMB

$\omega_m = \omega_b + \omega_c$  in the early Universe if  $LS\nu$  is relativistic



$1 + z_{\text{eq}} = (\omega_b + \omega_c)/\omega_r$   
independent of  $m_s$

$\omega_m^0 = \omega_b^0 + \omega_c^0 + \omega_\nu^0$  today

$LS\nu$  relativistic at recombination  
affects late time evolution only

Effects can be compensated with a variation in  $\Omega_\Lambda$

Degeneracies with spatial curvature are also possible

small effects on the SW plateau (cosmic variance!)

CMB is not the best direction

# Free-streaming - I

Massive neutrino



damping in the perturbations due to free-streaming length  $\lambda_{FS}$

Relativistic neutrinos

velocity  $v_s \simeq c$

$$\lambda_{FS}/a \propto (aH)^{-1} \propto t^{1/3} \text{ (MD)}$$

Non-relativistic neutrinos

$$\langle v_s \rangle = \frac{\int p^2 dp f(p) p/m_s}{\int p^2 dp f(p)} \propto \frac{\Delta N_{\text{eff}}}{\omega_s}$$

$$\lambda_{FS}/a \propto (a^2 H)^{-1} \propto t^{-1/3} \text{ (MD)}$$

$\Rightarrow$  Maximum  $\lambda_{FS}/a$  at the time of non-relativistic transition.



$$\text{Corresponds to } k_{\text{nr}} \simeq 0.0178 \Omega_m^{1/2} \left( \frac{T_\nu}{T_s} \right)^{1/2} \left( \frac{m_s}{1 \text{ eV}} \right)^{1/2} h \text{ Mpc}^{-1}$$

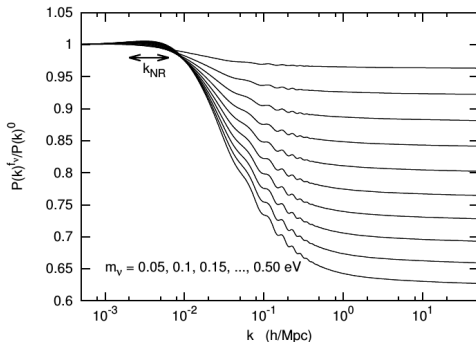
# Free-streaming - II

Damping occurs for all  $k \gtrsim k_{\text{nr}}$

[Neutrino Cosmology, Lesgourgues et al.]  
(fixed  $h, \omega_m, \omega_b, \omega_\Lambda$ )

Plot:  $\frac{P_{m_\nu > 0}(k)}{P_{m_\nu = 0}(k)}$

- top to bottom:  $m_\nu = 0.05$  eV to  $m_\nu = 0.5$  eV
- $\Delta P/P \simeq -7(8)(m_\nu/1 \text{ eV})$



Expected constraints from future surveys:

- Planck CMB + DES:  $\sigma(m_\nu) \simeq 0.04\text{--}0.06$  eV [Font-Ribera et al., 2014]
- Planck CMB + Euclid:  $\sigma(m_\nu) \simeq 0.03$  eV [Audren et al., 2013]

# CMB and SBL joint constraints

CMB:

(no SBL)

+SBL (DW)

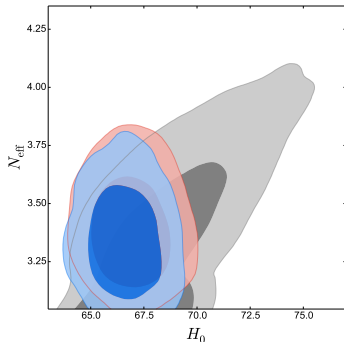
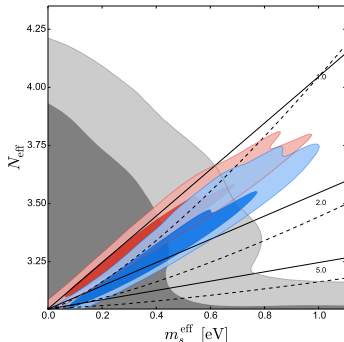
+SBL (TH)

solid lines: (DW)

$$m_s^{\text{eff}} = m_s \Delta N_{\text{eff}}$$

dashed lines: (TH)

$$m_s^{\text{eff}} = m_s (\Delta N_{\text{eff}})^{3/4}$$



- $\nu_s$  as Warm Dark Matter (WDM):  $N_{\text{eff}} \simeq 3.046$ , large  $m_s^{\text{eff}}$  (large  $m_s$ );
- SBL prior:  $m_s \simeq 1.2$  eV, but
 

$N_{\text{eff}} \simeq 4$  ( $\nu_s$  thermalized as  $\nu_{\text{SM}}$ ) disfavoured;
- (DW), (TH) models give similar results ( $N_{\text{eff}}$  slightly higher in (DW)).

