

Very-Short-BaseLine Electron Neutrino Disappearance

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work in collaboration with

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Standard Model: Massless Neutrinos

- ▶ Standard Model: $\nu_L, \nu_R^c \implies$ no Dirac mass term $\mathcal{L}^D \sim m^D \nu_L \nu_R$
- ▶ Majorana Neutrino: $\nu^c = \nu$
- ▶ $\nu_R^c = \nu_R \implies$ Majorana mass term $\mathcal{L}^M \sim m^M \nu_L \nu_R^c$
- ▶ Standard Model: Majorana mass term **not** allowed by $SU(2)_L \times U(1)_Y$
(no Higgs triplet)

- ▶ Neutrinos are special in the Standard Model: the only **neutral fermions**
- ▶ In extensions of the SM neutrinos can mix with non-SM fermions:

$$L_L = \begin{pmatrix} \nu_{eL} \\ e_L \end{pmatrix} \quad \begin{pmatrix} I=1/2 \\ Y=-1 \end{pmatrix} \quad \Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \quad \begin{pmatrix} I=1/2 \\ Y=+1 \end{pmatrix} \quad \tilde{\Phi} = i\tau_2 \Phi^* \quad \begin{pmatrix} I=1/2 \\ Y=-1 \end{pmatrix}$$

non-SM chiral fermion field $f_R = f_L^C \quad \begin{pmatrix} I=0 \\ Y=0 \end{pmatrix}$

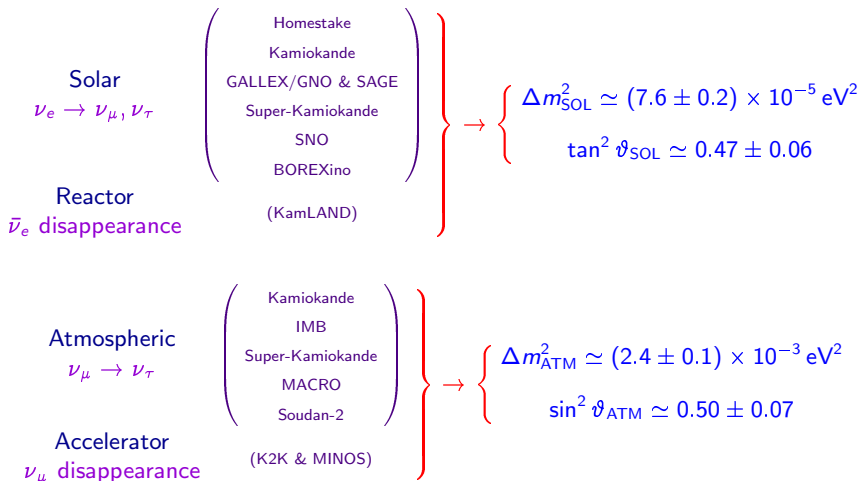
Dirac mass term $\sim \overline{L}_L \tilde{\Phi} f_R$ + Majorana mass term $\sim \overline{f_R^C} f_R$
 in some models f_R is called **right-handed neutrino**: $f_R \rightarrow \nu_R$

- ▶ If these non-SM fermions are light, they are called **sterile neutrinos**:

$$\nu_{sL} \equiv \nu_R^C$$

- ▶ Active neutrinos (ν_e, ν_μ, ν_τ) can oscillate into sterile neutrinos (ν_s)
- ▶ Extremely interesting window on physics beyond the SM
- ▶ Observable: **disappearance** of active neutrinos
- ▶ Many $\nu_e^{(-)}$ and $\nu_\mu^{(-)}$ disappearance experiments
- ▶ We focus on ν_e and $\bar{\nu}_e$ disappearance
- ▶ Gallium and MiniBooNE ν_e anomalies and reactor $\bar{\nu}_e$ data

Experimental Evidences of Neutrino Oscillations



Two scales of Δm^2 : $\Delta m_{\text{ATM}}^2 \simeq 30 \Delta m_{\text{SOL}}^2$

Large mixings: $\vartheta_{\text{ATM}} \simeq 45^\circ$, $\vartheta_{\text{SOL}} \simeq 34^\circ$

Three-Neutrino Mixing

$$\nu_{\alpha L} = \sum_{k=1}^3 U_{\alpha k} \nu_{kL} \quad (\alpha = e, \mu, \tau)$$

three flavor fields: ν_e, ν_μ, ν_τ

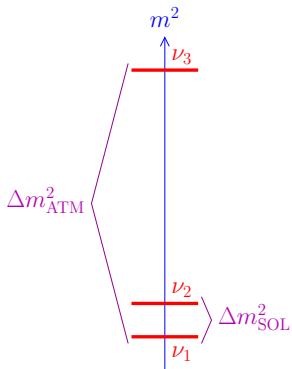
three massive fields: ν_1, ν_2, ν_3

$$\Delta m_{21}^2 + \Delta m_{32}^2 + \Delta m_{13}^2 = m_2^2 - m_1^2 + m_3^2 - m_2^2 + m_1^2 - m_3^2 = 0$$

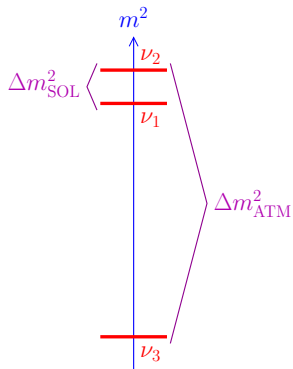
$$\Delta m_{\text{SOL}}^2 = \Delta m_{21}^2 \simeq (7.6 \pm 0.2) \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{\text{ATM}}^2 \simeq |\Delta m_{31}^2| \simeq |\Delta m_{32}^2| \simeq (2.4 \pm 0.1) \times 10^{-3} \text{ eV}^2$$

