

Fasi della QCD,
modelli di teoria dei campi e teoria del trasporto:
un approccio sistematico
alla fenomenologia degli ioni pesanti all'LHC

Partecipanti al progetto

6 - Risorse umane da impegnare nelle attività dell'Unità di Ricerca

6.1 - Personale a tempo indeterminato (A.1.1) e/o determinato (A.1.2)

Personale dipendente dell'Istituzione, sede dell'Unità di ricerca

n°	Cognome	Nome	Dipartimento/Istituto/ Divisione/Settore	Qualifica	Tipologia	Mesi/ uomo	Costo
1.	BARBARO	Maria Benedetta	FISICA TEORICA	Professore Associato non confermato	Tempo Indeterminato	16	80.000
TOTALE						16	80.000

Personale docente esterno alla sede dell'Unità di ricerca

n°	Cognome	Nome	Ente / Istituzione / Impresa	Dipartimento/Istituto/ Divisione/Settore	Qualifica	Tipologia	Mesi/ uomo	Costo
TOTALE							0	0

Personale di Enti/Istituzioni/Imprese esterno alla sede dell'Unità di ricerca

n°	Cognome	Nome	Ente / Istituzione / Impresa	Dipartimento/Istituto/ Divisione/Settore	Qualifica	Tipologia	Mesi/ uomo	Costo
1.	MONTENO	Marco	Istituto Nazionale di Fisica Nucleare		Primo ricercatore	Tempo Indeterminato	24	80.000
2.	DE PACE	Arturo	Istituto Nazionale di Fisica Nucleare		Primo ricercatore	Tempo Indeterminato	12	40.000
3.	NARDI	Marzia	Istituto Nazionale di Fisica Nucleare		Ricercatore a tempo det.	Tempo Determinato	24	0
TOTALE							60	120.000

6.2 -Assegnisti, dottorandi, post-doc e borsisti (A.2) - Già acquisiti con altri fondi e saltuariamente impiegato nel Progetto di Ricerca

n°	Cognome	Nome	Università	Dipartimento/Istituto	Qualifica	Mesi/ uomo
1.	BERAUDO	Andrea	Università degli Studi di TORINO	FISICA TEORICA	Assegnista	26
2.	ORTONA	Giacomo	Università degli Studi di TORINO		Dottorando	24

Purposes of the project (I)

- ❖ study the **microscopic origin** of the “nearly perfect fluid” behavior of QGP
- ❖ study the impact of a **finite shear viscosity** on various observables
- ❖ understand if the plasma to be created at LHC energies belongs to a **new phase**, with respect to the highly non-perturbative one created at RHIC
- ❖ two research units: University of Catania and Torino
 - ➡ more **theoretical** point of view (Torino)
 - ➡ more **phenomenological** point of view (Catania)

Purposes of the project (II)

- ❖ in particular:
 - ➡ development of **field-theoretical microscopic models** under the guidance of the **numerical lattice QCD results**
 - ➡ identify the **relevant degrees of freedom** in the different temperature/density regimes
 - ➡ provide a theoretical ground on which **a transport theory incorporating the field interactions** can be constructed
- ❖ verify the effects that the new proposed theoretical ideas have on the experimental observations at RHIC and at the upcoming LHC
- ❖ the study will be extended to **heavy flavors**
 - ➡ relevant at the LHC energies

Specific tasks of the Torino research unit

- ❖ Development of **phenomenological models** for QCD thermodynamics
 - ➡ capture the main features of QCD in a certain regime
 - ➡ reach **regions of the phase diagram** where lattice QCD cannot go
 - ➡ give an interpretation of lattice data in terms of **effective degrees of freedom**

- ❖ quarkonia correlators in a thermal medium

- ❖ effects of the **color glass condensate** on the dynamical evolution of the system

What happens below T_c ?