Solving  $\sigma_8$  Tension with the sterile neutrinoCMB+ $H_0$ +BAO+LSS:

(no SBL)

+SBL (DW)

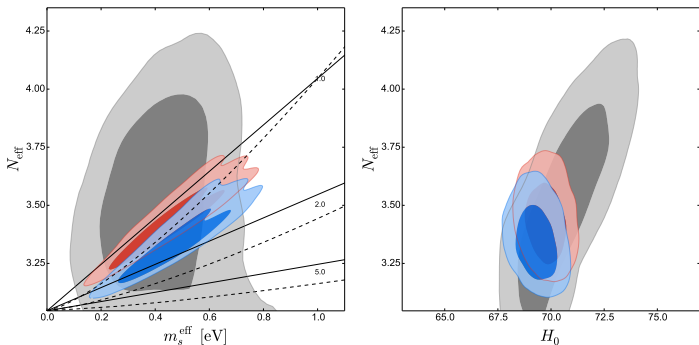
+SBL (TH)

solid lines: (DW)

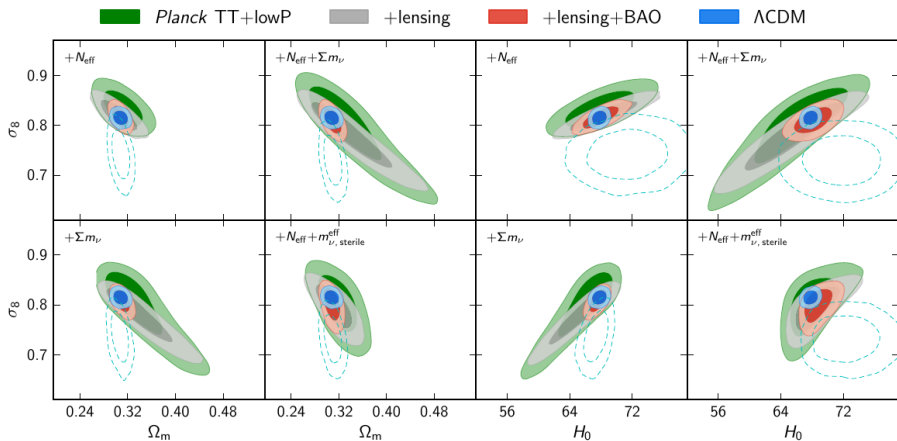
$$m_s^{\text{eff}} = m_s \Delta N_{\text{eff}}$$

dashed lines: (TH)

$$m_s^{\text{eff}} = m_s (\Delta N_{\text{eff}})^{3/4}$$



- LSS results give preference towards non-zero  $m_s^{\text{eff}} \rightarrow$  non-zero  $m_s$ : smaller  $\sigma_8$  from LSS can be addressed with massive  $\nu_s$  (due to free streaming);
- no SBL prior:  $N_{\text{eff}}$  constraints almost unchanged;
- with SBL prior: preference for  $N_{\text{eff}} > 3.046$  at more than  $2\sigma$ ;
- with SBL prior:  $N_{\text{eff}} \simeq 4$  still hardly disfavoured

Solving both  $\sigma_8$  and  $H_0$  Tension?

$H_0$  increases  $\Rightarrow \sigma_8$  increases (and viceversa)!

The correlations do not help.

# Incomplete Thermalization

Many probes constrain  $\Delta N_{\text{eff}} < 1$ . Do we need

- a mechanism to suppress oscillations and full thermalization of  $\nu_s$ ?
- to compensate  $\Delta N_{\text{eff}} = 1$  with additional mechanisms in Cosmology?

Some ideas:

- large lepton asymmetry [Foot et al., 1995; Mirizzi et al., 2012; many more]
- new neutrino interactions [Bento et al., 2001; Dasgupta et al., 2014; Hannestad et al., 2014; Saviano et al., 2014; many more]
- entropy production after neutrino decoupling [Ho et al., 2013]
- very low reheating temperature [Gelmini et al., 2004; Smirnov et al., 2006]
- time varying dark energy components [Giusarma et al., 2012]
- larger expansion rate at the time of  $\nu_s$  production [Rehagen et al., 2014]



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## 3 Inflationary Freedom

- The Inflationary Paradigm
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- Constraints on Light Sterile Neutrino Properties
- Constraints on the Primordial Power Spectrum

## 4 Coupled Dark Energy Scenario

# Primordial Power Spectrum from Inflation

Slow roll inflation [Linde, 1982]:

inflation occurred by a scalar field (Inflaton) rolling down a potential energy hill.