Allowed Three-Neutrino Schemes



"normal"



"inverted"

different signs of $\Delta m_{31}^2 \simeq \Delta m_{32}^2$

absolute scale is not determined by neutrino oscillation data

Gallium Anomaly

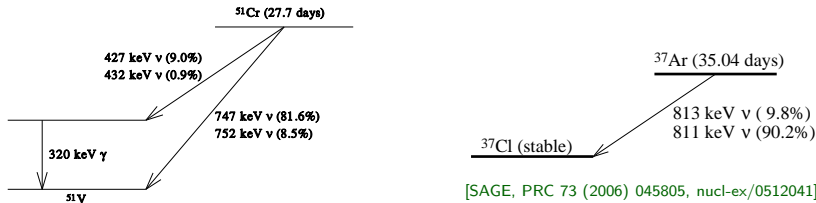
Gallium Radioactive Source Experiments

Tests of the solar neutrino detectors **GALLEX** (Cr1, Cr2) and **SAGE** (Cr, Ar)

Detection Process: $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$

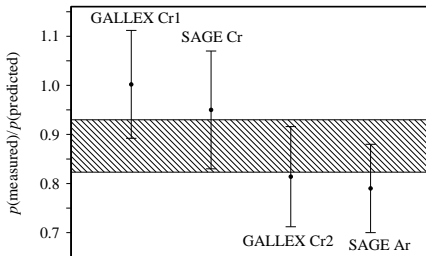
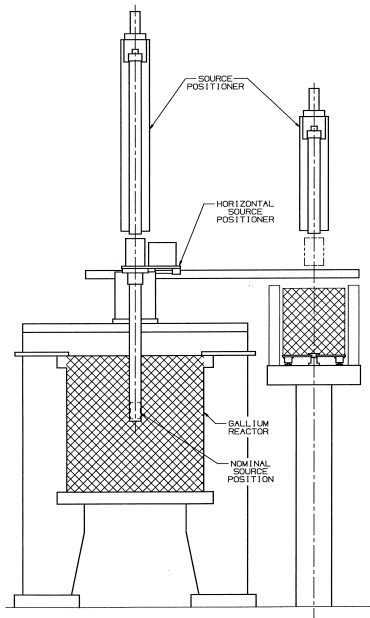
ν_e Sources: $e^- + {}^{51}\text{Cr} \rightarrow {}^{51}\text{V} + \nu_e$ $e^- + {}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl} + \nu_e$

	${}^{51}\text{Cr}$				${}^{37}\text{Ar}$	
E [keV]	747	752	427	432	811	813
B.R.	0.8163	0.0849	0.0895	0.0093	0.902	0.098



[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

[SAGE, PRC 59 (1999) 2246, hep-ph/9803418]

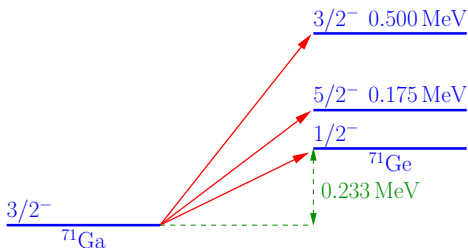


[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

$$R_{\text{Ga}} = 0.88 \pm 0.05$$

[SAGE, PRC 59 (1999) 2246, hep-ph/9803418]

- ▶ Deficit could be due to overestimate of $\sigma(\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-)$
- ▶ Calculation: Bahcall, PRC 56 (1997) 3391, hep-ph/9710491



- ▶ $\sigma_{\text{G.S.}}$ related to measured $\sigma(e^- + {}^{71}\text{Ge} \rightarrow {}^{71}\text{Ga} + \nu_e)$:

$$\sigma_{\text{G.S.}}({}^{51}\text{Cr}) = 55.3 \times 10^{-46} \text{ cm}^2 (1 \pm 0.004)_{3\sigma}$$

- ▶ $\sigma({}^{51}\text{Cr}) = \sigma_{\text{G.S.}}({}^{51}\text{Cr}) \left(1 + 0.669 \frac{\text{BGT}_{175 \text{ keV}}}{\text{BGT}_{\text{G.S.}}} + 0.220 \frac{\text{BGT}_{500 \text{ keV}}}{\text{BGT}_{\text{G.S.}}} \right)$

► Bahcall:

[Bahcall, PRC 56 (1997) 3391, hep-ph/9710491]

from $p + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + n$ measurements [Krofccheck et al., PRL 55 (1985) 1051]

$$\frac{\text{BGT}_{175\text{ keV}}}{\text{BGT}_{\text{G.S.}}} < 0.056 \Rightarrow \frac{\text{BGT}_{175\text{ keV}}}{\text{BGT}_{\text{G.S.}}} = \frac{0.056}{2} \quad \frac{\text{BGT}_{500\text{ keV}}}{\text{BGT}_{\text{G.S.}}} = 0.146$$

$$3\sigma \text{ lower limit: } \frac{\text{BGT}_{175\text{ keV}}}{\text{BGT}_{\text{G.S.}}} = \frac{\text{BGT}_{500\text{ keV}}}{\text{BGT}_{\text{G.S.}}} = 0$$

$$3\sigma \text{ upper limit: } \frac{\text{BGT}_{175\text{ keV}}}{\text{BGT}_{\text{G.S.}}} < 0.056 \times 2 \quad \frac{\text{BGT}_{500\text{ keV}}}{\text{BGT}_{\text{G.S.}}} = 0.146 \times 2$$

$$\sigma({}^{51}\text{Cr}) = 58.1 \times 10^{-46} \text{ cm}^2 \left(1_{-0.028}^{+0.036} \right)_{1\sigma}$$