- ❖ At low T and $\mu = 0$, QCD thermodynamics is dominated by **pions**
- ❖ The interaction between pions is **suppressed**
 - ➡ chiral perturbation theory: **pion contribution** to the thermodynamic potential
 - ➡ the energy density of pions from **3-loop ChPT** differs only less than 15% from the **ideal gas value**
P. Gerber and H. Leutwyler (1989)
- ❖ as T increases, heavier hadrons start to contribute
- ❖ for $T \geq 140 \text{ MeV}$ heavy states dominate the energy density

Why HRG?

- ❖ In the **virial expansion**, the partition function can be split into a **non-interacting** piece and a piece which includes **all interactions**
- ❖ **virial expansion** and experimental information on **scattering phase shift**
Prakash and Venugopalan (1992)
 - ➡ interplay between **attractive** and **repulsive** interaction

Interacting hadronic matter
can be well approximated by
a **non-interacting** gas of **resonances**

Features of HRG model

- ❖ An **increase of energy** in the system has three consequences:
 - ➡ a fixed temperature limit $T \rightarrow T_H$;
 - ➡ the momenta of the constituents do not continue to increase;
 - ➡ more and more species of **heavier particles** appear

New, non-kinetic way to use energy:
increasing the **number of species**
not the momentum per particle

- ❖ $T_H \simeq 150 - 200 \text{ MeV}$: critical temperature for transition to quark matter
Hagedorn and Rafelsky (1981); Blanchard, Fortunato and Satz (2004).

Partition function of HRG model

❖ The pressure can be written as

$$p^{HRG}/T^4 = \frac{1}{VT^3} \sum_{i \in \text{mesons}} \ln Z_{m_i}^M(T, V, \mu_{X^a}) + \frac{1}{VT^3} \sum_{i \in \text{baryons}} \ln Z_{m_i}^B(T, V, \mu_{X^a}),$$

where

$$\ln Z_{m_i}^{M/B} = \mp \frac{V d_i}{2\pi^2} \int_0^\infty dk k^2 \ln(1 \mp z_i e^{-\varepsilon_i/T}),$$

with energies $\varepsilon_i = \sqrt{k^2 + m_i^2}$, degeneracy factors d_i and fugacities

$$z_i = \exp\left(\left(\sum_a X_i^a \mu_{X^a}\right)/T\right).$$

X^a : all possible conserved charges, including the baryon number B , electric charge Q , strangeness S .

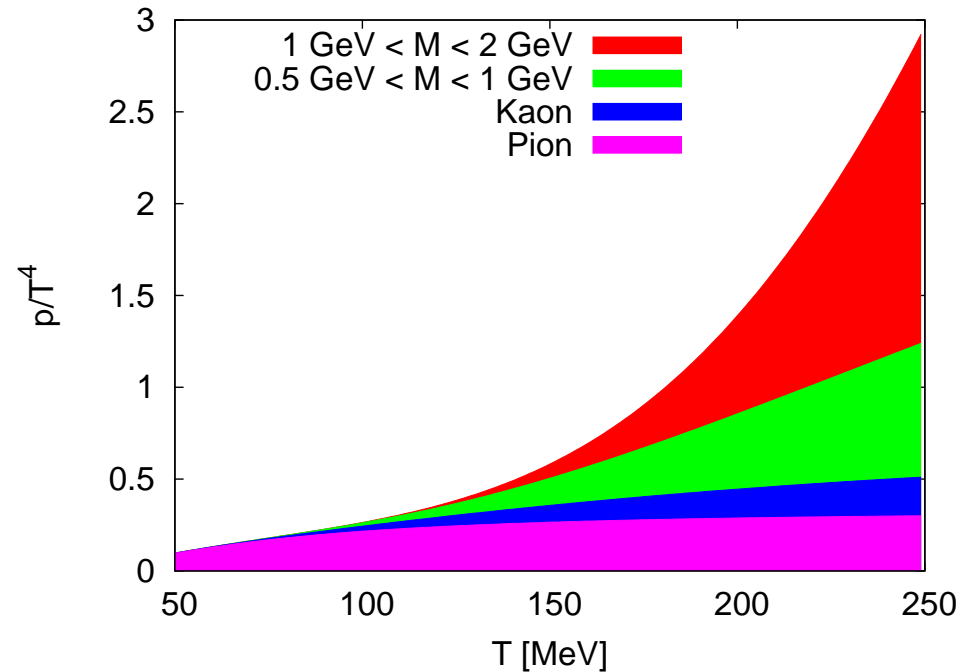
F. Karsch, A. Tawfik, K. Redlich; S. Ejiri, F. Karsch, K. Redlich