End of inflation depends on

- the shape of the inflaton potential  $V(\phi)$ ;
- the spatially varying perturbation of the inflaton field  $\delta\phi(t, \vec{x})$ .

Fluctuations in the inflaton modulate the end of inflation:  
in different regions, inflation ends at different times.

$\delta\phi(t, \vec{x})$  converted into energy density fluctuations  $\delta\rho$  after inflation.

⇒ small scale dependence of the Primordial Power Spectrum (PPS) of scalar perturbations:

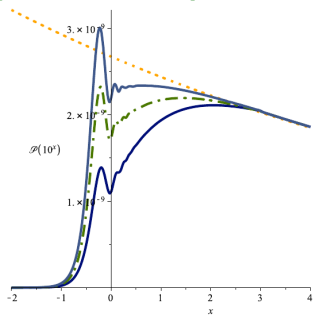
$$(n_s - 1) \equiv \frac{d \ln P_s(k)}{d \ln k} = 2 \frac{V''}{V} - 3 \left( \frac{V'}{V} \right)^2,$$

more general than  $P_s(k) = A_s(k/k_*)^{n_s-1}$ .

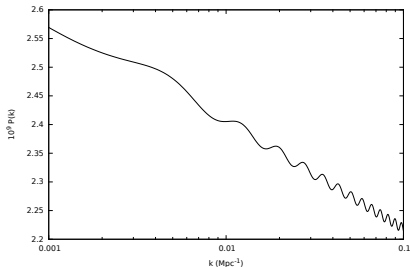
Is  $n_s$  constant?  
Can the PPS deviate from a Power-Law (PL)?

# Beyond Power-Law PPS: Theory

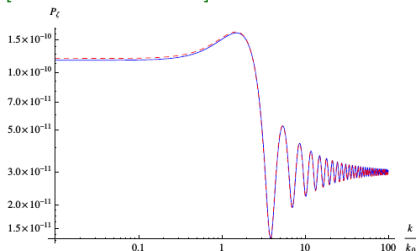
[Sagnotti et al, 2014]



[Mukhanov, 2013]



[Romano et al., 2014]

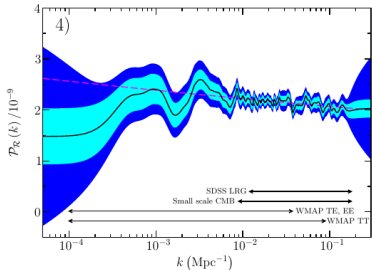


Given an inflationary model one gets one Primordial Power Spectrum (PPS), more or less complicated

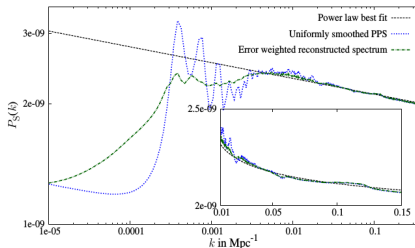
Much more models were developed: see e.g. [[“Encyclopædia Inflationaris”](#), Martin et al., 2014]

# Beyond Power-Law PPS: Reconstructions

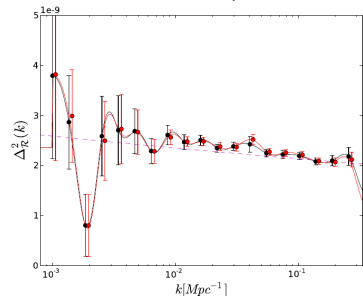
[Hunt et al., 2014] (WMAP data)



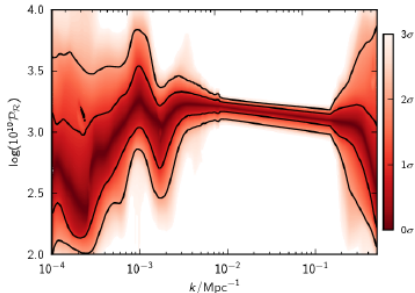
[Hazra et al, 2014] (Planck 2013 data)



[de Putter et al, 2014] (Planck 2013)



[Planck Collaboration, 2015]



# PCHIP Parametrization

Fix the Primordial Power Spectrum (PPS) form leads to possible bias:

⇒ analysis with free, non-parametric form for the PPS.