► Haxton:

[Hata, Haxton, PLB 353 (1995) 422, nucl-th/9503017; Haxton, PLB 431 (1998) 110, nucl-th/9804011]

“a sophisticated shell model calculation is performed ... for the transition to the first excited state in ${}^{71}\text{Ge}$. The calculation predicts destructive interference between the (p, n) spin and spin-tensor matrix elements.”

$$\sigma({}^{51}\text{Cr}) = 63.9 \times 10^{-46} \text{ cm}^2 (1 \pm 0.106)_{1\sigma}$$

	GALLEX		SAGE	
	Cr1	Cr2	Cr	Ar
R	1.00 ± 0.10	0.81 ± 0.10	0.95 ± 0.12	0.79 ± 0.10
$\langle L \rangle$	1.9 m		0.6 m	

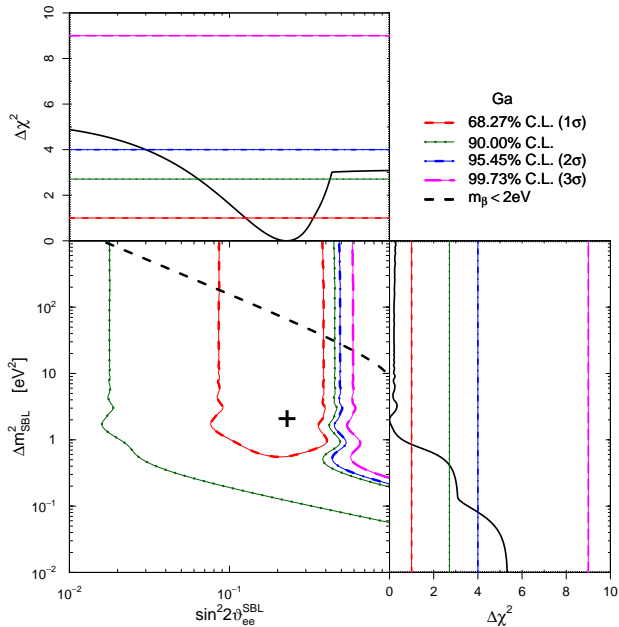
$$R_{\text{Ga}} = 0.88 \pm 0.05$$

[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

$$P_{\nu_e \rightarrow \nu_e}(L, E) = 1 - \sin^2 2\vartheta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

$$L_{\text{osc}} \lesssim 0.5 \text{ m} \implies \Delta m_{\text{SBL}}^2 \gtrsim 1 \text{ eV}^2 \implies \nu_e \rightarrow \nu_s$$

$$R = \frac{\int dV L^{-2} \sum_i (\text{B.R.})_i \sigma_i P_{\nu_e \rightarrow \nu_e}(L, E_i)}{\sum_i (\text{B.R.})_i \sigma_i \int dV L^{-2}}$$



$$\chi^2_{\min} = 2.94$$

$$\text{NdF} = 2$$

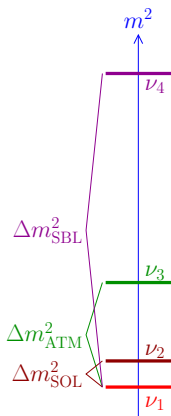
$$\text{GoF} = 23\%$$

$$\sin^2 2\vartheta = 0.22$$

$$\Delta m^2 = 1.98 \text{eV}^2$$

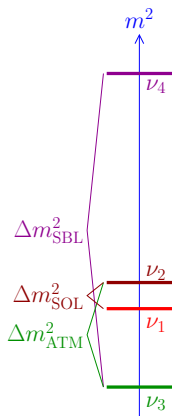
[Acero, C.G, Laveder, PRD 78 (2008) 073009, arXiv:0711.4222]

3+1 Four-Neutrino Mixing



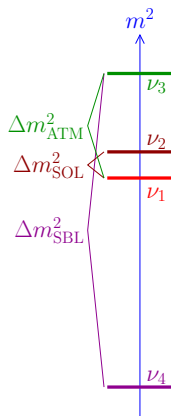
"normal"

$$|U_{e4}|^2 \ll 1$$



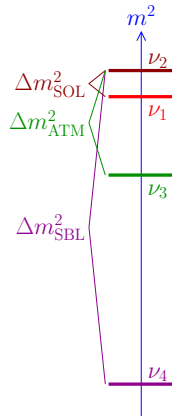
"3 ν -inverted"

$$|U_{\mu 4}|^2 \ll 1$$



"4 ν -inverted"

$$|U_{\tau 4}|^2 \ll 1$$



"fully-inverted"

$$|U_{s4}|^2 \simeq 1$$

$$P_{\nu_\alpha \rightarrow \nu_\beta}^{\text{SBL}} = \sin^2 2\vartheta_{\alpha\beta}^{\text{SBL}} \sin^2 \left(\frac{\Delta m_{\text{SBL}}^2 L}{4E} \right) \quad (\alpha \neq \beta)$$

$$\sin^2 2\vartheta_{\alpha\beta}^{\text{SBL}} = 4|U_{\alpha 4}|^2|U_{\beta 4}|^2$$

$$P_{\nu_\alpha \rightarrow \nu_\alpha}^{\text{SBL}} = 1 - \sin^2 2\vartheta_{\alpha\alpha}^{\text{SBL}} \sin^2 \left(\frac{\Delta m_{\text{SBL}}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\alpha}^{\text{SBL}} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

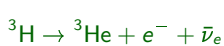
$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

$$\sin^2 2\vartheta_{ee}^{\text{SBL}} \simeq 0.22 \Rightarrow |U_{e4}|^2 \simeq 0.06$$

$$\sin^2 2\vartheta_{ee}^{\text{SBL}} \gtrsim 0.02 \Rightarrow |U_{e4}|^2 \gtrsim 0.005$$