Hadronic species from the Particle Data Book

hadron	m_i (GeV)	d_i	B_i	S_i	I_i	hadron	m_i (GeV)	d_i	B_i	S_i	I_i
π	0.140	3	0	0	1	N (1535)	1.530	4	1	0	1/2
K	0.496	2	0	1	1/2	π_1 (1600)	1.596	9	0	0	1
\overline{K}	0.496	2	0	-1	1/2	Δ (1600)	1.600	16	1	0	3/2
η	0.543	1	0	0	0	Λ (1600)	1.600	2	1	-1	0
ρ	0.776	9	0	0	1	Δ (1620)	1.630	8	1	0	3/2
ω	0.782	3	0	0	0	η_2 (1645)	1.617	5	0	0	0
K^*	0.892	6	0	1	1/2	N (1650)	1.655	4	1	0	1/2
\overline{K}^*	0.892	6	0	-1	1/2	ω (1650)	1.670	3	0	0	0
N	0.939	4	1	0	1/2	Σ (1660)	1.660	6	1	-1	1
η'	0.958	1	0	0	0	Λ (1670)	1.670	2	1	-1	0
f_0	0.980	1	0	0	0	Σ (1670)	1.670	2	1	-1	1
a_0	0.980	3	0	0	1	ω_3 (1670)	1.667	7	0	0	0
ϕ	1.020	3	0	0	0	π_2 (1670)	1.672	15	0	0	1
Λ	1.116	2	1	-1	0	Ω^-	1.672	4	1	-3	0
h_1	1.170	3	0	0	1	N (1675)	1.675	12	1	0	1/2
Σ	1.189	6	1	-1	1	ϕ (1680)	1.680	3	0	0	0
a_1	1.230	9	0	0	1	K^* (1680)	1.717	6	0	1	1/2
b_1	1.230	9	0	0	1	\overline{K}^* (1680)	1.717	6	0	-1	1/2
Δ	1.232	16	1	0	3/2	N (1680)	1.685	12	1	0	1/2
f_2	1.270	5	0	0	0	ρ_3 (1690)	1.688	21	0	0	1
K_1	1.273	6	0	1	1/2	Λ (1690)	1.690	4	1	-1	0
\overline{K}_1	1.273	6	0	-1	1/2	Ξ (1690)	1.690	8	1	-2	1/2
f_1	1.285	3	0	0	1	ρ (1700)	1.720	9	0	0	1
η (1295)	1.295	1	0	0	0	N (1700)	1.700	8	1	0	1/2
π (1300)	1.300	3	0	0	1	Δ (1700)	1.700	16	1	0	3/2