*Proposal:* fix a series of nodes  $k_1, \dots, k_{12}$  and use an interpolating function among them,

$$P_s(k) = P_0 \times f(k; P_{s,1}, \dots, P_{s,12}) \quad \text{with } P_0 = 2.2 \times 10^{-9}, P_{s,j} = P_s(k_j)$$

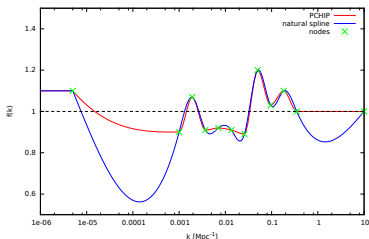
In our case we use:

PCHIP [Fritsch et al., 1980]

“piecewise cubic Hermite interpolating polynomial”

$$f(k; P_{s,1}, \dots, P_{s,12}) = \text{PCHIP}(k; P_{s,1}, \dots, P_{s,12})$$

Advantage over *natural cubic splines*:  
no spurious oscillations.



Interpolate piecewise a series of nodes  $P_{s,j} = P_s(k_j)$  with  $j \in [1, 12]$ :

- continue and derivable;
- preserve monotonicity of the nodes:
  - ▶ 1<sup>st</sup> derivative in the node fixed using the secants between consequent nodes;
  - ▶ if the monotonicity changes, the node is a local extremum;
- 2<sup>nd</sup> derivative not continue in the nodes.

# Light Sterile Neutrino Results - I

Standard: Power-Law (PL)

$\Lambda$ CDM(PL PPS) +  $\nu_s$  model

$$P_s(k) = A_s(k/k_{\text{pivot}})^{n_s-1}$$

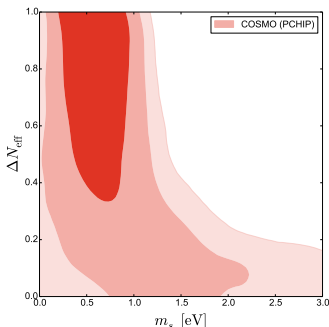
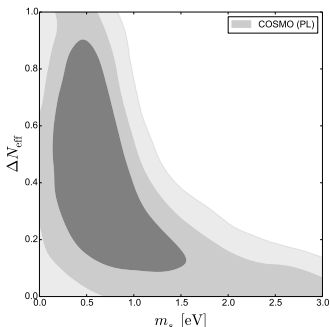
PPS

free form: nodes  $P_{s,1}, \dots, P_{s,12}$ ,  
interpolate with PCHIP function

$\Lambda$ CDM(PCHIP PPS) +  $\nu_s$  model

$$P_s(k) = P_0 \times f(k; P_{s,1}, \dots, P_{s,12})$$

Results for the **Thermal sterile neutrino**, mass  $m_s$ , no SBL prior on  $m_s$ :



- higher  $\Delta N_{\text{eff}}$  admitted;
- change on  $m_s$  constraints due to  $\Delta N_{\text{eff}}$  change;
- fully thermalized sterile neutrino preferred.

COSMO = CMB(Planck13+WMAP Polarization+ACT/SPT)+LSS(WiggleZ)+HST(Riess2011)+CFHTLenS+PlanckSZ

## Light Sterile Neutrino Results - II

Standard: Power-Law (PL)

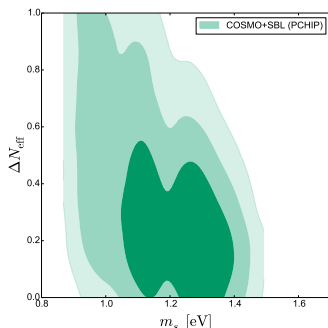
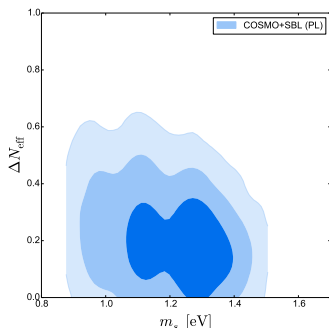
 $\Lambda$ CDM(PL PPS) +  $\nu_s$  model

$$P_s(k) = A_s(k/k_{\text{pivot}})^{n_s-1}$$

PPS

free form: nodes  $P_{s,1}, \dots, P_{s,12}$ ,  
interpolate with PCHIP function $\Lambda$ CDM(PCHIP PPS) +  $\nu_s$  model