↑
SBL

Tritium Beta-Decay

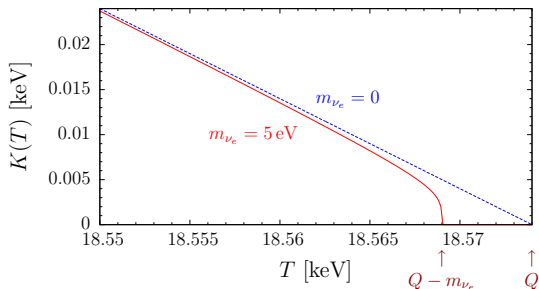


$$\frac{d\Gamma}{dT} = \frac{(\cos\vartheta_C G_F)^2}{2\pi^3} |\mathcal{M}|^2 F(E) p E (Q - T) \sqrt{(Q - T)^2 - m_{\nu_e}^2}$$

$$Q = M_{{}^3\text{H}} - M_{{}^3\text{He}} - m_e = 18.58 \text{ keV}$$

Kurie plot

$$K(T) = \sqrt{\frac{d\Gamma/dT}{\frac{(\cos\vartheta_C G_F)^2}{2\pi^3} |\mathcal{M}|^2 F(E) p E}} = \left[(Q - T) \sqrt{(Q - T)^2 - m_{\nu_e}^2} \right]^{1/2}$$



$$m_{\nu_e} < 2.2 \text{ eV} \quad (95\% \text{ C.L.})$$

Mainz & Troitsk

[Weinheimer, hep-ex/0210050]

future: KATRIN (start 2010)

[hep-ex/0109033] [hep-ex/0309007]

sensitivity: $m_{\nu_e} \simeq 0.2 \text{ eV}$

Neutrino Mixing: $m_{\nu_e} \implies m_\beta = \sqrt{\sum_k |U_{ek}|^2 m_k^2}$

4 ν -inverted and fully-inverted schemes

$$|U_{e1}|^2 + |U_{e2}|^2 + |U_{e3}|^2 \simeq 1 \qquad |U_{e4}|^2 \ll 1$$

$$m_\beta \simeq m_1 \simeq m_2 \simeq m_3 \simeq \sqrt{\Delta m_{\text{SBL}}^2}$$

$$\Delta m_{\text{SBL}}^2 \lesssim 5 \text{ eV}^2$$

Normal and 3ν -inverted schemes

$$m_\beta \lesssim 2 \text{ eV} \implies |U_{e4}|^2 m_4^2 \lesssim 4 \text{ eV}^2$$

$$m_4 \gg m_1, m_2, m_3 \implies m_4^2 \simeq \Delta m_{\text{SBL}}^2$$

$$\Delta m_{\text{SBL}}^2 \lesssim 4 |U_{e4}|^{-2} \text{ eV}^2$$

$$\sin^2 2\vartheta_{ee}^{\text{SBL}} = 4 |U_{e4}|^2 (1 - |U_{e4}|^2) \implies |U_{e4}|^2 = \frac{1}{2} \left(1 \pm \sqrt{1 - \sin^2 2\vartheta_{ee}^{\text{SBL}}} \right)$$

$$|U_{e4}|^2 < \frac{1}{2} \implies |U_{e4}|^2 = \frac{1}{2} \left(1 - \sqrt{1 - \sin^2 2\vartheta_{ee}^{\text{SBL}}} \right)$$

$$\Delta m_{\text{SBL}}^2 \lesssim \frac{8}{1 - \sqrt{1 - \sin^2 2\vartheta_{ee}^{\text{SBL}}}} \text{ eV}^2$$

$$\sin^2 2\vartheta_{ee}^{\text{SBL}} \gtrsim 0.02 \implies \Delta m_{\text{SBL}}^2 \lesssim 800 \text{ eV}^2$$

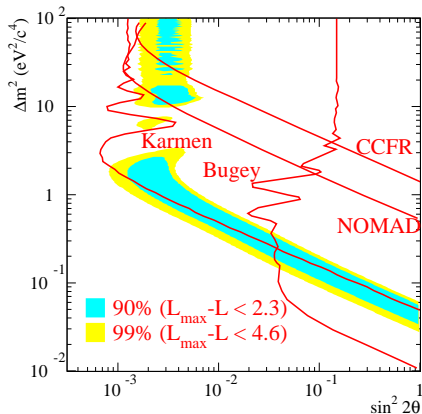
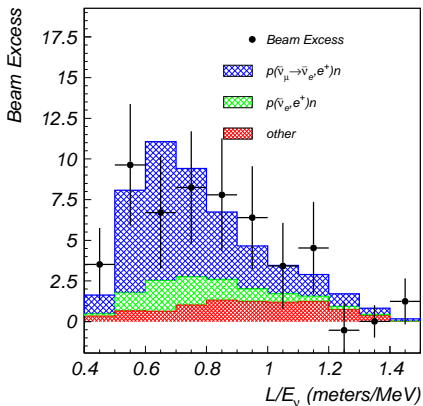
LSND

[PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 30 \text{ m}$$

$$20 \text{ MeV} \leq E \leq 200 \text{ MeV}$$



$$\Delta m_{\text{LSND}}^2 \gtrsim 0.2 \text{ eV}^2 \quad (\gg \Delta m_{\text{ATM}}^2 \gg \Delta m_{\text{SOL}}^2)$$