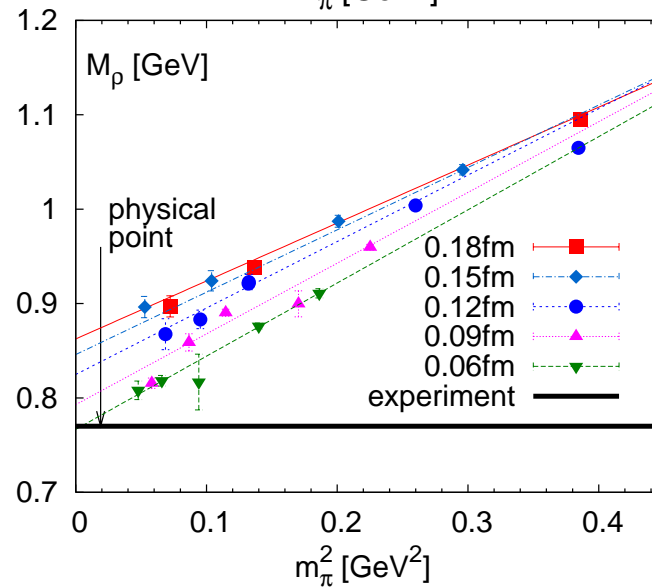
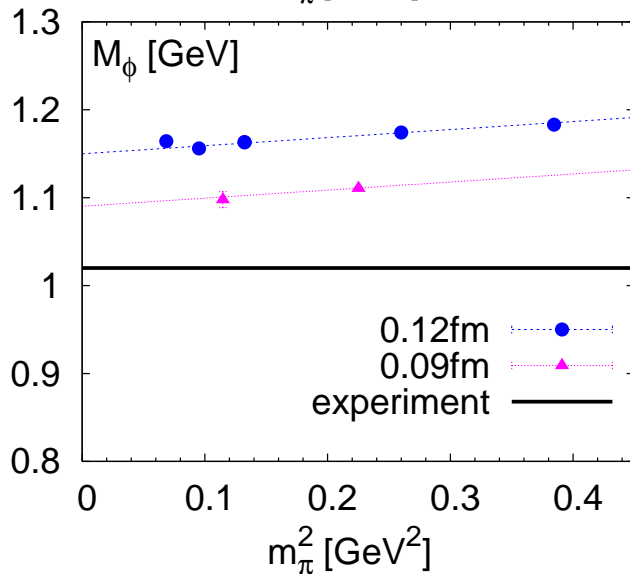
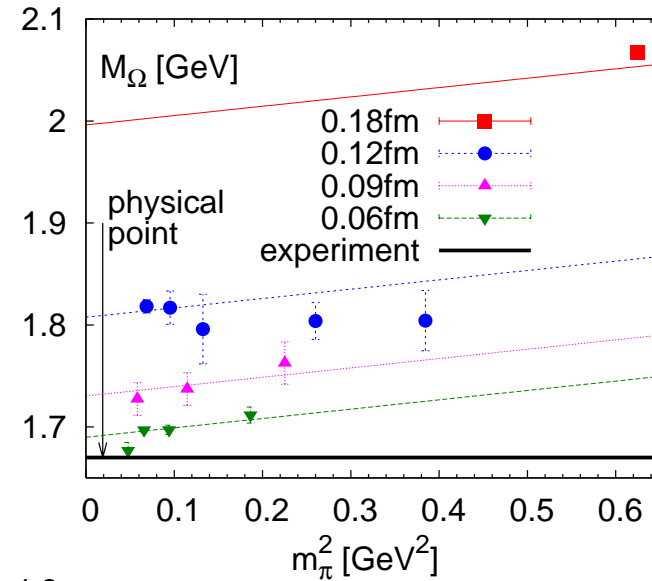
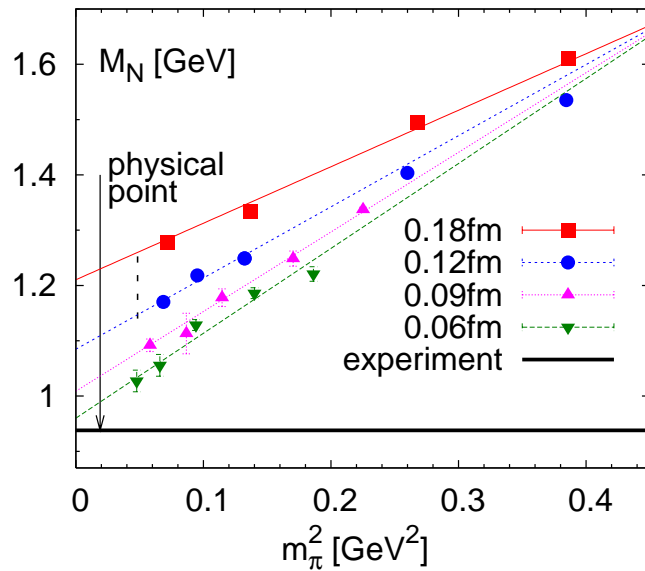
How many resonances do we include?