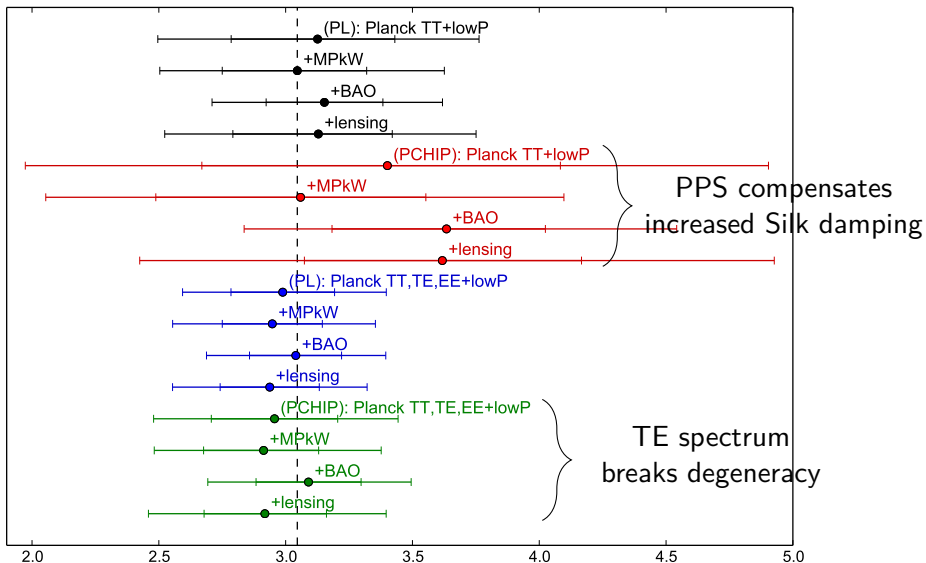
$$P_s(k) = P_0 \times f(k; P_{s,1}, \dots, P_{s,12})$$

Results for the Thermal sterile neutrino, mass  $m_s$ , with SBL prior on  $m_s$ :

- higher  $\Delta N_{\text{eff}}$  admitted;
- no change on  $m_s$  constraints;
- fully thermalized sterile neutrino admitted (inside  $2\sigma$  region).

COSMO = CMB(Planck13+WMAP Polarization+ACT/SPT)+LSS(WiggleZ)+HST(Riess2011)+CFHTLenS+PlanckSZ

# Degeneracy between PPS and Radiation Content



Planck 2015 CMB data

MPkW: matter power spectrum (WiggleZ) – BAO: BOSS DR11 + SDSS MGS + 6dF – lensing: Planck 2015 trispectrum

S. Gariazzo

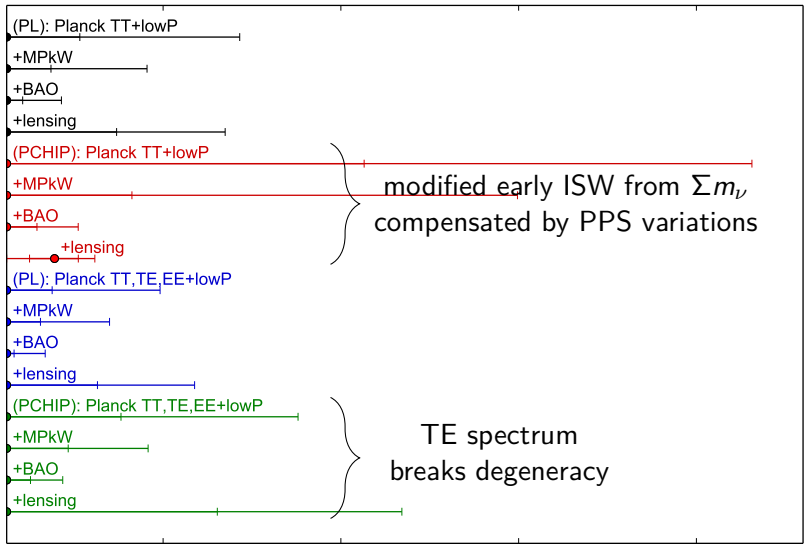
"New Developments in Cosmology"

Internal Seminar, Torino, 16/03/2016

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# Degeneracy between PPS and Neutrino Masses

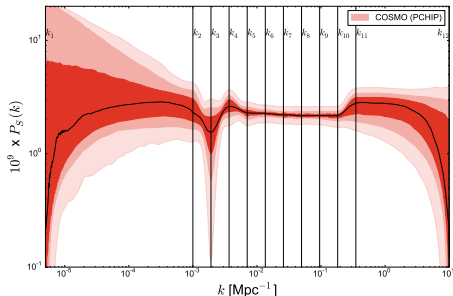


Planck 2015 CMB data  
 MPkW: matter power spectrum (WiggleZ) - BAO: BOSS DR11 + SDSS MGS + 6dF - lensing: Planck 2015 trispectrum  
 S. Gariazzo "New Developments in Cosmology" Internal Seminar, Torino, 16/03/2016