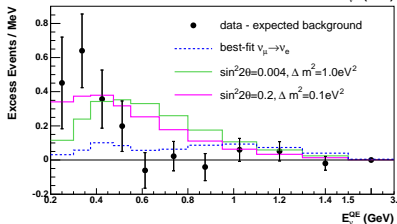
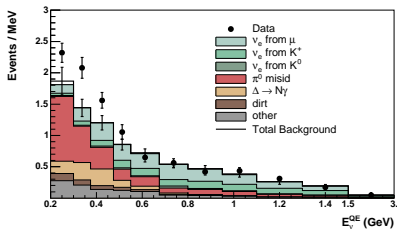
MiniBooNE

[PRL 98 (2007) 231801]

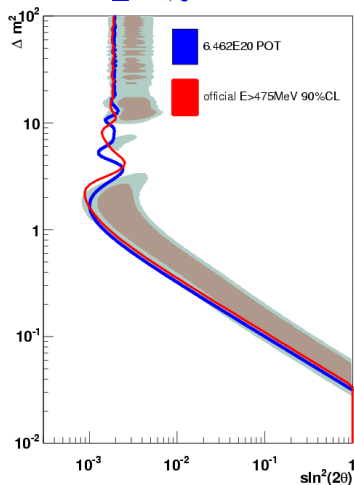
$$\nu_{\mu} \rightarrow \nu_e$$

$$L \simeq 541 \text{ m}$$

$$475 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$$



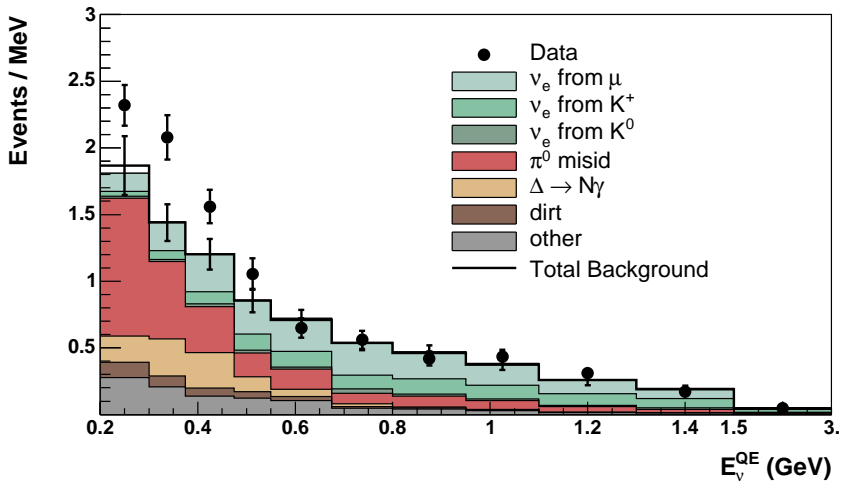
[PRL 102 (2009) 101802, arXiv:0812.2243]



[arXiv:0901.1648]

Low-Energy Anomaly!

MiniBooNE Low-Energy Anomaly



[PRL 102 (2009) 101802, arXiv:0812.2243]

$$N_{\nu,j}^{\text{the}} = f_{\nu} \left(P_{\nu_e \rightarrow \nu_e} N_{\nu_e,j}^{\text{cal}} + N_{\nu_{\mu},j}^{\text{cal}} \right)$$

$$N_{\nu_j}^{\text{the}} = f_{\nu} \left(P_{\nu_e \rightarrow \nu_e} N_{\nu_e j}^{\text{cal}} + N_{\nu_{\mu} j}^{\text{cal}} \right)$$

- ▶ Estimated 15% uncertainty of the calculated neutrino flux [MiniBooNE, PRD 79 (2009) 072002, arXiv:0806.1449] is consistent with measured ratio 1.21 ± 0.24 of detected and predicted charged-current quasi-elastic ν_{μ} events [MiniBooNE, PRL 100 (2008) 032301, arXiv:0706.0926]

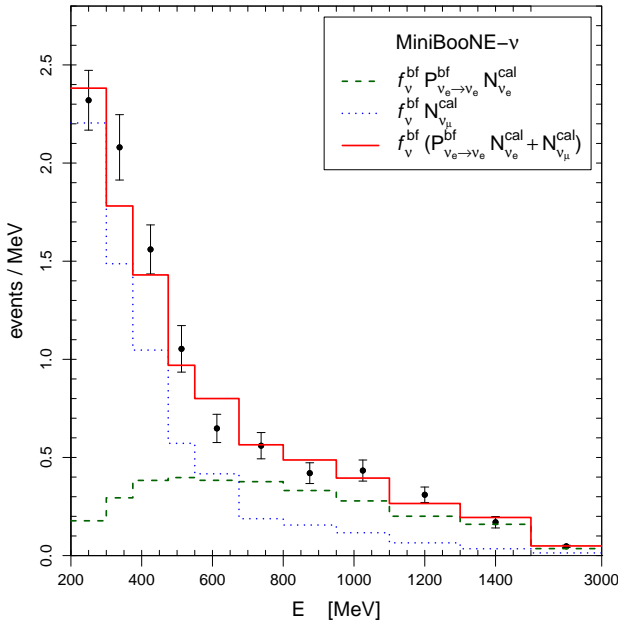
- ▶ We consider $\Delta m_{\text{SBL}}^2 \rightarrow \Delta m_{\text{VSBL}}^2 \gtrsim 20 \text{ eV}^2$

- ▶ $P_{\nu_e \rightarrow \nu_e}$ is practically constant in MiniBooNE

$$L_{\text{osc}}^{\text{MB}} = \frac{4\pi E}{\Delta m^2} \lesssim 400 \text{ m} < L^{\text{MB}} \simeq 541 \text{ m}$$