- ❖ With different mass cutoffs we can separate the contributions of different particles



- ❖ **No visible difference** between cuts at **2 GeV** and **2.5 GeV** in **our temperature regime**
- ❖ We include all resonances with $M \leq 2.5$ GeV
 - ➡ $\simeq 170$ different masses \leftrightarrow **1500 resonances**

Discretization effects



C. W. Bernard *et al.*, PRD (2001), C. Aubin *et al.*, PRD (2004), A. Bazavov *et al.*, 0903.3598.

Hadron masses

❖ Non-strange baryons and mesons:

$$r_1 m = r_1 m_0 + \frac{a_1 (r_1 m_\pi)^2}{1 + a_2 x} + \frac{b_1 x}{1 + b_2 x}, \quad x = \left(\frac{a}{r_1}\right)^2$$

❖ Strange baryons and mesons:

$$r_1 \cdot m_\Lambda(a, m_\pi) = r_1 m_\Lambda^{phys} + \frac{2}{3} \frac{a_1 (r_1 m_\pi)^2}{1 + a_2 x} + \frac{b_1 x}{1 + b_2 x} + \frac{r_1 \cdot (m_\Lambda^{phys} - m_p^{phys})}{1 + a_2 x} \left(\frac{m_s}{m_s^{phys}}\right),$$

$$r_1 \cdot m_\Sigma(a, m_\pi) = r_1 m_\Sigma^{phys} + \frac{1}{3} \frac{a_1 (r_1 m_\pi)^2}{1 + a_2 x} + \frac{b_1 x}{1 + b_2 x} + \frac{r_1 \cdot (m_\Sigma^{phys} - m_p^{phys})}{1 + a_2 x} \left(\frac{m_s}{m_s^{phys}}\right),$$

$$r_1 \cdot m_\Xi(a, m_\pi) = m_\Xi^{phys} + \frac{1}{3} \frac{a_1 (r_1 m_\pi)^2}{1 + a_2 x} + \frac{b_1 x}{1 + b_2 x} + \frac{r_1 \cdot (m_\Xi^{phys} - m_p^{phys})}{1 + a_2 x} \left(\frac{m_s}{m_s^{phys}}\right)$$

$$r_1 m_\Omega(a, m_\pi) = r_1 m_\Omega^{phys} + a_1 (r_1 m_\pi)^2 - a_1 (r_1 m_\pi^{phys})^2 + b_1 x + (m_\Omega^{phys} - m_\Delta^{phys}) \cdot 1.02 x$$

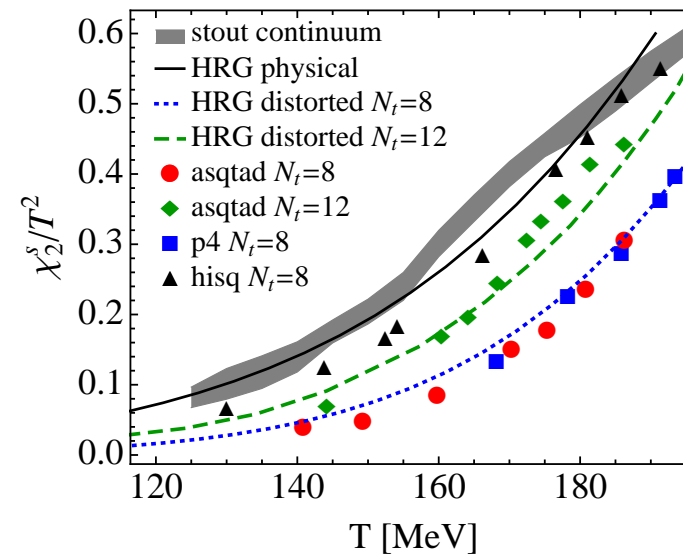
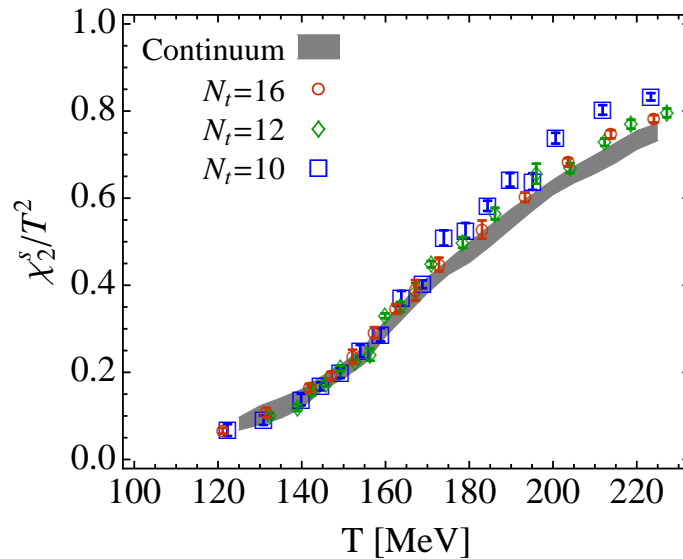
❖ **Distorted spectrum** implemented in the HRG model