# PPS Results

$\Lambda$ CDM(PCHIP PPS) +  $\nu_s$

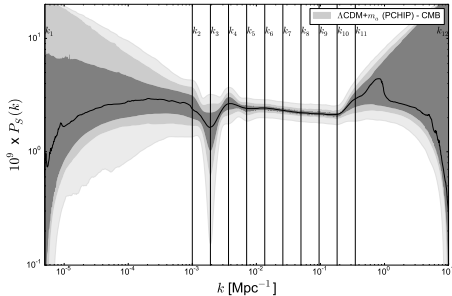
CMB(Planck13+WMAP Polarization+ACT/SPT)+  
LSS(WiggleZ)+HST(Riess2011)+CFHTLenS+PlanckSZ



[SG et al., JCAP 1504 (2015) 023]

$\Lambda$ CDM(PCHIP PPS) +  $m_a$

CMB(Planck13+WMAP Polarization+ACT/SPT)



[Di Valentino et al., PRD 91 (2015) 123505]

Different cosmological models, similar results:

- CMB constraints for  $1 \times 10^{-4} \text{ Mpc}^{-1} (\ell = 2) \leq k \leq 0.3 \text{ Mpc}^{-1} (\ell \simeq 2500)$ ;
- power-law is a good approximation in the range  $7 \times 10^{-3} \text{ Mpc}^{-1} \leq k \leq 0.2 \text{ Mpc}^{-1}$ ;
- feature at  $k = 2 \times 10^{-3} \text{ Mpc}^{-1}$  correspond to dip  $\ell \simeq 22$  in CMB spectrum;
- feature at  $k = 3.5 \times 10^{-3} \text{ Mpc}^{-1}$  correspond to small bump  $\ell \simeq 40$ .

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## 4 Coupled Dark Energy Scenario

## Model - I

DE-DM nature  
as particles?non-gravitational  
interactions?not with  
ordinary  
matter!

new DM-DE coupling?

stress-energy tensor conservation:

$$\begin{aligned}\nabla_{\mu} T_{\text{DM}}^{\mu\nu} &= Q u_{\text{DM}}^{\nu}/a \\ \nabla_{\mu} T_{\text{DE}}^{\mu\nu} &= -Q u_{\text{DM}}^{\nu}/a\end{aligned}$$

energy conservation:

$$\begin{aligned}\dot{\rho}_{\text{DM}} + 3\mathcal{H}\rho_{\text{DM}} &= +Q \\ \dot{\rho}_{\Lambda} + 3\mathcal{H}(1 + w_{\Lambda})\rho_{\Lambda} &= -Q\end{aligned}$$

Coupling parametrized through  $Q$ Our choice:  $Q = \xi\mathcal{H}\rho_{\Lambda}$ 
 $\xi < 0, w_{\Lambda} > -1$   
**MOD1: DM decays into DE**