- ▶ Very-Short-BaseLine (VSBL) because oscillation length in Gallium Radioactive Source Experiments and Reactor Neutrino Experiments is extremely small:

$$L_{\text{osc}}(1 \text{ MeV}) \lesssim 10 \text{ cm}$$



[C.G. Laveder, PRD 80 (2009) 013005, arXiv:0902.1992]

No Osc.

$$\chi_{\min}^2 = 27.2$$

$$\text{NdF} = 10$$

$$\text{GoF} = 0.2\%$$

$$f_{\nu} = 1.15$$

Osc.

$$\chi_{\min}^2 = 17.7$$

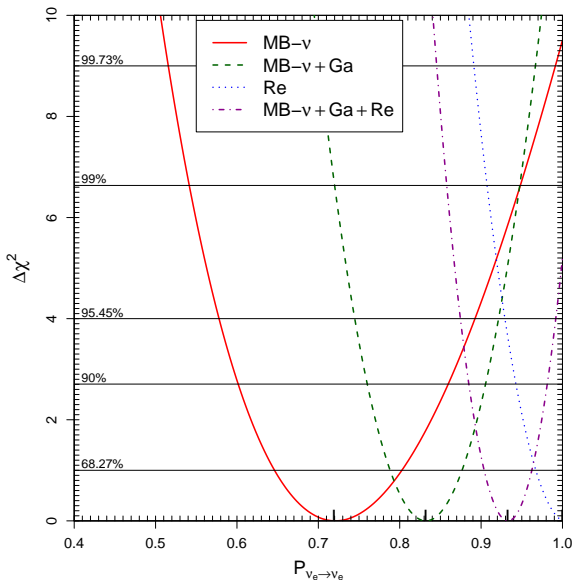
$$\text{NdF} = 9$$

$$\text{GoF} = 3.8\%$$

$$f_{\nu} = 1.31$$

$$P_{\nu_e \rightarrow \nu_e} = 0.72$$

MiniBooNE- ν + Gallium + Reactors



[C.G. Laveder, PRD 80 (2009) 013005, arXiv:0902.1992]

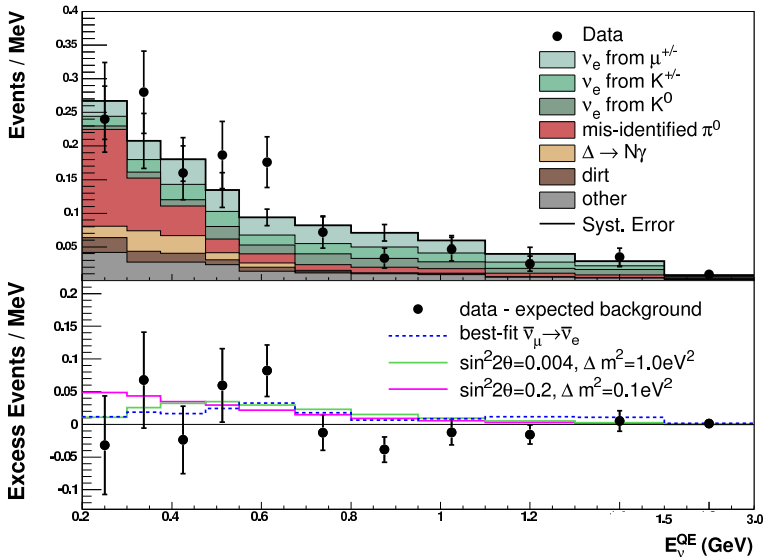
		MB- ν	MB- ν +Ga	Re	MB- ν +Ga+Re
No Osc.	χ_{\min}^2	27.2	34.0	2.9	36.9
	NDF	10	11	7	18
	GoF	0.2%	0.04%	89.8%	0.5%
	f_{ν}^{bf}	1.15	1.15		1.15
Osc.	χ_{\min}^2	17.7	20.1	2.9	31.7
	NDF	9	10	6	17
	GoF	3.8%	2.8%	82.7%	1.7%
	$P_{\nu_e \rightarrow \nu_e}^{\text{bf}}$	0.72	0.83	1.0	0.93
	f_{ν}^{bf}	1.31	1.24		1.19
PG	$\Delta\chi_{\min}^2$		2.4		11.1
	NDF		1		2
	GoF		12.4%		0.4%

[C.G. Laveder, PRD 80 (2009) 013005, arXiv:0902.1992]

PG = Parameter Goodness-of-fit

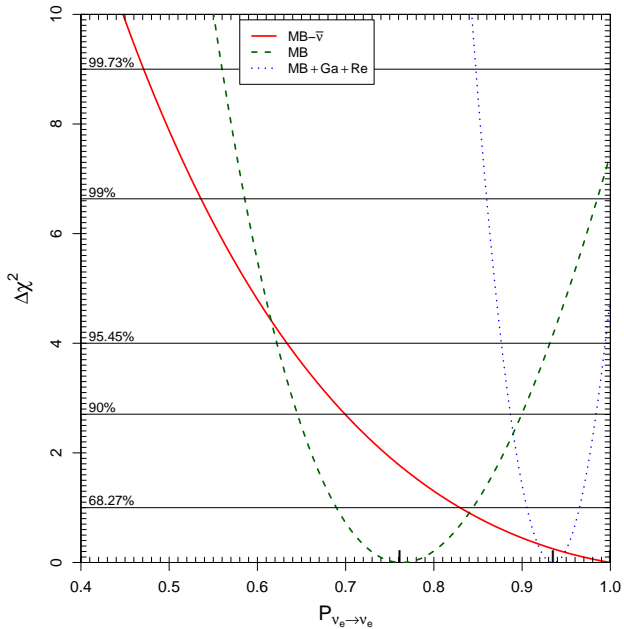
[Maltoni, Schwetz, PRD 68 (2003) 033020, hep-ph/0304176]

MiniBooNE Antineutrino Data



[PRL 103 (2009) 111801, arXiv:0904.1958]

No Low-Energy Anomaly!