❖ Assumption: **all resonances behave as their fundamental states**

P. Huovinen and P. Petreczky (2009).

Results: strangeness susceptibilities

$$\chi_n^S = T^n \frac{\partial^n p(T, \mu_B, \mu_S, \mu_I)}{\partial \mu_S^n} \Big|_{\mu_X=0}$$

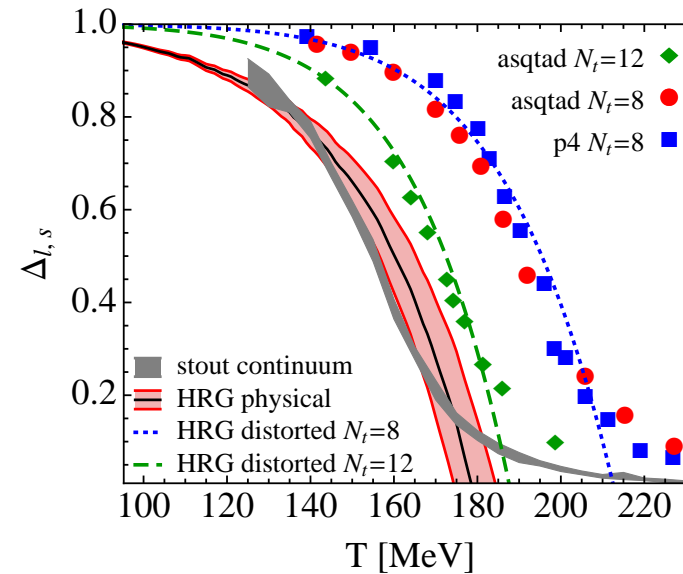
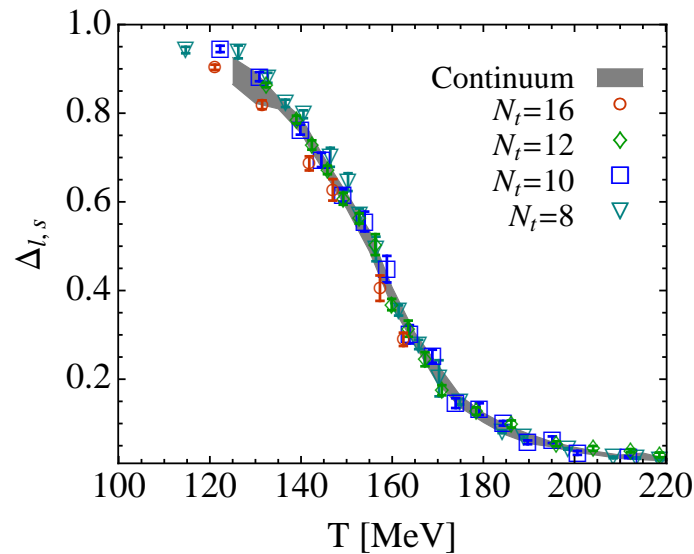


- ❖ HRG results in **good agreement** with stout action
- ❖ asqtad and p4 results show **similar shape** but **shift in temperature**
 - ➡ HRG results with corresponding **distorted spectrum** reproduce asqtad and p4 results