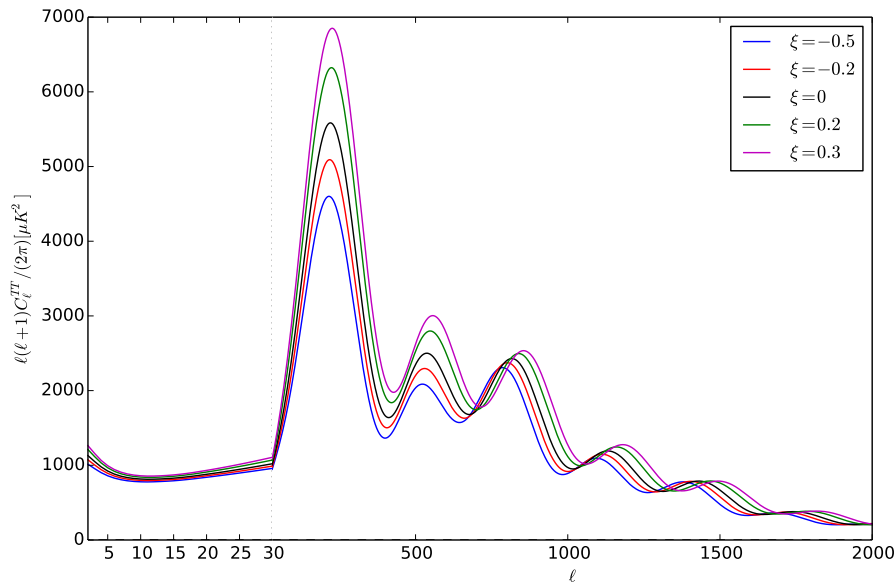
or

 $\xi > 0, w_{\Lambda} < -1$   
**MOD2: DE decays into DM**

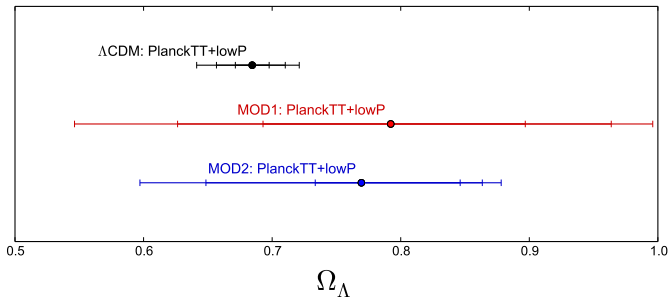
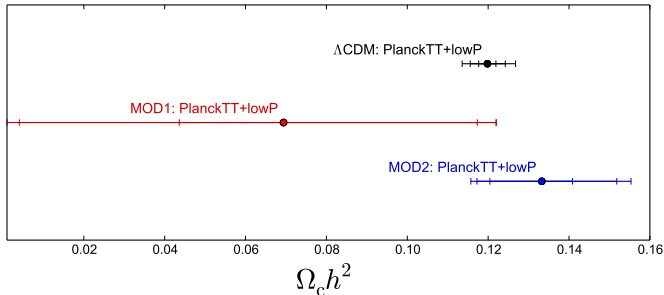
$\xi$  dimensionless coupling parameter – a scale factor –  $\mathcal{H}$  Hubble parameter  
 $\rho_{\text{DM}} (\rho_{\Lambda})$  DM (DE) energy density –  $u_{\text{DM}}^{\nu}$  DM four-velocity –  $w_{\Lambda}$  DE equation of state parameter ( $\rho_{\Lambda} = w_{\Lambda}\rho_{\Lambda}$ )

## Model - II

Coupled Dark Energy (CDE) influences the CMB spectrum:



## Results - I



$h = H_0 / (100 \text{ Km s}^{-1} \text{ Mpc}^{-1})$  dimensionless Hubble parameter

- $\Omega_c h^2 \propto \rho_{\text{DM}}$   
is physical

- MOD1

DM  $\rightarrow$  DE



less DM today

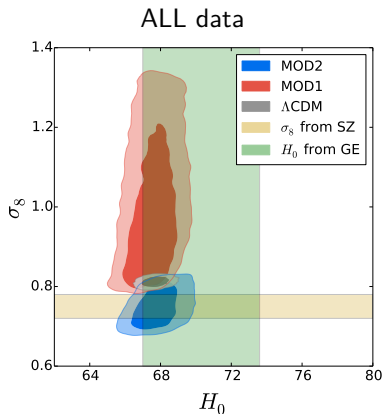
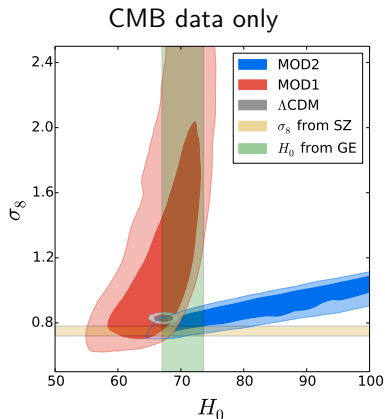
- MOD2

DE  $\rightarrow$  DM



more DM today  
also higher  $h!$

$\Omega_\Lambda \propto \rho_\Lambda / h^2$  is  
non-physical,  
depends on  $h!$

Results - II -  $H_0$  and  $\sigma_8$  tensions

more DM in the early Universe  $\implies$  stronger nonlinear evolution in **MOD1**

$H^2 \propto \rho_\Lambda \propto a^{-3(w_\Lambda+1)-\xi} \implies$  higher  $H_0$  in **MOD2**

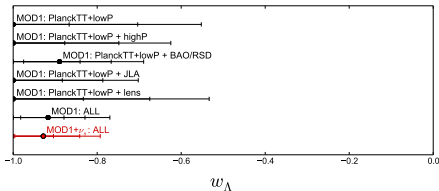
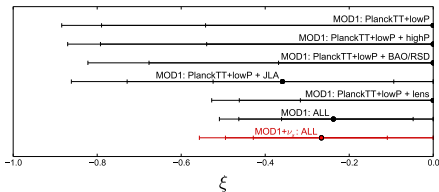
**MOD2** is better for reconciling CMB and local determinations