[C.G. Laveder, PRD 80 (2009) 013005, arXiv:0902.1992]

		MB- $\bar{\nu}$	MB- $\bar{\nu}$ +Re	MB	MB+Ga+Re
No Osc.	χ_{\min}^2	16.9	19.8	44.1	53.8
	NDF	10	17	21	29
	GoF	7.6%	28.5%	0.2%	0.3%
	$f_{\bar{\nu}}^{\text{bf}}$	1.08	1.08	1.08	1.08
Osc.	χ_{\min}^2	16.9	19.8	36.7	48.9
	NDF	9	16	19	27
	GoF	5.0%	23.0%	0.9%	0.6%
	$P_{\nu_e \rightarrow \nu_e}^{\text{bf}}$	1.00	1.00	0.76	0.93
	$f_{\bar{\nu}}^{\text{bf}}$	1.08	1.08	1.19	1.10
	f_{ν}^{bf}			1.28	1.19
PG	$\Delta\chi_{\min}^2$		0.0	2.1	8.3
	NDF		1	1	3
	GoF		100.0%	14.8%	4.1%

$$N_{\nu,j}^{\text{the}} = f_{\nu} \left(P_{\nu_e \rightarrow \nu_e} N_{\nu_e,j}^{\text{cal}} + N_{\nu_{\mu},j}^{\text{cal}} \right) \quad N_{\bar{\nu},j}^{\text{the}} = f_{\bar{\nu}} \left(P_{\nu_e \rightarrow \nu_e} N_{\bar{\nu}_e,j}^{\text{cal}} + N_{\bar{\nu}_{\mu},j}^{\text{cal}} \right)$$

[C.G. Laveder, PRD 80 (2009) 013005, arXiv:0902.1992]

Tension between neutrino and antineutrino data could be due to:

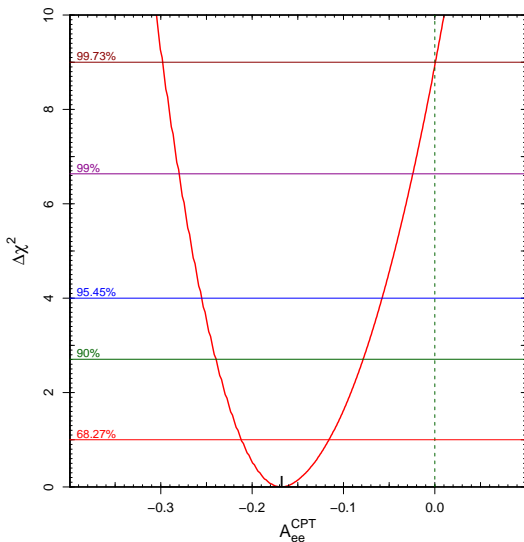
- ▶ Statistical fluctuations.
- ▶ Underestimate of systematic uncertainties.
- ▶ Our hypothesis of VSBL ν_e disappearance is excluded.
- ▶ Violation of CPT symmetry: $P_{\nu_e \rightarrow \nu_e} \neq P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}$.

$$\nu_\alpha \rightarrow \nu_\beta \xrightarrow{\text{CP}} \nu_{\bar{\alpha}} \rightarrow \nu_{\bar{\beta}} \xrightarrow{\text{T}} \nu_{\bar{\beta}} \rightarrow \nu_{\bar{\alpha}}$$

$$\text{CPT} \implies \boxed{P_{\nu_\alpha \rightarrow \nu_\beta} = P_{\nu_{\bar{\beta}} \rightarrow \nu_{\bar{\alpha}}}}$$

$$\alpha = \beta \implies \boxed{P_{\nu_\alpha \rightarrow \nu_\alpha} = P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\alpha}}$$

CPT Violation?



[C.G. Laveder, PRD 80 (2009) 013005, arXiv:0902.1992]

$$A_{ee}^{\text{CPT}} \equiv P_{\nu_e \rightarrow \nu_e} - P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}$$

$$\chi_{\min}^2 = 39.9$$

$$\text{NdF} = 26$$

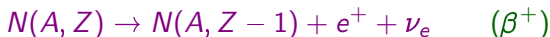
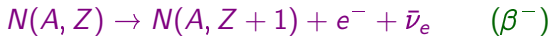
$$\text{GoF} = 4.0\%$$

$$A_{ee}^{\text{CPT}} = -0.17$$

Future Tests of (V)SBL ν_e and $\bar{\nu}_e$ Disappearance

The hypothesis of VSBL ν_e disappearance can be tested with high accuracy by future experiments with pure well-known electron neutrino beams:

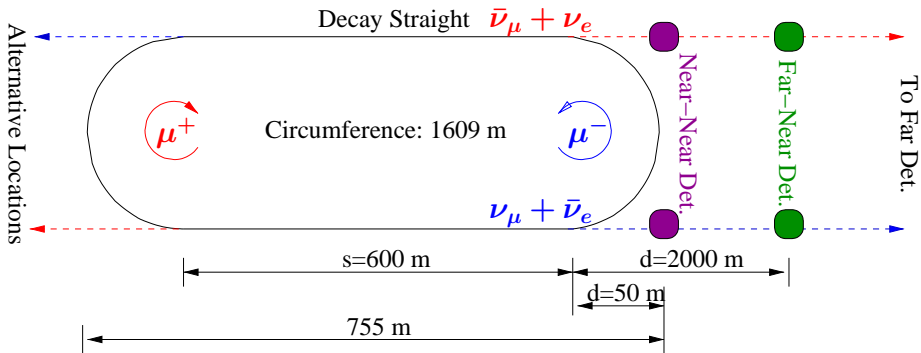
- ▶ SAGE collaboration is planning a new source experiment (ν_e)
- ▶ Beta-Beam experiments:



- ▶ Neutrino Factory experiments:



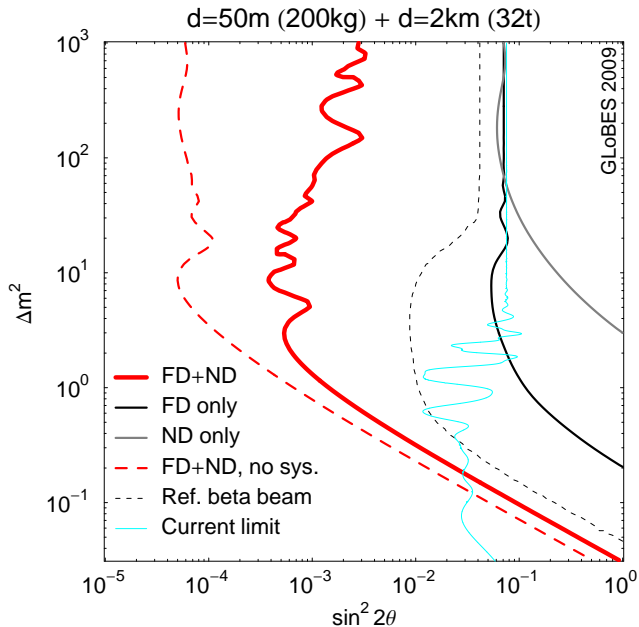
Neutrino Factory



[C.G, Laveder, Winter, PRD 80 (2009) 073005, arXiv:0907.5487]

Near Detectors: Scintillator or Iron Calorimeter
with perfect flavor identification

Systematic Uncertainties: Cross Section, Detector Normalization,
Energy Resolution and Calibration,
Backgrounds



[C.G. Laveder, Winter, PRD 80 (2009) 073005, arXiv:0907.5487]

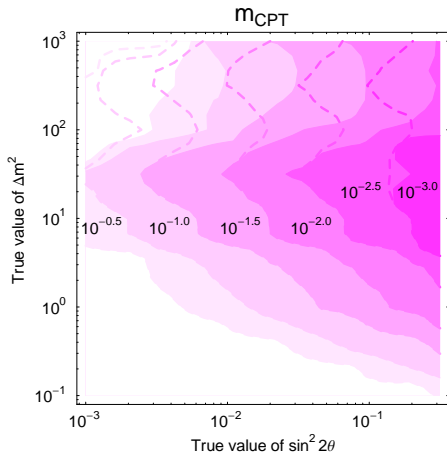
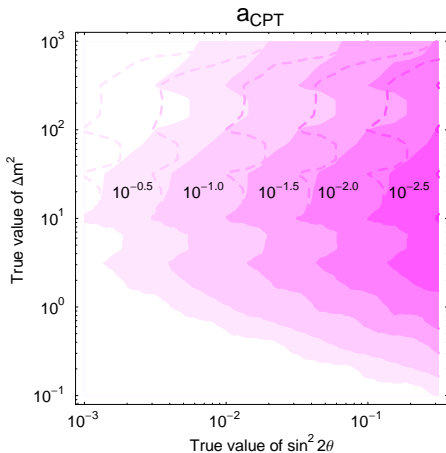
CPT Violation?

$$P_{\nu_e \rightarrow \nu_e} = 1 - \sin^2 2\vartheta_\nu \sin^2 \left(\frac{\Delta m_\nu^2 L}{4E} \right)$$

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} = 1 - \sin^2 2\vartheta_{\bar{\nu}} \sin^2 \left(\frac{\Delta m_{\bar{\nu}}^2 L}{4E} \right)$$

$$a_{\text{CPT}} \equiv \frac{\vartheta_\nu - \vartheta_{\bar{\nu}}}{\vartheta_\nu + \vartheta_{\bar{\nu}}}$$

$$m_{\text{CPT}} \equiv \frac{\Delta m_\nu^2 - \Delta m_{\bar{\nu}}^2}{\Delta m_\nu^2 + \Delta m_{\bar{\nu}}^2}$$



[C.G. Laveder, Winter, PRD 80 (2009) 073005, arXiv:0907.5487]

$$10^{-0.5} \simeq 0.3 \quad 10^{-1.5} \simeq 0.03 \quad 10^{-2.5} \simeq 0.003$$

dashed lines: no averaging over decay straights

Conclusions

- ▶ The Gallium anomaly may be due to $\nu_e \rightarrow \nu_s$ oscillations with $\sin^2 2\vartheta \gtrsim 0.1$ and $1 \text{ eV}^2 \lesssim \Delta m^2 \lesssim 800 \text{ eV}^2$
- ▶ These transitions may explain the MiniBooNE Low-Energy-Anomaly
- ▶ Tension between neutrino and antineutrino data could be an indication of CPT violation ($P_{\nu_e \rightarrow \nu_e} \neq P_{\bar{\nu}_e \rightarrow \bar{\nu}_e}$)
- ▶ (V)SBL ν_e and $\bar{\nu}_e$ disappearance can be checked in future
 - ▶ Beta-Beam experiments (pure ν_e or $\bar{\nu}_e$ beam from nuclear decay)
 - ▶ Neutrino Factory experiments (ν_e and $\bar{\nu}_\mu$ from μ^+ decay, or $\bar{\nu}_e$ and ν_μ from μ^- decay), which can test also CPT violation.