S. Borsanyi *et al.*, JHEP1009 (2010)

Results: subtracted chiral condensate

$$\Delta_{l,s} = \frac{\langle \bar{\psi}\psi \rangle_{l,T} - \frac{m_l}{m_s} \langle \bar{\psi}\psi \rangle_{s,T}}{\langle \bar{\psi}\psi \rangle_{l,0} - \frac{m_l}{m_s} \langle \bar{\psi}\psi \rangle_{s,0}}$$

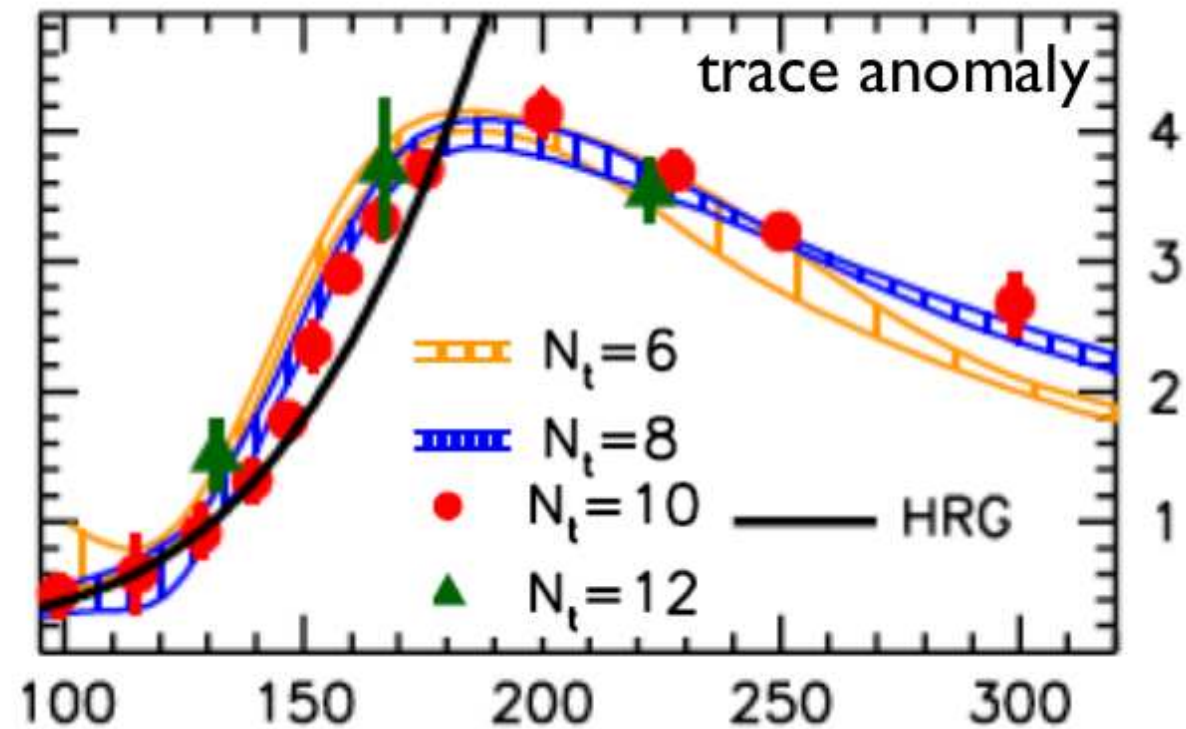


$$\langle \bar{\psi}\psi \rangle_s = \langle \bar{\psi}\psi \rangle_{s,0} + \langle \bar{\psi}\psi \rangle_K + \sum_{i \in \text{mesons}} \frac{\partial \ln Z_{m_i}^M}{\partial m_i} \frac{\partial m_i}{\partial m_s} + \sum_{i \in \text{baryons}} \frac{\partial \ln Z_{m_i}^B}{\partial m_i} \frac{\partial m_i}{\partial m_s}.$$