CMB=Planck TT+low- $\ell$  polarization

ALL=CMB + high- $\ell$  polarization + BAO/RSD (BOSS DR11, SDSS MGS, 6dF) + Supernovae (JLA) + Planck lensing trispectrum

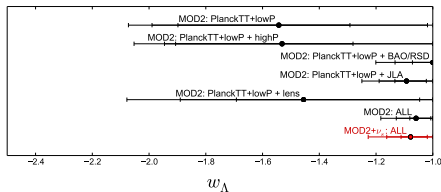
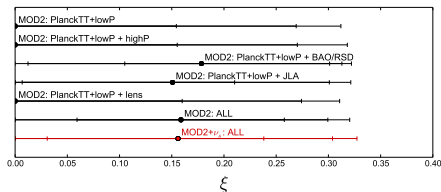
Results - III -  $\xi$  and  $w_\Lambda$ 

## MOD1



- JLA  $\rightarrow \xi \neq 0?$
- BAO/RSD  $\rightarrow w_\Lambda \neq -1?$

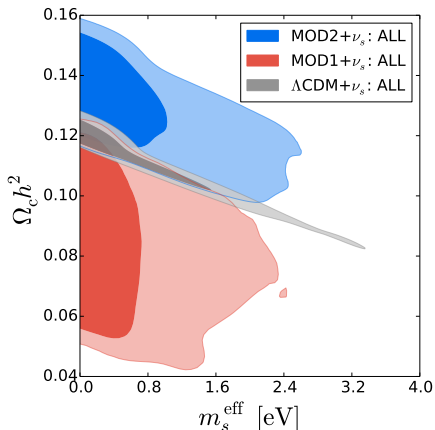
## MOD2



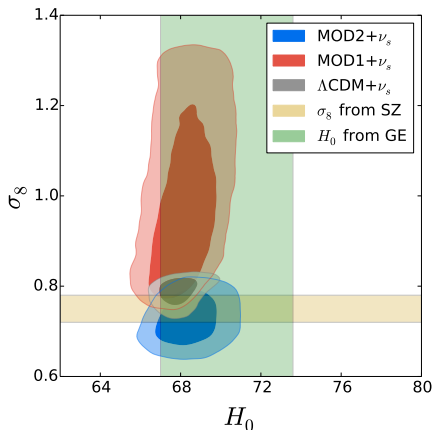
- CMB  $\rightarrow$  poor constraints on  $w_\Lambda$
- BAO/RSD, JLA  $\rightarrow$  preference for less DM today,  $w_\Lambda \simeq -1$

red points: CDE + LS $\nu$  models



Results - IV - What about LS $\nu$ ?

Degeneracy  $m_s^{\text{eff}} - \Omega_c h^2$  as expected  
for two dark matter components



No significant variations for the 2D  
contours in the  $\sigma_8 - H_0$  plane

Only upper limits for  $m_s^{\text{eff}} \Rightarrow$  LS $\nu$  is still disfavoured

# Conclusions

- Universe evolution explained well by  $\Lambda$ CDM model
  - ▶ cosmological constraints on standard particles (neutrinos) ✓
  - ▶ additional particles ?
  - ▶ tensions between cosmological and local measurements ( $H_0$ ,  $\sigma_8$ ) ✗
    - ★ unaccounted systematics or new physics ?
- $\nu$  oscillations anomalies at Short-Baseline distances
  - ▶ light ( $m_s \simeq 1$  eV) sterile neutrino (LS $\nu$ ) ?
  - ▶ LS $\nu$  can reduce  $H_0$  and  $\sigma_8$  tensions ✓
  - ▶ cosmological bounds disfavor a thermalized,  $m_s \simeq 1$  eV neutrino ✗
    - ★ new mechanisms suppress active-sterile oscillations in the early Universe ?
    - ★ new mechanisms compensate LS $\nu$  effects in cosmology ?
- CMB temperature spectrum at low- $\ell$ : inflationary freedom ?
  - ▶ primordial power spectrum can compensate LS $\nu$  effects in cosmology ✓
  - ▶ not if CMB polarization is included! ✗
- Coupling between Dark Matter (DM) and Dark Energy (DE) ?
  - ▶ can reduce  $H_0$  and  $\sigma_8$  tensions (DE $\rightarrow$ DM) ✓
  - ▶ LS $\nu$  bounds unchanged ✗

Thank you for the attention