◆ $\frac{\partial m_i}{\partial m_s}$ from fit to lattice data [Camalich, Geng and Vacas \(2010\)](#)

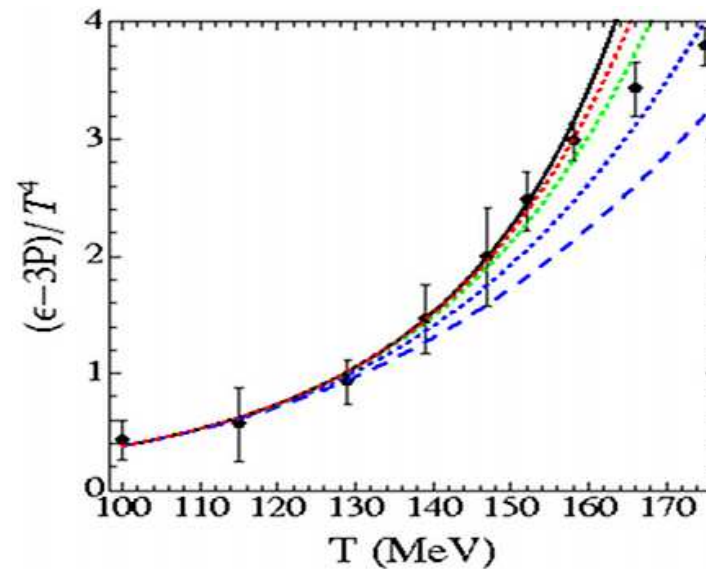
[S. Borsanyi et al., JHEP1009 \(2010\)](#)

Results: trace anomaly



❖ Very good agreement between HRG and lattice results

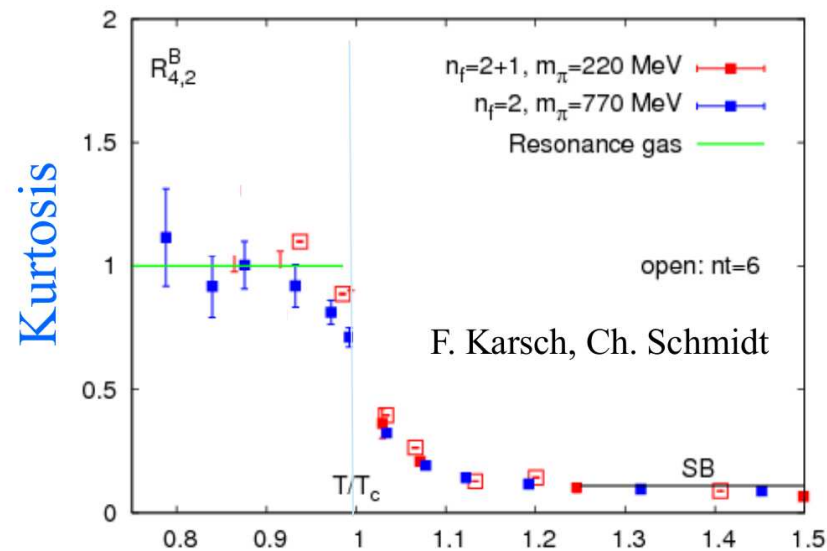
Inclusion of exponential spectrum in HRG model



- ❖ For large masses few states are known experimentally
- ❖ Inclusion of exponentially growing hadron mass spectrum
 J. Noronha-Hostler, C. Greiner, I. Shovkovy (2008); J. Noronha-Hostler, M. Beitel, C. Greiner, I. Shovkovy (2010)
- ❖ Agreement between lattice and HRG improved up to $T \sim 155$ MeV
 (A. Majumder, B. Müller: 1008.1747)

Open questions

- ❖ **Up to which temperature** should we describe the system in terms of the HRG model?
- ❖ $T_c \simeq 155 \text{ MeV}$, transition is a crossover
 - ➡ one should expect **deviations from HRG** already below T_c



$$R_{4,2}^B = \frac{C_4^B}{C_2^B}, \quad C_n^B = \frac{\partial^n p}{\partial \mu_B^n}$$